

*Corporate Office* : AESL, 3rd Floor, Incuspaze Campus-2, Plot-13, Sector-18, Udyog Vihar, Gurugram, Haryana-122018

# Memory Based Answers & Solutions

Time : 3 hrs.



M.M. : 300

# JEE (Main)-2025 (Online) Phase-1

# (Physics, Chemistry and Mathematics)

### **IMPORTANT INSTRUCTIONS:**

- (1) The test is of **3 hours** duration.
- (2) This test paper consists of 75 questions. Each subject (PCM) has 25 questions. The maximum marks are 300.
- (3) This question paper contains Three Parts. Part-A is Physics, Part-B is Chemistry and Part-C is Mathematics. Each part has only two sections: Section-A and Section-B.
- (4) Section A : Attempt all questions.
- (5) **Section B :** Attempt all questions.
- (6) Section A (01 20) contains 20 multiple choice questions which have only one correct answer.
   Each question carries +4 marks for correct answer and –1 mark for wrong answer.
- (7) Section B (21 25) contains 5 Numerical value based questions. The answer to each question should be rounded off to the nearest integer. Each question carries +4 marks for correct answer and –1 mark for wrong answer.





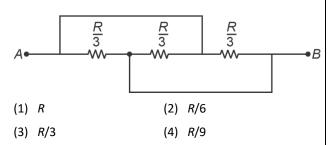
# PHYSICS

#### SECTION - A

**Multiple Choice Questions:** This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

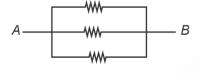
#### Choose the correct answer:

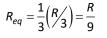
1. Find the equivalent resistance across A & B.



#### Answer (4)

sol. Equivalent circuit can be redrawn as





- 2. A uniform wire of linear charge density  $\lambda$  is placed along y-axis. The locus of equipotential surface is
  - (1)  $x^2 + y^2 + z^2 = \text{constant}$
  - (2)  $x^2 + z^2 = \text{constant}$
  - (3) xyz = constant
  - (4) xy + yz + zx = constant

#### Answer (2)

- **Sol.** Concentric cylinders are the equipotential surface.
- 3. Which of following reaction is correct?

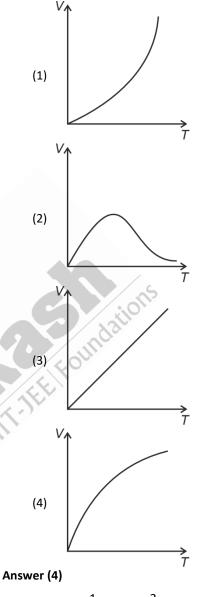
(Where symbols have their usual meanings)

(1) 
$$n \rightarrow p + e^- + v$$
 (2)  $n \rightarrow p + e^+ + v$ 

(3) 
$$n \rightarrow p + e^+ + \overline{v}$$
 (4)  $n \rightarrow p + e^- + \overline{v}$ 

Answer (4)

- **Sol.** In 2, 3 charge conservation is not holding and in neutron decay, antineutrino  $(\overline{v})$  is released.
- 4. The graph of root mean square velocity *v/s* temperature is

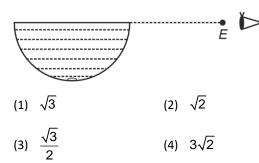


Sol. We know 
$$\frac{1}{2}MV_{Rms}^2 = \frac{3}{2}RT$$
  
 $\Rightarrow V_{RMS} = \sqrt{\frac{3RT}{M}} \Rightarrow V_{RMS} \alpha \sqrt{T}$ 

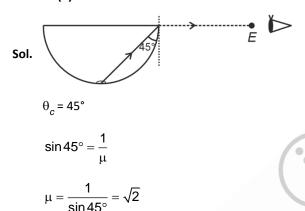


Nedical

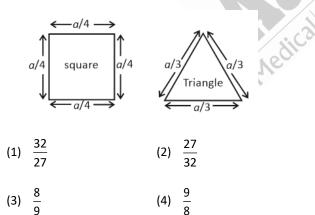
5. A coin is placed at the bottom of a hemispherical container filled with a liquid of refractive index  $\mu$ . Find the least refractive index if the coin is visible to an observer at *E*.



Answer (2)



 In the given figure, the square and the triangle have same resistance per unit length. Find the ratio of their resistances about adjacent corners.



#### Answer (2)

**Sol.** Let the resistance per unit length be  $\lambda$ , then

For square,

$$R_{\text{Square}} = \frac{\left(\frac{3\lambda a}{4}\right)\left(\frac{\lambda a}{4}\right)}{\frac{3\lambda a}{4} + \frac{\lambda a}{4}} = \frac{3\lambda a}{16}$$

For triangle,

$$R_{\text{Triangle}} = \frac{\left(\frac{2\lambda a}{3}\right)\left(\frac{\lambda a}{3}\right)}{\frac{2\lambda a}{3} + \frac{\lambda a}{3}} = \frac{2\lambda a}{9}$$

$$\frac{R_{\text{Square}}}{R_{\text{Triangle}}} = \frac{3\lambda a}{16} \times \frac{a}{2\lambda a} = \frac{27}{32}$$

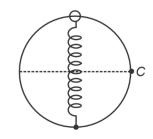
7. **Assertion :** Work done by central force is independent of path.

Reason : Potential energy is associated with every force.

- (1) Both Assertion and Reason are correct
- (2) Assertion is correct, Reason is incorrect
- (3) Assertion is incorrect, Reason is correct
- (4) Both Assertion and Reason are incorrect

Answer (4)

- **Sol.** Not all central force/s are conservative so work done by central force might depend on path.
- 8. There is smooth ring of radius *R* in vertical plane. A spring of natural length *R* & elastic constant *K* is vertical along a diameter. The free end is connected to bead of mass *m* & when slightly disturbed it reaches point *C* with speed v where v is







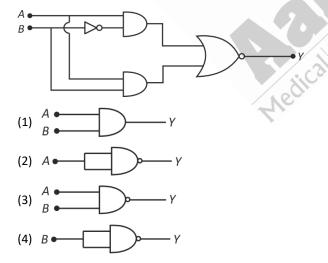
(1) 
$$\sqrt{\frac{KR^2(\sqrt{2}-1)+2mgR}{m}}$$
  
(2) 
$$\sqrt{\frac{2KR^2(\sqrt{2}-1)+2mgR}{m}}$$
  
(3) 
$$\sqrt{\frac{2KR^2(\sqrt{2}-1)+mgR}{m}}$$
  
(4) 
$$\sqrt{\frac{KR^2(\sqrt{2}-1)+mgR}{m}}$$

#### Answer (2)

**Sol.** Loss in PE = gain in KE

$$\frac{1}{2}\kappa(R^{2}) - \frac{1}{2}\kappa(\sqrt{2} - 1)^{2}R^{2} + mgR = \frac{1}{2}mv^{2}$$
$$\frac{1}{2}\kappa R^{2}\left\{1 - 2 - 1 + 2\sqrt{2}\right\} + mgR = \frac{1}{2}mv^{2}$$
$$\kappa R^{2}\left(\sqrt{2} - 1\right) + mgR = \frac{1}{2}mv^{2}$$
$$\sqrt{\frac{2\kappa R^{2}\left(\sqrt{2} - 1\right) + 2mgR}{m}} = v$$

9. The equivalent logic gate for the circuit shown below is



#### Answer (2)

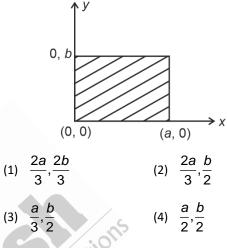
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Sol.  $Y = \overline{AB} + AB$  $Y = \overline{A(B} + B)$ 

 $Y = \overline{A}$ 

10. Surace mass density varies as  $\sigma = \frac{\sigma_0 x}{ab}$  for the given

plane sheet. Find the position of centre of mass for the distribution given



Answer (2)

**Sol.** As there is no variation of mass density in *y* direction. So

$$y_{\rm cm} = \frac{b}{2}$$

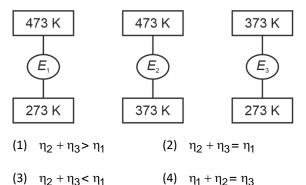
Now for *x* direction

$$dm = \left(\frac{\sigma_0 x}{ab}\right) b.dx$$
$$x_{cm} = \frac{\int_0^a x dm}{\int_0^a dm} = \frac{\frac{\sigma_0}{a} \int_0^a x^2 dx}{\frac{\sigma_0}{a} \int x dx}$$
$$\Rightarrow x_{cm} = \frac{a^3 \times 2}{3 \times a^2} = \frac{2}{3}a$$

So 
$$r_{cm} = \frac{2}{3}a, \frac{b}{2}$$

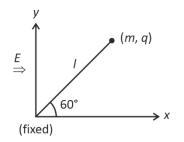


11.  $\eta_1$ ,  $\eta_2$  and  $\eta_3$  are the efficiencies of the three Carnot engines  $E_1$ ,  $E_2$  and  $E_3$  operating between temperatures shown in the figure. Choose the correct option relating the efficiencies.



#### Answer (1)

- Sol.  $\eta_1 = 1 \frac{273}{473} = \frac{200}{473}$  $\eta_2 = 1 - \frac{373}{473} = \frac{100}{473}$  $\eta_3 = 1 - \frac{273}{373} = \frac{100}{373}$  $\eta_1 - \eta_2 = \frac{100}{473} < \eta_3$ 
  - *i.e.*,  $\eta_2 + \eta_3 > \eta_1$
- 12. A simple pendulum of length *I* and bob of mass *m* is placed on smooth horizontal surface as shown. When electric field of strength *E* is switched on, the bob passes the *x*-axis with speed v then



(1) 
$$v = \sqrt{\frac{2qEI}{m}}$$
 (2)  $v = \sqrt{\frac{qEI}{m}}$ 

(3) 
$$v = \sqrt{\frac{qEl}{2m}}$$
 (4)  $v = 2\sqrt{\frac{qEl}{m}}$ 

Answer (2)

Sol. 
$$W = \Delta K$$

$$qE(I-I\cos 60^\circ)=\frac{1}{2}mv^2$$

$$\frac{qEl}{m} = v^2$$

13. **Statement-I**: Velocity of sound in solids is more compared to that in gases.

**Statement-II** : Bulk modules of gas is more than that of solids.

- (1) Statement-I is correct statement-II is correct
- (2) Statement-I is correct statement-II is incorrect
- (3) Statement-I is incorrect statement-II is correct
- (4) Statement-I is incorrect statement-II is incorrect

Answer (2)

**Sol.** Speed of sound in medium depends on elastic and inertia properly of medium.

for gas 
$$v = \sqrt{\frac{B}{\rho}}$$

for solids  $v = \sqrt{\frac{Y}{\rho}}$ 

The elastic properly of solids happens to be many fold greater than that of elastic properly of gases.

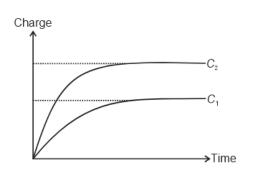
Bulk modulus of gas depends on the process,  $B = \frac{-\Delta P}{\Delta V / V}$ , which varies between 0 to  $\infty$  therefore in

general statement 2 is incorrect.





14. To capacitor  $C_1$  and  $C_2$  are connected across same battery and store energies  $\boldsymbol{U}_1$  and  $\boldsymbol{U}_2$  respectively at steady state. Choose the correct option by observing the graph of charge vs time shown below.



(1) 
$$\begin{array}{c} C_1 > C_2 \\ U_1 > U_2 \end{array}$$
 (2)  $\begin{array}{c} C_1 < C_2 \\ U_1 < U_2 \end{array}$ 

(3) 
$$\begin{array}{c} C_1 > C_2 \\ U_1 < U_2 \end{array}$$
 (4)  $\begin{array}{c} C_1 < C_2 \\ U_1 > U_2 \end{array}$ 

#### Answer (2)

(

Sol. Steady state

$$\frac{C_1}{C_2} = \frac{Q_1}{Q_2} < 1$$

(Connected across same

 $U_2$ 

potential difference)

$$\frac{C_1}{C_2} = \frac{U_1}{U_2} < 1$$

15. Energy of photon of wavelength  $\lambda$  is  $E_0$  which is equal to kinetic energy of proton of mass  $m_p$ . The ratio of de Broglie wavelengths of proton and photon is

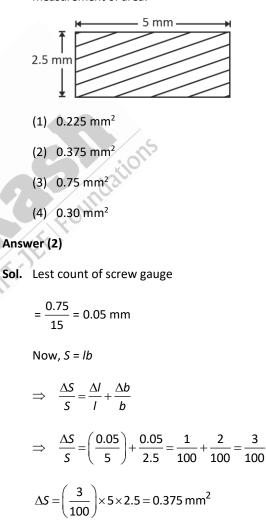
(1) 
$$\frac{1}{c}\sqrt{\frac{2E_0}{m_p}}$$
 (2)  $\frac{1}{c}\sqrt{\frac{E_0}{2m_p}}$   
(3)  $\frac{2}{c}\sqrt{\frac{E_0}{m_p}}$  (4)  $\frac{1}{2c}\sqrt{\frac{E_0}{m_p}}$ 

#### Answer (2)

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Sol. 
$$\frac{1}{2}m_{p}v^{2} = E_{0} \implies p = \sqrt{2m_{p}E_{0}} \qquad \lambda_{p} = \frac{h}{\sqrt{2m_{p}E_{0}}}$$
  
for photon  $\frac{hc}{\lambda} = E_{0} \implies \lambda_{ph} = \frac{hc}{E_{0}}$   
 $\implies \frac{\lambda_{p}}{\lambda_{ph}} = \frac{h}{\sqrt{2m_{p}E_{0}}} \times \frac{E_{0}}{hc} = \frac{1}{c}\sqrt{\frac{E_{0}}{2m_{p}}}$ 

16. The lengths of a rectangular sheet is measured from a screw gauge of pitch 0.75 mm and number of division on circular scale = 15. Find maximum possible error in measurement of area.





- 17. There are two prisms of refractive indices of 1.54 & 1.72 respectively. If ray is not deviating after passing through two prisms, then find prism angle of second prism if prism angle of first prism is 4°
  - (1) 2° (2) 3°
  - (3) 4° (4) 3.5°

#### Answer (2)

- **Sol.**  $S_1 = S_2$   $\Rightarrow (1.54 - 1)4^\circ = (1.72 - 1) A.$ 
  - $\Rightarrow A = 3^{\circ}$
- 18. The energy associated with a cylindrical region due to an EM wave  $E = 100\sin(kx - \omega t)$  is U<sub>0</sub>. Find the equation of EM wave for which a cylinder of same length and half the diameter (as previous one) contains same energy U<sub>0</sub>.
  - (1)  $200\sin(kx \omega t)$  (2)  $25\sin(\omega t kx)$
  - (3)  $50\sin(kx \omega t)$  (4)  $400\sin(\omega t kx)$

#### Answer (1)

**Sol.** For EM wave  $E = 100 \sin(\omega t - kx)$ 

Energy density  $\rho_{a_V} = \frac{1}{2} \in_0 (E_0)^2$ 

Initial volume  $v_0 = \pi R^2 I$ 

Volume in next situation =  $v = \frac{\pi R^2 I}{4} = \frac{V_0}{4}$ 

So, 
$$u_0 = \frac{1}{2} \in_0 (E_0)^2 \times V_0 = \frac{1}{2} \in_0 (E_1^2) \cdot \frac{V_0}{4}$$
  
 $\Rightarrow E_0^2 = \frac{E_1^2}{4} \Rightarrow E_1 = 2E_0 = 200 \text{ V/m}$ 

So, required equation will have 200 V/m of amplitude.

19.

20.



25.

Nedical



**Numerical Value Type Questions:** This section contains 5 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

21. The dimensions of Young's modules of elasticity per unit length is  $M^a L^b T^c$  then |a + b + c| is

Answer (3)

Sol. 
$$\frac{Y}{L} = \frac{MLT^{-2}}{L^2} \frac{1}{L} = ML^{-2}T^{-2}$$
  
 $|1-2-2| = 3$ 

22. In a YDSE, the distance of the 10<sup>th</sup> bright fringe from the central maxima is 10 mm when light of wavelength used is 600 nm. Find the distance (in mm) of the 10<sup>th</sup> bright fringe from the central maxima if light of wavelength 660 nm is used instead.

Answer (11) Sol.  $y = 10 \frac{\lambda D}{d}$  $\frac{y_2}{y_1} = \frac{\lambda_2}{\lambda_1}$  $y_2 = \frac{\lambda_2}{\lambda_1} \times y_1$  $= \frac{660 \text{ nm}}{600 \text{ nm}} \times 10 \text{ mm}$ = 11 mm23. 24.





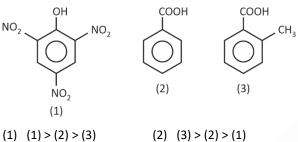
## **CHEMISTRY**

#### **SECTION - A**

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which ONLY ONE is correct.

#### Choose the correct answer :

1. What is the rate of reaction for releasing CO<sub>2</sub>(g) with aq. NaHCO₃ among following?



(4) (2) > (3) > (1)

- (1) (1) > (2) > (3)
- (3) (1) > (3) > (2)

#### Answer (3)

Sol. pKa (Benzoic acid): 4.27

pK<sub>a</sub> (o-Toluic acid) :  $3.91 \rightarrow$  due to ortho effect.

pK<sub>a</sub> (Picric acid) : 0.3

(+)

Consider the following carbocations 2.

$$(Ph)_{3}^{\oplus}C Ph_{2}CH CH_{3}CH_{2}-CH CH_{3}CH_{2}-CH CH_{3}CH_{2}-CH CH_{3}CH_{2}-CH CH_{3}CH_{3}CH_{3}-CH_{3}CH_{3}CH_{3}-CH_{3}CH_{3}CH_{3}-CH_{3}CH_{3}-CH_{$$

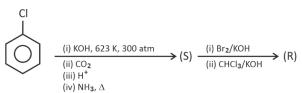
The correct increasing order of stability of these carbocations is:

(1) (i) < (ii) < (iii) < (iv) (2) (iv) < (iii) < (ii) < (i)(3) (ii) < (iii) < (iv) < (i) (4) (iv) < (iii) < (i) < (ii)

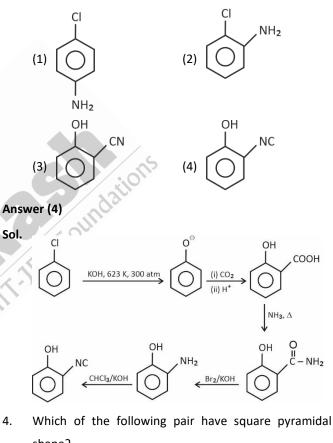
#### Answer (2)

Sol. Tropylium carbocation is most stable due to presence of aromaticity.

- $\therefore$  (i) > (ii) > (iii) > (iv) is the correct order of stability of carbocation.
- In the given reaction sequence: 3.



The compound R is



- 4. shape?
  - (1) BrF<sub>5</sub>, XeOF<sub>4</sub> (2) SbF<sub>5</sub>, BrF<sub>5</sub>
  - (3) PCl<sub>5</sub>, XeOF<sub>4</sub> (4) PCl<sub>5</sub>, SbF<sub>5</sub>

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Answer (1)
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dical

**Sol.** 
$$BrF_5 \Rightarrow sp^3d^2$$
  $F \searrow B \\ F \swarrow C$ 

Square pyramidal

$$XeOF_{4} \Rightarrow sp^{3}d^{2} \qquad F \swarrow Be^{V} F$$

Square pyramidal

- 5. Which of the following set of quantum numbers have same energy?
  - (a) n = 2, l = 2, m = +1
  - (b) n = 2, l = 1, m = −1
  - (c) n = 3, l = 2, m = 0
  - (d) n = 3, l = 2, m = 1
  - (1) a, b
  - (2) b, c
  - (3) c, d
  - (4) a, c

#### Answer (3)

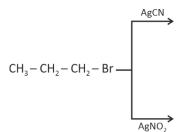
**Sol.:** (a)  $\Rightarrow$  2d = does not exist

(b)  $\Rightarrow 2p$ 

- (c)  $\Rightarrow$  3d same energy
- (d)  $\Rightarrow$  3d same energy

The value of n + l is same for (c) and (d) both represents 3d orbital

6. Consider the following reaction



The major product x and y respectively are

- (1) CH<sub>3</sub>CH<sub>2</sub>CH<sub>2</sub>ONO & CH<sub>3</sub>CH<sub>2</sub>CH<sub>2</sub>CN
- (2) CH<sub>3</sub>CH<sub>2</sub>CH<sub>2</sub>NO<sub>2</sub> & CH<sub>3</sub>CH<sub>2</sub>CH<sub>2</sub>CN
- (3) CH<sub>3</sub>CH<sub>2</sub>CH<sub>2</sub>NO<sub>2</sub> & CH<sub>3</sub>CH<sub>2</sub>CH<sub>2</sub>NC
- (4)  $CH_3CH_2CH_2ONO \& CH_3CH_2CH_2CN$

#### Answer (3)

**Sol.** CN<sup>-</sup> and NO<sub>2</sub><sup>-</sup> are ambidentate nucleophile but since

AgCN and  $AgNO_2$  are covalent compound, so only the nitrogen can donate electrons.

7. Match the following column and choose the correct option.

	Column-I		Column-II
(A)	$\mathrm{H_2O_2} \rightarrow \mathrm{H_2O} + \mathrm{O_2}$	(P)	Combustion
			reaction
(B)	NaH → Na + H <sub>2</sub>	(Q)	Disproportionation
			reaction
(C)	$CH_4 + O_2 \rightarrow$	(R)	Decomposition
	$CO_2 + H_2O$		reaction
(D)	$Fe + CuSO_4 \rightarrow$	(S)	Displacement
	FeSO <sub>4</sub> + Cu		reaction

- (1) A–(Q), B–(P), C–(R), D–(S)
- (2) A-(R), B-(Q), C-(S), D-(P)
- (3) A-(Q), B-(R), C-(P), D-(S)
- (4) A-(R), B-(Q), C-(P), D-(S)

Answer (3)

**Sol.**  $H_2O_2 \rightarrow H_2O + O_2$  : Disproportionation reaction

 $NaH \rightarrow Na + H_2$ : Decomposition reaction

 $\rm CH_4 + O_2 \rightarrow \rm CO_2 + H_2O\,$  : Combustion reaction

 $\mathsf{Fe} + \mathsf{CuSO}_4 \longrightarrow \mathsf{FeSO}_4 + \mathsf{Cu}\,: \mathsf{Displacement}\,\,\mathsf{reaction}$ 

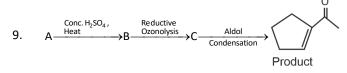




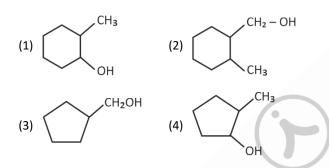
- Among the following the incorrect order of atomic radius is
  - (1) B > AI > Mg > F (2) AI > B > N > F
  - (3) Mg > Al > Be > O (4) Mg > Be > N > F

#### Answer (1)

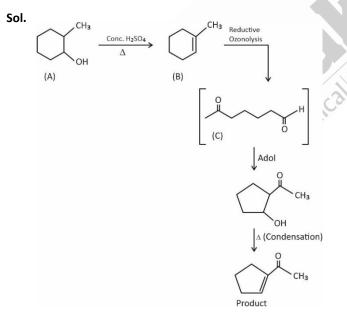
**Sol.** As we move down the group size increases whereas on moving left to right in a period size decreases



Identify the Compound A



Answer (1)



10.  $Et \ N \ Cl and Et \ CH \ CH \ (2)$ 

**Statement-I:** Compound (2) shows faster alkaline hydrolysis compared to (1).

**Statement-II:** Compound (1) shows substitution via neighbouring group participation.

- (1) Statement-I is correct and statement-II is incorrect
- (2) Statement-I is incorrect and statement-II is correct
- (3) Statement-I and statement-II both are correct
- (4) Statement-I and statement-II both are incorrect

#### Answer (2)

$$\mathbf{Sol.} \xrightarrow{\mathsf{Et}}_{\mathsf{Et}} \stackrel{\mathsf{N}}{\longrightarrow} \stackrel{\mathsf{Cl}}{\longrightarrow} \xrightarrow{\mathsf{Et}}_{\mathsf{Et}} \stackrel{\mathsf{N}}{\longrightarrow} \stackrel{\mathsf{Cl}}{\longrightarrow} \xrightarrow{\mathsf{Et}}_{\mathsf{Et}} \stackrel{\mathsf{N}}{\longrightarrow} \stackrel{\mathsf{N}}{\longrightarrow} \xrightarrow{\mathsf{Cl}}_{\mathsf{OH}} \stackrel{\mathsf{N}}{\longrightarrow} \xrightarrow{\mathsf{Cl}}_{\mathsf{OH}} \stackrel{\mathsf{N}}{\longrightarrow} \xrightarrow{\mathsf{N}}_{\mathsf{OH}} \stackrel{\mathsf{N}}{\longrightarrow} \xrightarrow{\mathsf{N}}_{\mathsf{N}} \stackrel{\mathsf{N}}{\longrightarrow} \xrightarrow{\mathsf{N}}_{\mathsf{OH}} \stackrel{\mathsf{N}}{\longrightarrow} \xrightarrow{\mathsf{N}}_{\mathsf{N}} \stackrel{\mathsf{N}}{\longrightarrow} \xrightarrow{\mathsf{N}}_{\mathsf{N}} \stackrel{\mathsf{N}}{\longrightarrow} \xrightarrow{\mathsf{N}}_{\mathsf{N}} \stackrel{\mathsf{N}}{\longrightarrow} \xrightarrow{\mathsf{N}}_{\mathsf{N}} \stackrel{\mathsf{N}}{\longrightarrow} \stackrel{\mathsf{N}}{\longrightarrow} \xrightarrow{\mathsf{N}}_{\mathsf{N}} \stackrel{\mathsf{N}}{\longrightarrow} \stackrel{\mathsf{N}}{\longrightarrow} \xrightarrow{\mathsf{N}}_{\mathsf{N}} \stackrel{\mathsf{N}}{\longrightarrow} \stackrel{\mathsf{N}}{$$

- 11. Which of the following has same energy in absence of electric and magnetic field for hydrogen atom?
  - (1) 2s, 3p (2) 3s, 2p
    - (4) 3s, 4f

Answer (3)

(3) 2s, 2p

- **Sol.** For hydrogen atom in absence of electric and magnetic field, energy only depends on principal quantum number(n). For same the value of n, energy will be same Hence 2s and 2p have same energy.
- 12. Which of the following reaction(s)/test(s) can be used to distinguish acetaldehyde and acetone?
  - (A) Iodoform Test (B) Cannizzaro
  - (C) Aldol Condensation (D) Fehling's Test
  - (E) Tollen's Test
- (F) Clemmensen's Reduction
- (1) (D), (E) Only
- (2) (A), (B), (C), (F) only
- (3) (B), (C), (F) only
- (4) (B), (C), (D), (E) only

#### Answer (1)



- **Sol.** CH<sub>3</sub>CHO will react with Fehling's solution and Tollen's reagent while CH<sub>3</sub>COCH<sub>3</sub> will not. Iodoform, Aldol and Clemmensen's reduction will be shown by both
- 13. Which of the following give violet colour in Borax bead test?
  - (1) Cr<sup>3+</sup>
  - (2) Mn<sup>2+</sup>
  - (3) Co<sup>3+</sup>
  - (4) Fe<sup>2+</sup>

#### Answer (2)

- Sol. Colour of Borax bead in oxidising flame is violet for Mn<sup>2+</sup>.
- 14. Which of the following compounds have the same number of lone pair on central atom as CIF<sub>3</sub>.
  - (1) XeF<sub>5</sub><sup>-</sup>
  - (2) XeF<sub>2</sub>
  - (3) BrF5
  - (4) l<sub>3</sub>

#### Answer (1)

Sol.  $CIF_{3} \Longrightarrow$ 



No. of lone pairs on central atom = 2



No. of lone pairs on central atom = 2

 $XeF_2 \Rightarrow$  no. of lone pairs on central atom = 3

 $I_3^- \Rightarrow$  no. of lone pairs on central atom = 3

 $BrF_5 \Rightarrow$  no. of lone pair on central atom-1

 Statement 1: For titration of oxalic acid using KMnO<sub>4</sub>, warming of acid solution is required whereas in case of Ferrous Ammonium Sulphate, it is done at room temperature.

**Statement 2:** Fe<sup>2+</sup> converts to Fe<sup>3+</sup> during titration.

- (1) Both Statement 1 and statement 2 are correct
- (2) Statement 1 is correct and statement 2 is incorrect
- (3) Statement 1 is incorrect and statement 2 is correct
- (4) Both Statement 1 and statement 2 both are incorrect

#### Answer (1)

**Sol.** In case of oxalic acid warming of solution (50°C-60°C) is done as rate of reaction is very slow at room temperature.

$$Fe^{2+} + MnO_{4}^{-} + 8H^{+} \rightarrow Mn^{2+} + 4H_{2}O + 5Fe^{3+}$$

oundation

16. 17.

18.

19. 20.

Medic

#### **SECTION - B**

**Numerical Value Type Questions:** This section contains 5 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

21.  $\Delta_f H$  of H(g) is 222 kJ/mol,  $\Delta_f H$  of O(g) is 250 kJ/mol,  $\Delta_f H$  of H<sub>2</sub>O(g) is -248 kJ/mol. What is the value of Bond Energy of O – H bond in H<sub>2</sub>O in kJ/mol?

#### Answer (471)

**Sol.** 
$$H_2(g) + \frac{1}{2}O_2(g) \longrightarrow H_2O(g)$$

$$\Delta H_{f} = \sum (B.E. of reactant) - \sum (B.E. of product)$$





 $-248 = 444 + 250 - (2 \times B.E._{O-H})$ 2B.E.<sub>O-H</sub> = 942 2B.E.<sub>O-H</sub> = 471 kJ / mole

22. 70% by mass solution of HNO₃ is taken having density1.41 g/mL. Calculate the molarity of solution

#### Answer (16)

Sol.  $M = \frac{10xd}{M_0}$ =  $\frac{10 \times 70 \times 1.41}{63}$ = 15.66 M

 1g of a non-electrolyte solute (MW = 256 g/mol) is dissolved in 50g of solvent, freezing point of solution is lowered by 0.40 K. Calculate the Molal depression constant of solvent.

#### Answer (5)

**Sol.**  $\Delta T_f = ik_f \times m$ 

$$\Delta T_{f} = ixk_{f} \times \frac{W_{solute}}{MW_{solute} \times W_{solvent}} \times 1000$$

$$0.4 = k_f \times \frac{1 \times 1000}{256 \times 50}$$

$$k_{f} = \frac{0.4 \times 256 \times 50}{1000}$$

k<sub>f</sub> = 5.12 K kg mol<sup>-1</sup>

 A compound contains 14.4% carbon, 1.2% hydrogen and 84.4% chlorine, calculate empirical formula mass of compound.

(Molar mass of C = 12, H = 1, Cl = 35.5]

#### Answer (84)

**Sol.** Let mass of compound = 100g

Mole Molar ratio

1

$$C = 14.4g \implies \frac{14.4}{12} = 1.2$$

$$H = 1.2g \implies \frac{1.2}{1} = 1.2 \qquad 1$$

$$CI = 84.4g \implies \frac{84.4}{35.5} = 2.4 \qquad 2$$

$$E.F. = CHCl_2$$

E.F. mass = 84

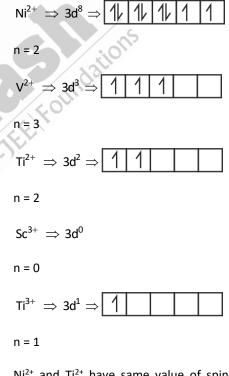
25. How many of the following ions have same value of spin only magnetic moment?

Ni<sup>2+</sup>, V<sup>2+</sup>, Ti<sup>2+</sup>, Sc<sup>3+</sup>, Ti<sup>3+</sup>

#### Answer (2)

**Sol.** The ions having same number of unpaired electrons having same value of spin only magnetic moment.

 $\mu = \sqrt{n(n+2)}$  BM (n = Number of unpaired electron)



Ni<sup>2+</sup> and Ti<sup>2+</sup> have same value of spin only magnetic moment.



JEE (Main)-2025 : Phase-1 (28-01-2025)-Morning



## MATHEMATICS

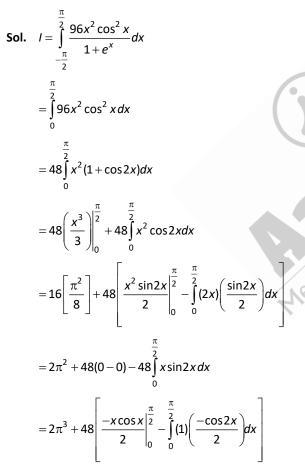
#### SECTION - A

**Multiple Choice Questions:** This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

#### Choose the correct answer :

1.	If $I = \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{96x^2 \cos \theta}{1 + e^x}$	$dx = \pi(\alpha\pi^2 + \beta)$ , then $(\alpha + \beta)^2$ is	
	(1) 100	(2) 144	
	(3) 169	(4) 196	

Answer (1)



$=2\pi^3-48\left[\left(\frac{\pi}{2}\right)\times\frac{1}{2}\right]+48\int_{0}^{\frac{\pi}{2}}\frac{\cos 2x}{2}dx$
$=2\pi^{2}-12\pi+24\left(\frac{\sin 2x}{2}\right)\Big _{0}^{\frac{\pi}{2}}$
$= 2\pi^2 - 12\pi + (0 - 0) = \pi \left[ 2\pi^2 - 12 \right]$
$=\pi\left[lpha\pi^{2}+\beta ight]$
$\Rightarrow \alpha = 2, \beta = -12$
$\Rightarrow (\alpha + \beta)^2 = (2 - 12)^2 = 100$

2. Number of ways to form 5 digit numbers greater than 50000 with the use of digits 0, 1, 2, 3, 4, 5, 6, 7 such that sum of first and last digit is not more than 8, is equal to

	(1)	511	9	(2)	5120		
	(3)	460	7	(4)	4608		
Ansv	ver (	3)	ons				
Sol.	<u>a b</u>	<u>c d e</u>	131101	<i>a</i> ≥ 5			
7			mos	$a + e \leq 8$			
		20		not a	all <i>b, c, d, e</i> are zero		
	K.			if <i>a</i> =	= 5.		
$\langle \cdot \rangle$	$\Rightarrow$	(i)	<i>a</i> = 5				
			5 <u>e</u>	$\Rightarrow e$	∈ {3, 2, 1, 0}		
			8 <sup>3</sup> ·4 − 1 ways				
	$\Rightarrow$	(ii)	<i>a</i> = 6				
			6 <u>e</u>	$\Rightarrow e$	∈ {2, 1, 0}		
			8 <sup>3</sup> ·3 ways				
	$\Rightarrow$	(iii)	<i>a</i> = 7				
			7 <u>e</u>	$\Rightarrow e$	∈ {1, 0}		
			$\Rightarrow$ 8 <sup>3</sup> ·2 ways				
	$\Rightarrow$	Tota	al ways				
		$\Rightarrow$ 8	$8^{3}(2+3+4) - 1 = 40$	608 –	1 = 4607		





Medical II	T-JEE   Foundations				JEE (Main)	-2025 :	Phase-1 (28-0
3.	If the image of the point $A$ $\frac{x-1}{2} = \frac{y-2}{1} = \frac{z-1}{1}$ is $Q(\alpha, \beta, \gamma)$			Sol.	$\int_{0}^{x} tf(t)dt = x^{2}f(x)$	)	
	equal to				Differentiating b	ooth sid	des w.r.t ' <i>x</i> '
	(1) 7				$xf(x)=x^2f'(x)+2$	xf(x)	
	(2) $\frac{31}{3}$				$\frac{x^2 dy}{dx} + xy = 0$		
	(3) $\frac{11}{3}$				$\frac{dy}{y} = \frac{-dx}{x}$		
	(4) 8				$\ln y + \ln x = \ln c$		
	wer (2)				yx = c		
ol.	<i>P</i> (4, 4, 3)				As <i>f</i> (2) = 3		
	$\frac{x-1}{2} = \frac{y-2}{1} = \frac{z-1}{1} = \lambda$				6 = <i>c</i>		
	Any pint of line $R(2\lambda + 1, \lambda + 2, \lambda)$	λ+1)			∴ <i>yx</i> = 6		
	$\overrightarrow{PR}:(2\lambda-3)\hat{i}+(\lambda-2)\hat{j}+(\lambda-2)\hat{j}$				∴ Put <i>x</i> = 6		
	$\overrightarrow{PR}$ < 2, 1, 1 > = 0	/			<i>y</i> (6) = 6		
	$2(2\lambda - 3) + (\lambda - 2) + 2(\lambda - 2) = 0$				<i>y</i> = 1		
	$2(2\lambda - 3) + (\lambda - 2) + 2(\lambda - 2) = 0$ $6\lambda = 10$				Option (1) is cor	rect	
	$\lambda = \frac{5}{2}$			5.	Let $R$ be a relat $(x + y)$ is even}, t		
	3				(1) Reflexive ar	nd sym	metric but not
	$\therefore R\left(\frac{13}{3},\frac{11}{3},\frac{8}{3}\right)$				(2) Reflexive ar	nd tran	sitive but not s
	Now, <i>Q</i> (α, β, γ)				(3) Transitive o	nly	
					(4) Equivalence relation		
	$\frac{\alpha+4}{2} = \frac{13}{3}, \ \frac{\beta+4}{2} = \frac{11}{3}, \ \frac{\gamma+3}{2} = \frac{11}{3}, \ \gamma+$	3		Ans	wer (4)		
	$\alpha = \frac{14}{3}, \ \beta = \frac{10}{3}, \ \gamma = \frac{7}{3}$		XiC	Sol.	for reflexive		
	3, 5, 3, 7, 3		Medic		If $(x, x) \in Z$		
	$\alpha + \beta + \gamma = \frac{14 + 10 + 7}{3} = \frac{31}{3}$				R : $x + x + 2x$	$\Rightarrow$	R is relexive
	3 3				For symmetric		
1.	If $\int_{0}^{x} tf(t)dt = x^{2}f(x)$ and $f(2) = 3$ ,	then <i>f</i> (6)	equals to		If $(x, y) \in R$	$\Rightarrow$	<i>x</i> + <i>y</i> = even
	0						<i>y</i> + <i>x</i> = even (
	(1) 1 (2)						R is symmetr
_	(3) 3 (4)	2			If $(x, y) \in R$		<i>x</i> + <i>y</i> = even
Ans	wer (1)				$(y, z) \in R$	$\Rightarrow$	<i>y</i> + <i>z</i> = even

that  $R = \{(x, y) : x, y \in Z \text{ and }$ elation R is tric but not transitive ve but not symmetric is relexive + *y* = even  $+x = even 6(y, x) \in R$ is symmetric





**IEE (Main)-2025 : Phase-1 (28-01-2025)-Morning**  

$$\Rightarrow x + 2y + Z \in even \Rightarrow x + Z = even - 2y even$$

$$\Rightarrow \frac{x + z \in even}{x + z \in even} \Rightarrow x + Z = even - 2y even$$

$$\Rightarrow \frac{x + z \in even}{x + z \in even} \Rightarrow x + Z = even - 2y even$$

$$\Rightarrow x + 2y + Z \in even \Rightarrow x + Z = even - 2y even$$

$$\Rightarrow x + 2y + Z = even \Rightarrow x + Z = even - 2y even$$

$$\Rightarrow x = (2\sqrt{2} - 1)$$
as  $-2\sqrt{2} - 1 < \frac{3}{2}$ 
(i)  $x \le \frac{3}{2} \Rightarrow x^2 - (2x - 3) - 4 = 0$ 

$$\Rightarrow x^2 - 2x - 1 - 0 = 0 \Rightarrow (x - 1)^2 = 2$$

$$\Rightarrow x = 2\sqrt{2} + 1 \Rightarrow x = -2\sqrt{2} + 1$$
(i)  $x \le \frac{3}{2} \Rightarrow x^2 - (2x - 3) - 4 = 0$ 

$$\Rightarrow x^2 - 2x - 1 - 0 = 0 \Rightarrow (x - 1)^2 = 2$$

$$\Rightarrow x = 2\sqrt{2} + 1 \Rightarrow x = -2\sqrt{2} + 1$$
(i)  $x \le \frac{3}{2} \Rightarrow x^2 - (2x - 3) - 4 = 0$ 

$$\Rightarrow x^2 - 2x - 1 - 0 = 0 \Rightarrow (x - 1)^2 = 2$$

$$\Rightarrow x = 2\sqrt{2} + 1 \Rightarrow x = -2\sqrt{2} + 1$$
(i)  $x \le \frac{3}{2}$ 

$$\Rightarrow two roots are  $x = -\sqrt{2} + 1, 2\sqrt{2} - 1$ 

$$\Rightarrow Sun of squares = 12 - 6\sqrt{2} - 6(2 - \sqrt{2})$$
8. Area enclosed by  
$$\{(x, y): 0 \le y \le 2|x| + 1, 0 \le y \le x^2 + 1, |x| \le 3\}$$
 is equals to  
(1)  $\frac{17}{3}$ 
(2)  $\frac{32}{3}$ 
(3)  $\frac{64}{3}$ 
(4)  $\frac{80}{3}$ 
**Answer (3) Answer (3) Area**

$$= 2\left[\frac{3}{6}(x^2 + 1)dn + \frac{1}{2}(5 + 7) \times 1\right]$$

$$= \frac{64}{3}$$$$

٨

Aakash





There are 2 bad oranges mixed with 7 good oranges and 9. 2 oranges are drawn at random. Let X be the number of bad oranges. The variance of X is

(1)	51 268	(2)	49 162
(3)	$\frac{63}{108}$	(4)	91 206

Answer (2)

Sol. 
$$\frac{X}{P(X)} \frac{0}{\frac{7}{C_2}} \frac{1}{\frac{7}{C_1} \cdot \frac{2}{C_1}} \frac{2}{\frac{2}{C_2}} \frac{2}{\frac{9}{C_2}}$$
Variance =  $0^2 \cdot \frac{7}{\frac{9}{C_2}} + 1^2 \cdot \frac{7}{\frac{9}{C_2}} + 2^2 \cdot \frac{2}{\frac{9}{C_2}}$ 

$$- \left(\frac{0 \cdot \frac{7}{C_2}}{\frac{9}{C_2}} + \frac{1 \cdot \frac{7}{C_1} \cdot \frac{2}{C_1}}{\frac{9}{C_2}} + \frac{2 \cdot \frac{2}{C_2}}{\frac{9}{C_2}}\right)^2$$

$$= \frac{7}{18} + \frac{4}{36} - \left(\frac{7}{18} + \frac{2}{36}\right)^2$$

$$= \frac{49}{162}$$
10. Let  $f(x) = \frac{2^x}{\sqrt{x}}$ , then  $\sum_{i=1}^{81} f\left(\frac{k}{x_i}\right)$  is equal to

(3) 
$$41\sqrt{2}$$
 (4) 81  
Answer (1)  
Sol.  $f(x) = \frac{2^{x}}{2^{x} + 2^{1/2}} = \frac{2^{x}}{2^{x} + \sqrt{2}}$   
 $f(1-x) = \frac{2^{1-x}}{2^{1-x} + 2^{1/2}} = \frac{\frac{2}{2^{x}}}{\frac{2}{2^{x}} + 2^{1/2}} = \frac{2}{2 + \sqrt{2} 2^{x}}$   
 $= \frac{\sqrt{2}}{2^{x} + \sqrt{2}}$   
 $\Rightarrow f(x) + f(1-x) = \frac{\sqrt{2} + 2^{x}}{\sqrt{2} + 2^{x}} = 1$ 

JEE (Main)-2025 : Phase-1 (28-01-2025)-Morning

$$\Rightarrow \sum_{k=1}^{81} f\left(\frac{k}{82}\right) + f\left(\frac{2}{82}\right) + \left(f\left(\frac{3}{82}\right)\right) + \dots$$

$$\dots + f\left(\frac{40}{82}\right) + f\left(\frac{41}{82}\right) + f\left(\frac{42}{82}\right)$$

$$+ \dots + f\left(\frac{79}{82}\right) + f\left(\frac{81}{82}\right) + f\left(\frac{81}{82}\right)$$

$$= \left[f\left(\frac{1}{82}\right) + f\left(\frac{81}{82}\right)\right] + \left[f\left(\frac{2}{82}\right) + f\left(\frac{80}{82}\right)\right] + \dots$$

$$+ \left[f\left(\frac{40}{82}\right) + f\left(\frac{42}{82}\right) + f\left(\frac{41}{82}\right)\right]$$

$$= \left(\frac{1+1+\dots+1}{40 \text{ times}}\right) + f\left(\frac{1}{2}\right)$$

$$= 40 + \frac{\sqrt{2}}{\sqrt{2} + \sqrt{2}} = 40 + \frac{1}{2} = \frac{81}{2}$$
11. If  $2a_{n+2} = 5a_{n+1} - 3a_n$ , where  $n = 0, 1, 2, \dots$ . If  $a_0 = 3$  and  $a_1 = 4$ , then the value of  $\sum_{k=1}^{100} a_k$  is equal to  
(1)  $3a_{100} - 91$  (2)  $3a_{99} - 91$   
(3)  $3a_{100} + 91$  (4)  $3a_{99} + 91$ 
Answer (1)  
Sol.  $2a_{n+2} = 5a_{n+1} - 3a_n = 0$ 

$$\Rightarrow t = 1, \frac{3}{2}$$

$$\therefore a_n = A \cdot (1)^n + B \cdot \left(\frac{3}{2}\right)^2$$
 $a_0 = 3, a_1 = 4$ 

$$\therefore A = 1, B = 2$$
 $a_n = 1 + 2 \cdot \left(\frac{3}{2}\right)^n$ 
 $S_{100} = 100 - 6\left(1 - \left(\frac{3}{2}\right)^{100}\right)$ 

 $= 3a_{100} - 99$ 



Using 
$$\Rightarrow \left(\frac{3}{2}\right)^{100} = \left(\frac{a_{100} - 1}{2}\right)^{100}$$
  
 $a_{100} = 2 \cdot \left(\frac{3}{2}\right)^{100} + 1$ 

12. Let  $k_1$  and  $k_2$  be two randomly selected natural numbers.

The probability that  $(i)^{k_1} + (i)^{k_2}$  is non-zero is (where *i*  $=\sqrt{-1}$ ) (1)  $\frac{1}{2}$ (2)  $\frac{3}{4}$ (4)  $\frac{1}{6}$ (3)  $\frac{1}{4}$ 

#### Answer (2)

**Sol.** 
$$(i)^{k_1} + (i)^{k_2}$$
 is non zero

$$\Rightarrow k_1 : 4\lambda_1 + r_1, \quad r_1 \in \{0, 1, 2, 3\}$$
$$K_2 : 4\lambda_2 + r_2, \quad r_2 \in \{0, 1, 2, 3\}$$

The pairs to get zero will be

- (1, -1), (i, -i)
- $\Rightarrow$  (i) (1, -1) pair  $\Rightarrow$  ( $r_1, r_2$ )  $\in$  {(2, 0), (0, 2)} (ii) (*i*, –*i*) pair  $\Rightarrow$  ( $r_1, r_2$ )  $\in$  {(1, 3), (3, 1)}

$$\Rightarrow \text{ probablity } \left(i^{k_1} + i^{k_2} \neq 0\right)$$

= 1 – probablity  $(i^{k_1} + i^{k_2} \neq 0)$ 

- $=1-\frac{4}{16}=\frac{12}{16}=\frac{3}{4}$
- Nedici 13. In  $\triangle ABC$ ,  $A(4\sin\theta, 4\cos\theta)$ ,  $B(-2\cos\theta, 0)$  and  $C(2, 2\sin\theta)$ . If locus of centroid is  $(3x - 2)^2 + (3y)^2 = \alpha$ , then  $\alpha$  is
  - (1) 20
  - (2) 4
  - (3) 16
  - (4) 12

#### Answer (1)

Sol. 
$$h = \frac{4\sin\theta - 2\cos\theta + 2}{3} \Rightarrow 3h - 2 = 4\sin\theta - 2\cos\theta \dots (1)$$

$$k = \frac{4\cos\theta - 2\sin\theta}{3} \Rightarrow 3k = 4\cos\theta + 2\sin\theta \dots (2)$$

$$(1)^{2} + (2)^{2}$$

$$(3h - 2)^{2} + (3k)^{2} = (4\sin\theta - 2\cos\theta)^{2} + (4\cos\theta + 2\sin\theta)^{2}$$

$$= 16\sin^{2}\theta + 4\cos^{2}\theta - 8\sin\theta\cos\theta + 16\cos^{2}\theta + 4\sin^{2}\theta - 8\sin\theta\cos\theta$$

$$(3h - 2)^{2} + (3k)^{2} = 20$$

$$(3x - 2)^{2} + (3k)^{2} = 20$$
14. Let  $E_{1} : \frac{x^{2}}{9} + \frac{y^{2}}{4} = 1$  be an ellipse and a series of ellipse are drawn that  $E_{l+1}$  has same centre, eccentricity as  $E_{l}$  and  $E_{l+1}$ 's major axis is minor axis of  $E_{l}$ . If  $S_{l}$  be the area of  $E_{l}$ , then  $\left(\frac{5}{\pi}\sum_{l=1}^{\infty}S_{l}\right)$  is equal to
$$(1) \quad 63 \qquad (2) \quad 54$$

$$(3) \quad 45 \qquad (4) \quad 72$$
Answer (2)
Sol. Let  $b_{l}$  be minor axis of  $E_{l}$ 

$$a_{l}$$
 be major axis of  $E_{l+1}$ 

$$A_{l+1}$$
 major axis of  $E_{l+1}$ 

$$\Rightarrow e_{l+1} = 1 - \frac{b_{l+1}^{2}}{a_{l+1}^{2}}$$
, also  $a_{l+1} = b_{l}$  and  $e_{l} = e_{l+1}$ 

$$= \frac{b_{l}^{2}}{a_{l}^{2}} = \frac{b_{l+1}^{2}}{(b_{l})^{2}} \Rightarrow b_{l+1} = \frac{b_{l}^{2}}{a_{l}}$$

 $\Rightarrow$  Area of  $E_i = S_i = pa_ib_i$ 

$$\Rightarrow S_{i+1} = \pi a_{i+1} b_{i+1}$$
$$= \pi (b_i) \left( \frac{b_i^2}{a_i} \right)$$





$$= \pi(b_i a_i) \left(\frac{b_i}{a_i}\right)^2$$

$$S_{i+1} = S_i (1 - e_i^2)$$

$$\Rightarrow S_{i+1} = S_i \left(1 - \left(1 - \frac{4}{9}\right)\right) = S_i \cdot \frac{4}{9}$$

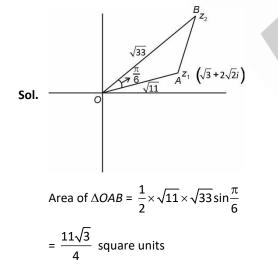
$$\Rightarrow S_i = 6\pi, S_2 = 6\pi \cdot \frac{4}{9} S_3 = 6\pi \cdot \left(\frac{4}{9}\right)^2$$

$$\Rightarrow \sum_{k=1}^{\infty} S_i = \left(\frac{6\pi}{1 - \frac{4}{9}}\right) = \frac{54\pi}{5}$$

$$\Rightarrow \frac{5}{\pi} \sum_{k=1}^{\infty} S_i = \frac{5}{\pi} \cdot \frac{54\pi}{5} = 54$$
15. Let  $z_1 = \sqrt{3} + 2\sqrt{2}i$  and  $\sqrt{3} |z_1| = |z_2|$  and  $\arg(z_2) = \arg(z_1) + \frac{\pi}{6}$ , then the area of triangle with vertices  $z_1, z_2$  and origin is (in sq. units)

(1) 
$$\frac{11\sqrt{3}}{4}$$
 (2)  $\frac{11\sqrt{2}}{3}$   
(3)  $\frac{11}{4}$  (4)  $\frac{2\sqrt{2}}{3}$ 

Answer (1)



### JEE (Main)-2025 : Phase-1 (28-01-2025)-Morning

16. Let 
$$f(x) = \begin{cases} 2x, \ x < 0 \\ \min(1 + x + [x], 1 + 2[x]), \ 0 \le x < 2 \\ 5, \ x \ge 2 \end{cases}$$

If  $\alpha$  is the number of points of discontinuity and  $\beta$  is the number of points of non-differentiability, then  $(\alpha + \beta)$  is equal to (where [.] denote greatest integer function)

Answer (1)

Sol. 
$$f(x) = \begin{cases} 2x, & x < 0 \\ \min(1+x+[x], 1+2[x]), & 0 \le x < 2 \\ 5 & x \ge 2 \end{cases}$$
$$1+x+[x] = 1+\{x\}+2[x]$$
Since  $\{x\} \ge 0 \ \forall x \in R$ 
$$\Rightarrow 1+x+[x] \ge 1+2[x]$$
$$\Rightarrow f(x) = \begin{cases} 2x, & x < 0 \\ 1+2[x], & 0 \le x < 0 \\ 5 & x \ge 2 \end{cases}$$

Number of discontinuity =  $3 \Rightarrow \alpha = 3$ Number of point of non-differentiability =  $3 \Rightarrow \beta = 3$ 

- 17. If  $\alpha = 1 + \sum_{n=1}^{6} (-3)^{n-1} \cdot {}^{12}C_{2n-1}$ , then distance of point  $(12, \sqrt{3})$  from the line  $\alpha x \sqrt{3}y + 100 = 0$  is, (1)  $\frac{109}{2}$ (2) 55
  - (3) 54

(4) 109





ledic

$$\begin{aligned} \text{Sol.} \quad & \alpha = 1 + \sum_{r=1}^{6} (-3)^{r-1} \cdot {}^{12}C_{2r-1} \\ & = 1 + \sum_{r=1}^{6} \left[ \left( \sqrt{3}i \right)^2 \right]^{r-1} \cdot {}^{12}C_{2r-1} \\ & = 1 + \frac{1}{\sqrt{3}i} \sum_{r=1}^{6} \left( \sqrt{3}i \right)^{2r-1} \cdot {}^{12}C_{2r-1} \\ & \text{Let } \sqrt{3}i = x \\ & \Rightarrow \quad \alpha = 1 + \frac{1}{\sqrt{3}i} \sum_{r=1}^{6} {}^{12}C_{2r-1} \cdot x^{2r-1} \\ & \alpha = 1 + \frac{1}{\sqrt{3}i} \left[ {}^{12}C_1 \cdot x^1 + {}^{12}C_3 \cdot x^3 + {}^{12}C_5 \cdot x^5 + \\ & \dots + {}^{12}C_{11} \cdot x^{11} \right] \\ & \text{Let} \quad \begin{pmatrix} 1 + x \end{pmatrix}^{12} = {}^{12}C_0 \cdot x^0 + {}^{12}C_1 \cdot x^1 + \\ & {}^{12}C_2 \cdot x^2 + \dots + {}^{12}C_{12} \cdot x^{12} \\ & (1 - x)^{12} = {}^{12}C_0 \cdot x^0 - {}^{12}C_1 \cdot x^1 + \\ & {}^{12}C_2 \cdot x^2 + \dots + {}^{12}C_{12} \cdot x^{12} \\ & (1 - x)^{12} = {}^{12}C_0 \cdot x^0 - {}^{12}C_1 \cdot x^1 + \\ & {}^{12}C_2 \cdot x^2 - {}^{12}C_3 \cdot x^3 \dots + {}^{12}C_{12} \cdot x^{12} \\ & (1 + x)^{12} - (1 - x)^{12} = 2 \left( {}^{12}C_1 \cdot x^1 + {}^{12}C_3 \cdot x^3 + \\ & \dots + {}^{12}C_{11} \cdot x^{11} \right) \\ & \Rightarrow \quad \alpha = 1 + \frac{1}{\sqrt{3}i} \left[ \frac{\left( 1 + \sqrt{3}i \right)^{12} - \left( 1 - \sqrt{3}i \right)^{12}}{2} \right] \\ & \alpha = 1 + \frac{1}{\sqrt{3}i} \left[ \frac{\left( 1 + \sqrt{3}i \right)^{12} - \left( 1 - \sqrt{3}i \right)^{12}}{2} \right] \\ & \text{Since, } \quad \omega = -\frac{1}{2} + \frac{\sqrt{3}i}{2} \qquad \Rightarrow \quad -2\omega = 1 - \sqrt{3}i \\ & \omega^2 = -\frac{1}{2} - \frac{\sqrt{3}i}{2} \qquad \Rightarrow \quad -2\omega^2 = 1 + \sqrt{3}i \\ & \Rightarrow \quad \alpha = 1 + \frac{1}{\sqrt{3}i} \left( \frac{\left( -2\omega^2 \right)^{12} - \left( 2\omega \right)^{12}}{2} \right) \\ & = 1 + \frac{2^{11}}{\sqrt{3}i} \left( \omega^{24} - \omega^{12} \right) \end{aligned}$$

$$= 1 + \frac{2^{11}}{\sqrt{3i}} (1 - 1) = 1$$
  

$$\alpha = 1, \implies \text{perpendicular distance from } (12, \sqrt{3}) \text{ is}$$
  

$$\frac{\left|12 - \sqrt{3}(\sqrt{3}) + 100\right|}{\sqrt{1^2 + (\sqrt{3})^2}} = \frac{109}{2}$$

kash

18.

19.

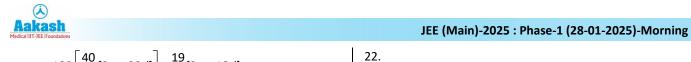
20.

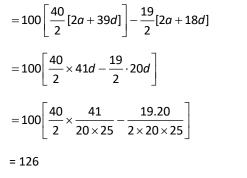
#### SECTION - B

**Numerical Value Type Questions:** This section contains 5 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

21. In an AP,  $T_m = \frac{1}{25}$ ,  $T_{25} = \frac{1}{20}$  and  $20\sum_{r=1}^{25} T_r = 13$ , then  $5m\sum_{r=m}^{2m} T_r$  equals Answer (126) Sol.  $T_m = a + (m+1)d \cdot \frac{1}{25}$  ...(1)  $T_{25} = a + 24d = \frac{1}{20}$   $20 \times \frac{2r}{2} \left[ a + \frac{1}{20} \right] = 13 \Rightarrow a = \frac{1}{20 \times 25}$   $20\sum_{r=1}^{25} T = 20 \times \frac{25}{2} [2a + 24d] = 13$   $d = \frac{1}{20 \times 25}$ Substitute a and d in (i)  $\Rightarrow m = 20$ Now  $5m\sum_{r=m}^{2m} T_r = 5 \times 20 \left[ \sum_{r=20}^{40} T_r \right]$ 







25.



