

29/01/2025

Evening



Aakash

Medical | IIT-JEE | Foundations

Corporate Office : AESL, 3rd Floor, Incuspaze Campus-2, Plot-13, Sector-18, Udyog Vihar,
Gurugram, Haryana-122018

Memory Based Answers & Solutions

Time : 3 hrs.

for

M.M. : 300

JEE (Main)-2025 (Online) Phase-1

(Physics, Chemistry and Mathematics)

IMPORTANT INSTRUCTIONS:

- (1) The test is of **3 hours** duration.
- (2) This test paper consists of 75 questions. Each subject (PCM) has 25 questions. The maximum marks are 300.
- (3) This question paper contains **Three Parts**. **Part-A** is Physics, **Part-B** is Chemistry and **Part-C** is **Mathematics**. Each part has only two sections: **Section-A** and **Section-B**.
- (4) **Section - A** : Attempt all questions.
- (5) **Section - B** : Attempt all questions.
- (6) **Section - A (01 – 20)** contains 20 multiple choice questions which have **only one correct answer**. Each question carries **+4 marks** for correct answer and **-1 mark** for wrong answer.
- (7) **Section - B (21 – 25)** contains 5 **Numerical value** based questions. The answer to each question should be rounded off to the **nearest integer**. Each question carries **+4 marks** for correct answer and **-1 mark** for wrong answer.

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JEE (Advanced) 2024

AIR	Name	Classroom
25	Rishi Shekher Shukla	2 Year Classroom
67	Krishna Sai Shishir	2 Year Classroom
78	Abhishek Jain	2 Year Classroom
93	Hardik Aggarwal	2 Year Classroom
95	Ujjwal Singh	2 Year Classroom
98	Rachit Aggarwal	2 Year Classroom

JEE (Main) 2024

AIR	Name	Classroom	State
1	Sarvvi Jais	2 Year Classroom	Karnataka Topper
15	M Sai Divya Tuja Reddy	2 Year Classroom	Telangana Topper
19	Rishi Shekher Shukla	2 Year Classroom	Telangana Topper

Sol. $L = mvr$

$$L = m\sqrt{\frac{GM}{r}}r$$

$$L = m\sqrt{GMr}$$

$$\frac{L_B}{L_A} = \frac{1}{4\sqrt{3}} \cdot \frac{1}{2} = \frac{1}{8\sqrt{3}}$$

9. A capacitor $C_1 = 6 \mu\text{F}$, initially charged with a cell of emf 5V is disconnected and connected to another capacitor $C_2 = 12 \mu\text{F}$ which is initially neutral. The charges on C_1 and C_2 after connection are

- (1) $0 \mu\text{C}, 30 \mu\text{C}$ (2) $10 \mu\text{C}, 20 \mu\text{C}$
(3) $20 \mu\text{C}, 10 \mu\text{C}$ (4) $30 \mu\text{C}, 0 \mu\text{C}$

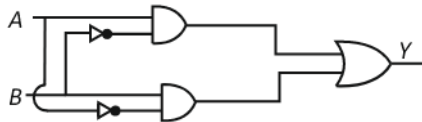
Answer (2)

Sol. Potential difference at equilibrium

$$V = \frac{C_1V_1 + C_2V_2}{C_1 + C_2} = \frac{(6\mu\text{F})(5\text{V})}{(6\mu\text{F}) + (12\mu\text{F})} = \frac{5}{3}\text{V}$$

$$q_1 = C_1V = (6\mu\text{F})\left(\frac{5}{3}\text{V}\right) = 10 \mu\text{C}$$

10. The truth table for the logical circuit shown below is



(1)

A	B	Y
0	0	0
0	1	0
1	0	0
1	1	1

(2)

A	B	Y
0	0	0
0	1	1
1	0	1
1	1	0

(3)

A	B	Y
0	0	0
0	1	1
1	0	1
1	1	1

(4)

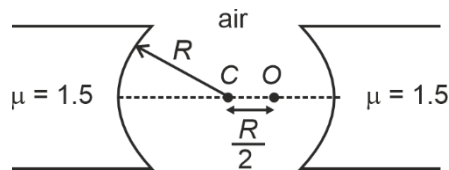
A	B	Y
0	0	1
0	1	0
1	0	0
1	1	1

Answer (2)

Sol. $Y = \overline{AB} + \overline{BA}$

This is a XOR gate

11. Figure shows two spherical surfaces of radius R having common centre. If the object is placed at O , find the distance between the first images formed by both the surfaces



- (1) $\frac{4R}{35}$ (2) $\frac{4R}{27}$
(3) $\frac{4R}{70}$ (4) $\frac{2R}{35}$

Answer (1)

Sol. For right surface

$$\frac{1.5}{v_1} - \frac{1}{-R/2} = \frac{0.5}{-R}$$

$$\frac{1.5}{v_1} = \frac{-2}{R} - \frac{0.5}{R}$$

$$v_1 = \frac{-3R}{5}$$

For left surface

$$\frac{1.5}{v_2} - \frac{1}{-3R} = \frac{0.5}{-R}$$

$$v_2 = \frac{-9R}{7}$$

$$d = 2R - \left(\frac{3R}{5} + \frac{9R}{7}\right)$$

$$d = \frac{4R}{35}$$

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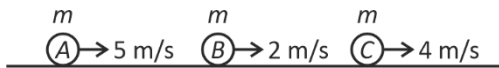
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12. Three particles of same mass are moving as shown. (all collisions are elastic)



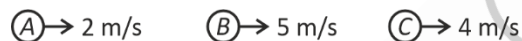
S_1 : After all collisions velocities are 4 m/s, 2 m/s and 5 m/s.

S_2 : Velocities are get interchanged in elastic collision of same mass.

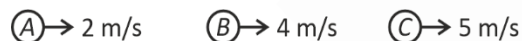
- (1) S_1 : Correct, S_2 : Correct
- (2) S_1 : Incorrect, S_2 : Correct
- (3) S_1 : Incorrect, S_2 : Incorrect
- (4) S_1 : Correct, S_2 : Incorrect

Answer (2)

Sol. After 1st collision



After 2nd collision

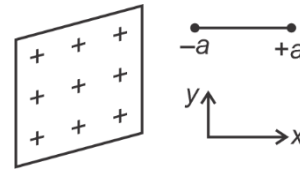


13. An electromagnetic wave propagates in +X-direction. Then, electric field and magnetic field are directed along
- (1) X, Y
 - (2) Y, Z
 - (3) Z, Y
 - (4) Y, X

Answer (2)

Sol. $\hat{C} = \hat{E} \times \hat{B}$

14. A dipole is placed such that its axis is perpendicular to the infinite charged sheet. Select the correct options



- (a) $T_{net} = 0$, F_{net} is along -ve x-axis
 - (b) $T_{net} = 0$, $U = \min$
 - (c) $T_{net} = 0$, $F_{net} = 0$
 - (d) T_{net} and U both are maximum
- (1) (a), (b), (c) and (d)
 - (2) (b) and (c)
 - (3) (a) and (c)
 - (4) (b) and (d)

Answer (2)

Sol. $T = \vec{p} \times \vec{E} = pE \sin\theta = 0$

$$U = -\vec{p} \cdot \vec{E} = -pE$$

$$\therefore T = 0, U = \min$$

$$F_{net} = 0$$

15. A cup of coffee take a time 't' to cool from 90°C to 80°C in a surrounding of 20°C. If a similar cup of coffee is cooled from 80°C to 60°C in the same surrounding, it takes a time
- (1) $\frac{13t}{5}$
 - (2) $\frac{5t}{13}$
 - (3) $\frac{12t}{5}$
 - (4) 2t

Answer (1)

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Sol. From Newtons law of cooling

$$-\frac{\theta_2 - \theta_1}{t} = C \left(\frac{\theta_2 + \theta_1}{2} - \theta_s \right)$$

$$\Rightarrow -\left(\frac{80^\circ\text{C} - 90^\circ\text{C}}{t} \right) = C \left(\frac{90^\circ\text{C} + 80^\circ\text{C}}{2} - 20^\circ\text{C} \right)$$

$$\frac{10^\circ\text{C}}{t} = C(65^\circ\text{C})$$

$$C = \frac{2}{13t}$$

Also,

$$-\left(\frac{60^\circ\text{C} - 80^\circ\text{C}}{t'} \right) = C \left(\frac{60^\circ\text{C} + 80^\circ\text{C}}{2} - 20^\circ\text{C} \right)$$

$$\frac{20^\circ\text{C}}{t'} = C(50^\circ\text{C})$$

$$C = \frac{2}{5t'}$$

$$\frac{2}{13t} = \frac{2}{5t'}$$

$$t' = \frac{13t}{5}$$

16.

17.

18.

19.

20.

SECTION - B

Numerical Value Type Questions: This section contains 5 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

21. A converging lens of focal length 24 cm, made of glass ($\mu_{\text{glass}} = 1.5$) is immersed completely in water ($\mu_{\text{water}} = 1.33$). It will now behave like a converging lens of focal length _____ cm.

Answer (96)

$$\text{Sol. } f_{\text{air}} (\mu_{\text{glass}} - 1) = f_{\text{water}} \left(\frac{\mu_{\text{glass}}}{\mu_{\text{water}}} - 1 \right)$$

$$(+24 \text{ cm}) (1.5 - 1) = f_{\text{water}} \left(\frac{1.5}{1.33} - 1 \right)$$

$$24 \times \frac{1}{2} = f \times \frac{1}{8}$$

$$f = 12 \times 8$$

$$f_{\text{water}} = 96 \text{ cm}$$

22. Find the number of spectral lines in H-atom when de-excite from $n = 4$ to ground state

Answer (6)

Sol. Number = 3×2

$$= 6$$

23. For a certain mechanical system the rate of accretion $\frac{dm}{dt}$

is proportional to \sqrt{v} , where m is mass, t is time and v is velocity, then the power is proportional to $v^{n/2}$ where n is _____.

Answer (5)

$$\text{Sol. } F = \left(\frac{dm}{dt} \right) v = (R\sqrt{v}) v = Rv^{3/2}$$

$$P = Fv = (Rv^{3/2}) v = Rv^{5/2}$$

24.

25.

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CHEMISTRY

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

Choose the correct answer :

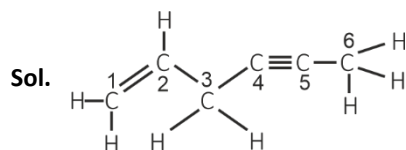
- Which one of the following forms most stable carbocation ?
 (1) $(\text{Ph})_3\text{C-Br}$
 (2) $\text{C}_6\text{H}_5\text{CH}_2\text{Br}$
 (3) $\text{C}_6\text{H}_5\text{CH}(\text{Br})\text{CH}_3$
 (4) $\text{CH}_3\text{CH}_2\text{CH}_2\text{CH}_2\text{Br}$

Answer (1)

Sol. $(\text{Ph})_3\text{C-Br}$ Forms $\text{Ph}-\overset{\oplus}{\text{C}}(\text{Ph})_2$ as the most stable intermediate among the given compounds.

- Number of σ and π bonds respectively in hex-1-en-4-yne are
 (1) 13, 3
 (2) 14, 3
 (3) 3, 14
 (4) 14, 13

Answer (1)



Hex-1-en-4-yne

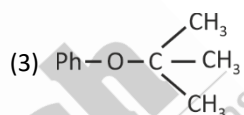
$\Rightarrow 13 \sigma$ and 3π bonds

- Which element in group 15 has the lowest Ionisation Energy
 (1) Bi
 (2) P
 (3) As
 (4) Sb

Answer (1)

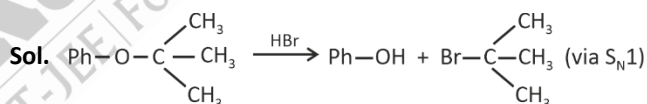
Sol. $\text{N} > \text{P} > \text{As} > \text{Sb} > \text{Bi}$
 $\frac{1402}{1012} > \frac{947}{834} > \frac{703}{703} \text{ kJ/mol}$

- Which of the following ether react with HBr to form phenol?
 (1) $\text{Ph-CH}_2\text{-O-CH}_2\text{-CH}_3$
 (2) $\text{Ph-CH}_2\text{-OCH}_3$

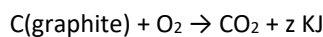
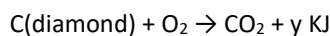
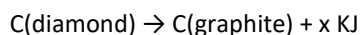


- (4) $\text{Ph-CH}_2\text{-O-CH}_2\text{-Ph}$

Answer (3)



- Consider the following thermochemical reactions and choose the correct option.



- (1) $x = y + z$ (2) $x = y - z$
 (3) $x + y = z$ (4) $x + y = -z$

Answer (2)

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- Sol.** (1) $C(\text{diamond}) \rightarrow C(\text{graphite}) \quad \Delta H_1 = -x\text{kJ}$
 (2) $C(\text{diamond}) + O_2(g) \rightarrow CO_2(g) \quad \Delta H_2 = -y\text{kJ}$
 (3) $C(\text{graphite}) + O_2(g) \rightarrow CO_2(g) \quad \Delta H_3 = -z\text{kJ}$

From (1), (2) and (3), we get

$$\Delta H_1 = \Delta H_2 - \Delta H_3$$

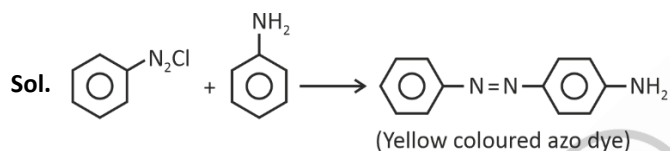
$$-x = -y + z$$

$$x = y - z$$

6. Which of the following will give azo dye test?

- (1) Aniline (2) Anisole
 (3) Benzene (4) Benzaldehyde

Answer (1)



7. Which of the following is an essential amino acid?

- (1) Alanine (2) Glycine
 (3) Valine (4) Aspartic acid

Answer (3)

Sol. Tryptophan, Threonine, Histidine, Valine, Isoleucine, Phenylalanine, Methionine, Arginine, Leucine and Lysine are essential amino acids.

8. A drug becomes ineffective when it decomposes to 50 % its concentration. If 16 mg of said drug becomes 4 mg in 12 months, find the time in which drug becomes ineffective given that decomposition of drug follows first order kinetics.

- (1) 6 months (2) 3 months
 (3) 2 months (4) 12 months

Answer (1)

Sol. Drug $\xrightarrow{\text{1st order}}$ Products

Initial mass of drug = 16 mg

Mass of drug after 12 months = 4 mg

$t_{3/4} = 12$ months

$2t_{1/2} = 12$ months

$t_{1/2} = 6$ months

\therefore Drug becomes ineffective in 6 months.

9. Which of the following gives O_2 predominantly on electrolysis among the following?

- A. Aq. $AgNO_3$ (Pt electrodes)
 B. Aq. $AgNO_3$ (Ag electrodes)
 C. Conc. H_2SO_4 (Pt electrodes)
 D. Dilute H_2SO_4 (Pt electrodes)

(1) A, B only

(2) B, C only

(3) A, B, C only

(4) A, D only

Answer (4)

Sol. Aq. $AgNO_3$ (Pt electrodes)

Cathode : $Ag^+ + e^- \rightarrow Ag$

Anode : $2H_2O \rightarrow O_2 + 4H^+ + 4e^-$

Dilute H_2SO_4 (Pt electrodes)

Cathode : $2H_2O + 2e^- \rightarrow H_2 + OH^-$

Anode : $2H_2O \rightarrow O_2 + 4H^+ + e^-$

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SECTION - B

Numerical Value Type Questions: This section contains 5 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

21. 0.41 g of BaSO₄ is obtained from 0.2 g of organic compound in Carius method. What is the percentage of sulphur present in organic compound?

Answer (28)

Sol. Moles of BaSO₄ = $\frac{0.41}{233}$ mol

$$\text{Mass of sulphur} = \frac{0.41}{233} \times 32 \text{ g}$$

$$= 0.056 \text{ g}$$

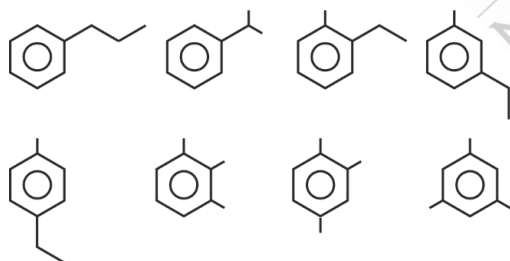
$$\% \text{ of sulphur in organic compound} = \frac{0.056}{0.2} \times 100$$

$$= 28\%$$

22. The number of benzenoid structural isomers having molecular formula C₉H₁₂ which do not give Baeyer's reagent test is ?

Answer (8)

Sol. D.U. = $\frac{18 + 2 - 12}{2} = 4$



Baeyer's Reagent (cold dil. KMnO₄) reacts with alkene and alkynes and not with benzene.

23. How many maximum spectral lines are observed when a sample of hydrogen atoms de-excited from n = 4 to n = 1?

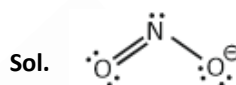
Answer (6)

Sol. Maximum number of spectral lines = $\frac{n(n-1)}{2}$

$$= \frac{4(4-1)}{2} = \frac{12}{2} = 6$$

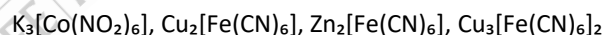
24. Find number of non-bonding electron in NO₂⁻ ion is _____.

Answer (12)



Number of non-bonding electrons will be
= 4 + 2 + 6
= 12

25. Find spin only magnetic moment of yellow coloured complex compound



Answer (0)

Sol. Cu₂[Fe(CN)₆] = Chocolate brown ppt

Zn₂[Fe(CN)₆] = White ppt

Cu₃[Fe(CN)₆]₂ = Green ppt

K₃[Co(NO₂)₆] = Yellow ppt

In K₃[Co(NO₂)₆], Co³⁺ with SFL(NO₂⁻) has electronic configuration t_{2g}⁶ e_g⁰

Number of unpaired e⁻ = 0

So, μ = 0

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4. Let the line L be $\frac{x-1}{1} = \frac{y-4}{3} = \frac{z-7}{5}$ and foot of perpendicular from $(1, -2, -1)$ to L is (α, β, γ) , then $\alpha + \beta + \gamma$ is

- (1) $-\frac{69}{35}$ (2) $\frac{102}{35}$
(3) $\frac{69}{35}$ (4) $-\frac{102}{35}$

Answer (4)

Sol. $\frac{x-1}{1} = \frac{y-4}{3} = \frac{z-7}{5} = \lambda$

Point on line $A(\lambda + 1, 3\lambda + 4, 5\lambda + 7)$

$B(1, -2, -1)$

$\overrightarrow{AB} \cdot \langle 1, 3, 5 \rangle = 0$

$\lambda \cdot 1 + 3(3\lambda + 4) + 5(5\lambda + 7) = 0$

$35\lambda + 18 + 40 = 0$

$\lambda = -\frac{58}{35}$

$(\alpha, \beta, \gamma) \equiv \left(-\frac{23}{35}, -\frac{34}{35}, -\frac{9}{7} \right)$

$\alpha + \beta + \gamma = -\frac{102}{35}$

5. If the exhaustive values of a for which the equation $2x^2 + (a - 5)x + 15 = 3a$ has no real roots is (α, β) , then $|4(\alpha + \beta)|$ is equal to

- (1) 56 (2) 52
(3) 54 (4) 18

Answer (1)

Sol. No real roots \Rightarrow discriminant is negative

$\Rightarrow (a - 5)^2 - 4(2)(15 - 3a) < 0$

$\Rightarrow a^2 - 10a + 25 - 120 + 24a < 0$

$a^2 + 14a - 95 < 0$

$(a + 19)(a - 5) < 0$

$\Rightarrow a \in (-19, 5)$

$\alpha = -19$

$\alpha = 5$

$|4(\alpha + \beta)|$

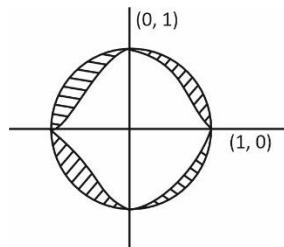
$= |4(-19)| = 56$

6. Area enclosed between the curves $|y| = 1 - x^2$ and $x^2 + y^2 = 1$ is $(\pi - \alpha)$ sq. units, then 9α is

- (1) 8 (2) 16
(3) 32 (4) 24

Answer (2)

Sol.



Area = $\pi - 4 \int_0^1 (1 - x^2) dx$

$= \pi - 4 \left[x - \frac{x^3}{3} \right]_0^1$

$= \pi - 4 \times \frac{2}{3} = \left(\pi - \frac{8}{3} \right)$ sq unit

$= \pi - \alpha$

$\Rightarrow \pi = \frac{8}{3}$

$9\alpha = 16$

7. If $\log y = x \log \frac{2}{5}$, $x \in \mathbb{N} \cup \{0\}$. Then sum of all values of y equals to

- (1) $\frac{5}{3}$ (2) $\frac{2}{3}$
(3) $\frac{5}{4}$ (4) $\frac{8}{3}$

Answer (1)

Sol. $\log y = x \log \frac{2}{5}$

$\log y = \log \left(\frac{2}{5} \right)^x$

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AIR 25 Rishi Shekher Shukla 2-Year Classroom	AIR 67 Krishna Sai Shishir 2-Year Classroom	AIR 78 Abhishek Jain 2-Year Classroom	AIR 93 Hardik Aggarwal 2-Year Classroom	AIR 95 Ujjwal Singh 2-Year Classroom	AIR 98 Rachit Aggarwal 2-Year Classroom
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JEE (Main) 2024

100 PERCENTILE Karnataka Topper AIR 1 Samol Jain 2-Year Classroom	100 PERCENTILE Telangana Topper AIR 15 M Sai Divya Teja Reddy 2-Year Classroom	100 PERCENTILE Telangana Topper AIR 19 Rishi Shekher Shukla 2-Year Classroom
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$$y = \left(\frac{2}{5}\right)^x$$

$$x \in \mathbb{N} \cup \{0\}$$

$$\Rightarrow y = 1, \frac{2}{5}, \left(\frac{2}{5}\right)^2 \dots \text{which is in G.P.}$$

$$\text{Sum of all values of } \sum y = \frac{1}{1 - \frac{2}{5}} = \frac{5}{3}$$

8. There is an arithmetic progression $a_1, a_2, a_3, \dots, a_{2024}$ and $a_1 + (a_5 + a_{10} + a_{15} \dots a_{2020}) + a_{2024} = 2233$. Find the value of $a_1 + a_2 + a_3 + \dots + a_{2024}$.

- (1) 11034 (2) 11132
 (3) 10432 (4) 20462

Answer (2)

Sol. $\because a_1, a_2, a_3, \dots, a_{2024}$ are in A.P.

$$\text{Then } a_1 + a_{2024} = a_2 + a_{2023} = \dots = a_r + a_{2024-r+1} = l$$

$$\therefore a_1 + (a_5 + a_{10} + \dots + a_{2020}) + a_{2024} = 2023$$

$$\text{or, } (202l) + l = 2023$$

$$\text{or, } 203l = 2233$$

$$\therefore a_1 + a_2 + \dots + a_{2024} = 1012 \times l$$

$$= 1012 \times \frac{2233}{203}$$

$$= 1012 \times 11$$

$$= 11132$$

9. Two points (4, 2) and (0, 2) lie on the circle whose centre lies on $3x + 2y + 2 = 0$, then length of chord whose mid point is (1, 2), is

- (1) $\sqrt{3}$ (2) $\sqrt{5}$
 (3) $2\sqrt{3}$ (4) $2\sqrt{5}$

Answer (3)

Sol. Let the centre be $(-2\alpha, 3\alpha - 1)$

$$\sqrt{(-2\alpha - 4)^2 + (3\alpha - 3)^2} = \sqrt{(-2\alpha - 0)^2 + (3\alpha - 3)^2}$$

$$\Rightarrow (-2\alpha - 4)^2 = (-2\alpha)^2$$

$$\Rightarrow -2\alpha - 4 = -2\alpha$$

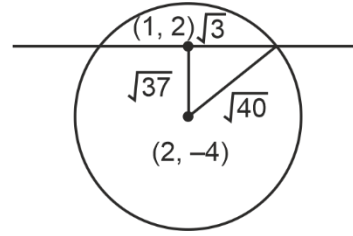
$$\Rightarrow \text{No solution}$$

$$-2\alpha - 4 = -2\alpha$$

$$\Rightarrow \boxed{\alpha = -1}$$

Centre will be (2, -4), radius $\sqrt{4 + 36} = \sqrt{40}$

$$(x - 2)^2 + (y + 4)^2 = 40$$



$$\Rightarrow \text{Length of chord} = 2\sqrt{3}$$

10. If $\lim_{t \rightarrow 0} \left(\int_0^1 (3x + 5)^t dx \right)^{\frac{1}{t}} = \alpha \left(\frac{8}{5} \right)^{\frac{p}{q}}$, then α is

- (1) 32 (2) 16
 (3) 8 (4) 64

Answer (1)

$$\text{Sol. Since, } \int_0^1 (3x + 5)^t dx = \frac{8^{t+1} - 5^{t+1}}{3(t+1)}$$

$$\Rightarrow L = \lim_{t \rightarrow 0} \left(\frac{8^{t+1} - 5^{t+1}}{3(t+1)} \right)^{\frac{1}{t}}$$

$$\Rightarrow L = \lim_{t \rightarrow 0} (1 + f(t))^{\frac{1}{f(t)} \cdot \frac{f(t)}{t}}$$

$$\text{Where } f(t) = \frac{8^{t+1} - 5^{t+1}}{3(t+1)} - 1 = \frac{8^{t+1} - 5^{t+1} - 3t - 3}{3(t+1)}$$

$$\Rightarrow \text{Since, } \lim_{t \rightarrow 0} f(t) = 0$$

$$L = \lim_{t \rightarrow 0} e^{\frac{f(t)}{t}} = e^{\lim_{t \rightarrow 0} \frac{f(t)}{t}} = e^{\lim_{t \rightarrow 0} f'(t)}$$

$$f'(t) = \frac{8.8^t \ln 8 - 5.5^t \ln 5 - 3}{3(t+1)} - \frac{8^{t-1} - 5^{t+1} - 3t - 3}{3(t+1)^2}$$

$$\lim_{t \rightarrow 0} f'(t) = \frac{8 \ln 8 - 5 \ln 5 - 3}{3} = \frac{1}{3} \ln \left(\frac{8^8}{5^5} \right) - 1$$

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JEE (Main) 2024

Karnataka Topper	100 Percentile	Telangana Topper	100 Percentile	Telangana Topper	100 Percentile
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$$L = e^{\ln\left(\frac{8^8}{5^5}\right)^{\frac{1}{3}} - 1} = \left(\frac{8^8}{5^5}\right)^{\frac{1}{3}} \cdot e^{-1} = \frac{\left(\frac{8^8}{5^5}\right)^{\frac{1}{3}}}{e}$$

$$= \frac{1}{e} \left(\frac{8}{5}\right)^{\frac{5}{3}} \cdot 8^3 = \frac{32 \left(\frac{8}{5}\right)^{\frac{5}{3}}}{4e}$$

$$\Rightarrow \alpha = 32$$

11. The value of $\int_0^{\frac{\pi}{4}} \left(\sin\left(4x - \frac{\pi}{2}\right) + \sin[2x] \right) dx$ is
(where $[\cdot]$ denotes the greatest integer function)
- (1) $\frac{1}{2} + \left(\frac{\pi-2}{4}\right)\sin 1$ (2) $\frac{1}{4} + \left(\frac{\pi-2}{2}\right)\sin 1$
(3) $\frac{1}{2} - \left(\frac{\pi-2}{4}\right)\sin 1$ (4) $\frac{1}{4} - \left(\frac{\pi-2}{2}\right)\sin 1$

Answer (1)

Sol. $\int_0^{\frac{\pi}{4}} \left(\sin\left|4x - \frac{\pi}{2}\right| + \sin[2x] \right) dx$

$$= \int_0^{\frac{\pi}{4}} \sin\left|4x - \frac{\pi}{2}\right| dx + \int_0^{\frac{\pi}{4}} \sin[2x] dx$$

$$= \int_0^{\frac{\pi}{8}} \sin\left|\frac{\pi}{2} - 4x\right| dx + \int_{\frac{\pi}{8}}^{\frac{\pi}{4}} \sin\left[4x - \frac{\pi}{2}\right] dx + \int_0^{\frac{1}{2}} 0 dx$$

$$+ \int_{\frac{1}{2}}^1 \sin(1) dx$$

$$= \int_0^{\frac{\pi}{8}} \cos 4x dx + \int_{\frac{\pi}{8}}^{\frac{\pi}{4}} \cos 4x dx + \sin 1 \cdot \left(\frac{\pi}{4} - \frac{1}{2}\right)$$

$$= \left[\frac{\sin 4x}{4}\right]_0^{\frac{\pi}{8}} - \left[\frac{\sin 4x}{4}\right]_{\frac{\pi}{8}}^{\frac{\pi}{4}} + \frac{(x-2)\sin 1}{4}$$

$$= \frac{1}{4} + \frac{1}{4} + \frac{(\pi-2)\sin 1}{4}$$

$$= \frac{(\pi-2)\sin(1) + 2}{4} = \frac{1}{2} + \left(\frac{\pi-2}{4}\right)\sin 1$$

12.
13.
14.
15.
16.
17.
18.
19.
20.

SECTION - B

Numerical Value Type Questions: This section contains 5 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

21. Let $a_{ij} = (\sqrt{2})^{i+j}$, $A = [a_{ij}]_{3 \times 1}$. If sum of third row of A^2 is $\alpha + \beta\sqrt{2}$, then $\alpha + \beta$ is

Answer (224)

Sol. $\begin{bmatrix} 2 & 2\sqrt{2} & 4 \\ 2\sqrt{2} & 4 & 4\sqrt{2} \\ 4 & 4\sqrt{2} & 8 \end{bmatrix} \begin{bmatrix} 2 & 2\sqrt{2} & 4 \\ 2\sqrt{2} & 4 & 4\sqrt{2} \\ 4 & 4\sqrt{2} & 8 \end{bmatrix} = \begin{bmatrix} 28 & 28\sqrt{2} & 56 \\ 28\sqrt{2} & 56 & 56\sqrt{2} \\ 56 & 56\sqrt{2} & 112 \end{bmatrix}$

$$56 + 112 + 56\sqrt{2}$$

$$168 + 56\sqrt{2}$$

$$\alpha + \beta\sqrt{2}$$

$$\alpha + \beta = 224$$

22. If 3^{107} is divided by 23, then remainder is

Answer (06)

Sol. Notice that, $3^4 \equiv (12) \pmod{23}$

$$\Rightarrow 3^8 \equiv 144 \equiv 6 \pmod{23}$$

$$3^{11} \equiv 1 \pmod{23}$$

$$(3^{11})^9 \equiv 1 \pmod{23}$$

$$3^{99} \equiv 1 \pmod{23}$$

$$3^8 \cdot 3^{99} \equiv 1 \pmod{23}$$

$$\Rightarrow 3^{107} \equiv 6 \pmod{23}$$

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23. If α, β are the values of m where
 $x + y + 2z = 1$
 $x + 2y + 4z = m$
 $x + 4y + 8z = m^2$ have infinitely many solutions.
 Then $\sum_{n=1}^{10} (n^\alpha + n^\beta)$ is equal to

Answer (440)

Sol. For infinite solution

$$\Delta = \Delta_1 = \Delta_2 = \Delta_3 = 0$$

$$\Delta = \begin{vmatrix} 1 & 1 & 2 \\ 1 & 2 & 4 \\ 1 & 4 & 8 \end{vmatrix} = 0$$

$$\Delta_1 = \begin{vmatrix} 1 & 1 & 2 \\ m & 2 & 4 \\ m^2 & 4 & 8 \end{vmatrix} = 0$$

$$\Delta_2 = \begin{vmatrix} 1 & 1 & 2 \\ 1 & m & 4 \\ 1 & m^2 & 8 \end{vmatrix} = 0 \Rightarrow m^2 + 3m - 2$$

$$\Rightarrow m^2 - 3m + 2 = 0$$

$$m = 2, 1$$

$$\Delta_3 = \begin{vmatrix} 1 & 1 & 1 \\ 1 & 2 & m \\ 1 & 4 & m^2 \end{vmatrix} = 0 \Rightarrow m^2 - 3m + 2 = 0$$

$$\Rightarrow m = 2, 1 \Rightarrow \alpha = 1, \beta = 2$$

$$\sum_{n=1}^{10} (n)^1 + (n)^2 = \frac{10 \times 11}{2} + \frac{10 \times 11 \times 21}{6}$$

$$= 440$$

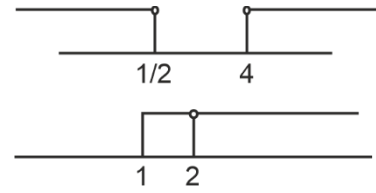
24. If the domain of $\log_{x-1} \left(\frac{2x^2 - 9x + 4}{x^2 - 4x + 5} \right)$ is (α, ∞) and $\log_5(18x - x^2 - 77)$ is (β, γ) , then the value of $\alpha^2 + \beta^2 + \gamma^2$ is

Answer (186)

Sol. $\frac{2x^2 - 9x + 4}{x^2 - 4x + 5} > 0 \dots(i)$

$$x - 1 > 0, x - 1 \neq 1$$

$$\Rightarrow (2x - 1)(x - 4) > 0$$



$$\therefore x \in (4, \infty)$$

$$\therefore \alpha = 4$$

$$\log_5(18x - x^2 - 77)$$

$$\Rightarrow 18x - x^2 - 77 > 0$$

$$\Rightarrow x^2 - 18x + 77 < 0$$

$$\Rightarrow (x - 7)(x - 11) < 0$$

$$x \in (7, 11)$$

$$\therefore \beta = 7, \gamma = 11$$

$$\therefore \alpha^2 + \beta^2 + \gamma^2$$

$$= 16 + 49 + 121$$

$$= 186$$

25. The equation $\alpha x + \beta y = 109$ is chord of ellipse $\frac{x^2}{9} + \frac{y^2}{4} = 1$ having midpoint $\left(\frac{5}{2}, \frac{1}{2} \right)$, then $\alpha + \beta$ is

Answer (58)

Sol. Chord with given middle point

$$T = S_1$$

$$\frac{5}{18}x + \frac{y}{8} = \frac{25}{36} + \frac{1}{16} = \frac{109}{144}$$

$$40x + 18y = 109$$

$$\equiv \alpha x + \beta y = 109$$

$$\Rightarrow \alpha = 40 \quad \beta = 18$$

$$\alpha + \beta = 58$$



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