

KOLHAN UNIVERSITY, CHAIBASA JHARKHAND



Syllabus for FYUGP (Mathematics Major & Minor)

As per

Revised Curriculum and Credit Frame work of NEP- 2020

To be effective from academic session 2022-26

University Department of Mathematics
Kolhan University, Chaibasa
West Singhbhum, Jharkhand-833202

**UNIVERSITY DEPARTMENT OF MATHEMATICS
KOLHAN UNIVERSITY, CHAIBASA**

Four-Year under Graduate Programme (FYUGP)

As per Provisions of NEP-2020 to be implemented from Academic Year 2022-23

COMPOSITION OF BOARD OF STUDIES

1. **Dr. Bijay Kumar Sinha**
Head, University Department of Mathematics,
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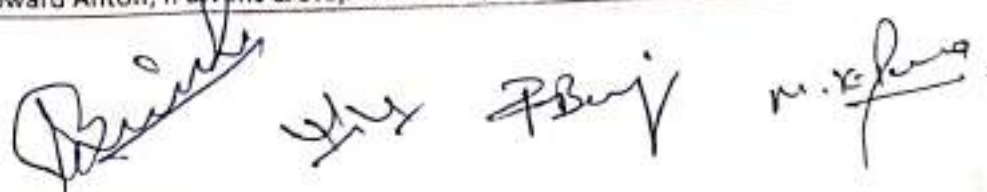
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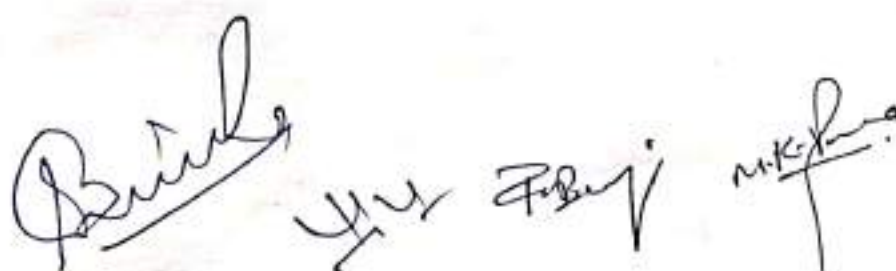
| Semester | Paper | Code | Course Title | Credit |
|----------|------------------|-------|---------------------------------------------|--------|
| I | Major-01 | MJ-1 | Calculus | 4 |
| | Major-02 | MJ-2 | Matrices | 4 |
| II | Major-03 | MJ-3 | Analytical Geometry & Trigonometry | 4 |
| | Major-04 | MJ-4 | Real Analysis | 4 |
| III | Major-05 | MJ-5 | Vector | 4 |
| | Major-06 | MJ-6 | Real Analysis & Set theory | 4 |
| IV | Major-07 | MJ-7 | Ordinary Differential Equation | 4 |
| | Major-08 | MJ-8 | Group Theory | 4 |
| | Major-09 | MJ-9 | Mechanics | 4 |
| V | Major-10 | MJ-10 | Theory of Equation & Higher Arithmetic | 4 |
| | Major-11 | MJ-11 | Complex Analysis | 4 |
| | Major-12 | MJ-12 | Dynamics & Statics | 4 |
| VI | Major-13 | MJ-13 | LPP & Statistics | 4 |
| | Major-14 | MJ-14 | Analysis II & Ring | 4 |
| | Major-15 | MJ-15 | Numerical Analysis & Programming in C | 4 |
| VII | Major-16 | MJ-16 | Fluid Mechanics & Special Function | 4 |
| | Major-17 | MJ-17 | Metric space & Discrete Mathematics | 4 |
| | Major-18 | MJ-18 | Integral Transform | 4 |
| | Major-19 | MJ-19 | Partial Differentiation | 4 |
| VIII | Major-20 | MJ-20 | Linear Algebra & Linear Difference equation | 4 |
| | Advance Major-01 | AMJ-1 | Topology | 4 |
| | Advance Major-02 | AMJ-2 | Complex Analysis II | 4 |
| | Advance Major-03 | AMJ-3 | Real Analysis & Measure Theory | 4 |



| Program: Certificate | Year: First | Semester: I |
|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------|
| Class: UG | | |
| Subject: Mathematics | | |
| Course Code: MJ-1 | Course Title: Calculus | |
| Course Learning Outcomes: This course will enable the students to: <ol style="list-style-type: none"> Apply the rules of differentiation, including the chain rule, to compute derivatives of functions. Also, able to apply different mean value theorems, such as Rolle's theorem and Lagrange's mean value theorem, to establish results about the behavior of differentiable functions. Approximate functions using Maclaurin's and Taylor's series, analyze the error of these approximations using Taylor's theorem with Lagrange, Cauchy, and Roche-Schlomilch forms of remainder, and use these results to find extrema of functions. Define and compute the curvature of a curve at a given point, and understand its geometric significance and identify the different types of asymptotes of general algebraic curves, including parallel asymptotes, asymptotes parallel to axes, and slant asymptotes. Trace Cartesian, polar, and parametric curves and identify their key features, as well as use calculus techniques to analyze the behavior of curves and solve real-world problems that involve curve tracing. Derive and apply reduction formulae, parameterize curves, and compute arc length, area of bounded curves, volume, and surface area of surfaces of revolution. | | |
| Credit: 4 (Theory) | Compulsory | |
| Full Marks: 75 | Time: 3 Hours | |
| Unit | Content | Hours |
| I | Differential calculus: Differentiability of a real valued function, Geometrical interpretation of differentiability, Rules of differentiation, Chain rule of differentiation; Darboux's theorem, Rolle's theorem, Lagrange's mean value theorem, Cauchy's mean value theorem, Geometrical interpretation of mean value theorems, Successive differentiation, Leibnitz's theorem. | 15 h |
| II | Expansions of Functions: Maclaurin's and Taylor's theorems for expansion of a function in an infinite series, Taylor's theorem in finite form with Lagrange, Cauchy and Roche-Schlomilch forms of remainder, Maxima and minima. | 12 h |
| III | Curvature and Asymptotes: Curvature; Asymptotes of general algebraic curves, Parallel asymptotes, Asymptotes parallel to axes; Symmetry, Concavity and convexity, Points of inflection, Tangents at origin, Multiple points, Position and nature of double points. | 13 h |
| IV | Curve Tracing: Tracing of Cartesian, polar and parametric curves; Envelope and evolutes. | 10 h |
| V | Integral Calculus: Reduction formulae, derivations and illustrations of reduction formulae of the type $\int \sin^n x \, dx$, $\int \cos^n x \, dx$, $\int \tan^n x \, dx$, $\int \sin^n x \cos^m x \, dx$ and $\int \cos^n x \sin^m x \, dx$, parametric equations, parameterizing a curve, arc length, arc length of parametric curves, Area of bounded curve, volume and area of surface of revolution. | 10 h |
| Sessional Internal Assessment (SIA) Full Marks – 25 Marks A – Internal written Examination – 20 Marks (1 Hr) B – Over All Performance including Regularity – 05 Marks | | |
| Books Recommended: 1. R. K. Dwivedi, Calculus, 1 st Edition, Pragati Prakashan, Meerut, India (2019). 2. Howard Anton, I. Bivens & Stephan Davis (2016). Calculus (10th edition). Wiley India. | | |



| Program: Certificate | Year: First | Semester: II |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------|
| Class: UG | | |
| Subject: Mathematics | | |
| Course Code: MJ-2 | Course Title: Matrices | |
| Course Learning Outcomes: This course will enable the students to: <ol style="list-style-type: none"> Understand and apply fundamental concepts in number theory, including well ordering property, division algorithm, congruence relations, mathematical induction, and the fundamental theorem of arithmetic. Gain a thorough understanding of matrices, including types of matrices, determinants, operations, invertibility, matrix rank, normal forms, and the rank-nullity theorem. Gain a strong grasp of systems of linear equations, including their matrix form, augmented matrices, consistency (both necessary and sufficient conditions), and methods for solving homogeneous and non-homogeneous linear equations. Find eigenvalues and corresponding eigenvectors for a square matrix. | | |
| Credit: 4 (Theory) | Compulsory | |
| Full Marks: 75 | Time: 3 Hours | |
| Unit | Content | Hours |
| I | Theory of numbers: Well-ordering property (WOP) of positive integers, Division algorithm, Divisibility and Euclidean algorithm, Congruence relation between integers, Principles of Mathematical Induction, Fundamental Theorem of Arithmetic. | 15 h |
| II | Matrices: Matrices and types of matrices, determinants, operations on matrices, submatrix, block Matrix, Invertible Matrices, Uniqueness of Inverse Matrix, Rank of a matrix, Normal form PAQ, Canonical or Echelon form, Rank-Nullity Theorem of a Matrix. | 15 h |
| III | System of linear equations: Matrix form of system of linear equations, augmented matrix, consistent and inconsistent system of linear equations, necessary and sufficient condition consistency of a system of linear equations, method of solving of homogeneous and non-homogeneous linear equations. | 15 h |
| IV | Eigen values and Eigen vectors of matrices: Characteristic polynomial of a matrix, Eigen values and Eigen vectors, A.M. and G.M. of Eigen values, Theorems on Eigen values and Eigen vectors, Minimal Polynomial, Cayley-Hamilton theorem. | 15 h |
| Sessional Internal Assessment (SIA) Full Marks – 25 Marks A – Internal written Examination – 20 Marks (1 Hr) B – Over All Performance including Regularity – 05 Marks | | |
| Books Recommended: <ol style="list-style-type: none"> David M. Burton (2007). Elementary Number Theory (7th edition). McGraw-Hill Vasishtha A. R., Vasishtha A. K. (2011). Matrices. Krishna's Prakashan Media (P) Ltd Bernard Kolman & David R. Hill (2003). Introductory Linear Algebra with Applications (7th edition). Pearson Education Pvt. Ltd. India. David C. Lay, Steven R. Lay & Judi J. McDonald (2016). Linear Algebra and its Applications (5th edition), Pearson Education Pvt. Ltd. India. Pankaj Kumar Manjhi (2018). Algebra. (1st edition) Pragati Prakashan, Meerut | | |



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| Program: Certificate | Year: First | Semester: II |
| Class: UG | | |
| Subject: Mathematics | | |
| Course Code: MJ-3 | Course Title: Analytic Geometry and Trigonometry | |

Course Learning Outcomes: This course will enable the students to:

- Develop skills in two-dimensional analytical geometry, including transformations of rectangular axes, reduction of general equations to normal form, analysis of conic systems, and understanding the polar equation of conics.
- Gain proficiency in three-dimensional analytical geometry, including the concepts of direction cosines, straight lines, planes, spheres, intersecting spheres, spheres passing through a given circle, cones, and cylinders.
- Gain the ability to analyze and classify conicoids, understand their plane sections, determine generating lines, reduce equations to normal form, and classify quadrics.
- Develop concepts in trigonometry, including the polar form of complex numbers, DeMoivre's theorem, and its applications in trigonometric function expansions.
- Develop proficiency in working with hyperbolic and exponential functions, understanding their properties and applications.

Credit: 4 (Theory) Compulsory

Full Marks: 75 Time: 3 Hours

| Unit | Content | Hours |
|------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------|
| I | Analytical geometry of two dimensions: Transformation of rectangular axes, General equation of second degree and its reduction to normal form, Systems of conics, Polar equation of a conic. | 15 h |
| II | Analytical geometry of three dimensions: Direction cosines, Straight line, Plane, Sphere, Two Intersecting Spheres, Spheres Through a Given Circle, Cone, Cylinder. | 15 h |
| III | Conicoid: Central conicoids, paraboloids, plane sections of conicoids, Generating lines. Reduction of second-degree equations to normal form; classification of quadrics. | 15 h |
| IV | Trigonometry: Polar form of complex number, nth roots of unity, De-Moivre's Theorem, Applications of De-Moivre's Theorem in expansions trigonometric function, Hyperbolic function, Exponential Function and their properties. | 15 h |

Sessional Internal Assessment (SIA) Full Marks – 25 Marks

A – Internal written Examination – 20 Marks (1 Hr)

B – Over All Performance including Regularity – 05 Marks

Books Recommended:

- Loney, S. L., Elements of Coordinate Geometry.
- Shanti Narayan, Analytical Geometry – Three Dimensions.
- Bell, R- J. T., Elementary Treatise on Coordinate Geometry.
- Chaki, M. C, A Textbook of Analytical Geometry, Calcutta Publishers.
- Chakraborty, J. G., and Ghosh, P. R., Advanced Analytical Dynamics.
- Titu Andreescu, & Dorin Andrica (2011) ... Complex Numbers from A to...Z. (2nd edition). Birkhauser.
- James Ward Brown and Ruel V. Churchill, Complex Variables and Applications, 8th Ed., McGraw – Hill International Edition. Mfg)

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| Program: Diploma | Year: Second | Semester: III |
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| Class: UG | | |
| Subject: Mathematics | | |
| Course Code: MJ-4 | Course Title: Real Analysis | |
| Course Learning Outcomes: This course will enable the students to: <ol style="list-style-type: none"> Understand many properties of the real line \mathbb{R} and learn to define sequence in terms of functions from \mathbb{R} to a subset of \mathbb{R}. Recognize bounded, convergent, divergent, Cauchy and monotonic sequences and to calculate their limit superior, limit inferior, and the limit of a bounded sequence. Apply the ratio, root, alternating series and limit comparison tests for convergence and absolute convergence of an infinite series of real numbers. Learn some of the properties of Riemann integrable functions, and the applications of the fundamental theorems of integration. | | |
| Credit: 4 (Theory) | Compulsory | |
| Full Marks: 75 | Time: 3 Hours | |
| Unit | Content | Hours |
| I | Real Number System Axioms in \mathbb{R} , Absolute value of a real number; Bounds of a sets, Supremum and infimum of a nonempty subset of \mathbb{R} , The completeness property of \mathbb{R} , Archimedean property, Definition and types of intervals, Neighborhood of a point in \mathbb{R} , Open, closed and perfect sets in \mathbb{R} | 15 h |
| II | Sequences of Real Numbers: Convergent sequence, Limit of a sequence, Bounded sequence, Limit theorems, Monotone sequences, Weierstrass' theorem for \square sequences, Monotone convergence theorem, Subsequences, Bolzano sequences, Limit superior and limit inferior of a sequence of real numbers, Cauchy sequence, Cauchy's first theorem on limit, Cauchy's convergence criterion, Completeness property of set of real number. | 15 h |
| III | Infinite Series Convergence and divergence of infinite series of positive real numbers, Necessary condition for convergence, Cauchy criterion for convergence; Tests for convergence of positive term series; Basic comparison test, Limit comparison test, D'Alembert's ratio test, Raabe's test, Logarithmic test, Cauchy's condensation Test, De Morgan & Bertrand's test, Higher logarithmic test, Gauss's test, Cauchy's root test, Integral test; | 20 h |
| IV | Alternating series: Alternating series, Leibniz test, Absolute and conditional convergence. Properties of absolutely convergent series. | 10 h |
| Sessional Internal Assessment (SIA) Full Marks 25 Marks A Internal written Examination 20 Marks (1 Hr) B Over All Performance including Regularity 05 Marks | | |
| Books Recommended: 1. Real Analysis: Dasgupta & Prasad 2. Real Analysis: Lalji Prasad 3. Real Analysis: K.K. Jha 4. Principle of Real Analysis: S. C. Malik | | |

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| Program: Diploma | Year: Second | Semester: III |
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| Class: UG | | |
| Subject: Mathematics | | |
| Course Code: MJ-5 | Course Title: Vectors | |
| Course Learning Outcomes: This course will enable the students to: <ul style="list-style-type: none"> a) Understand the concepts of scalar & vector products of three and four vectors. b) Understand the concept of vector function of scalar variable t, Scalar point functions, vector point functions, Grad, Curl and Divergence. c) Inter-relationship amongst the line integral, double and triple integral formulations d) Realize importance of Green, Gauss and Stokes' theorems in other branches of mathematics. | | |
| Credit: 4 (Theory) | Compulsory | |
| Full Marks: 75 | Time: 3 Hours | |
| Unit | Content | Hours |
| I | Product of three & four vectors: Product of 3 & 4 vectors, Reciprocal system of vectors, Lami's theorem, $\lambda - \mu$ theorem, work done, Moment of force. Couple. | 15 h |
| II | Vector Differentiation: Vector function of scalar variable t , it's derivative and geometrical meaning. Derivative of product of two and three vectors | 15 h |
| III | Grad, Divergence & Curl: Scalar point function and vector point function, grad, divergence and curl, their expansion formulae and properties. | 15 h |
| IV | Green's, Stoke's & Gauss's Divergence theorem: Line integrals. Applications of line integrals: Mass and Work, Fundamental theorem for line integrals, Conservative vector fields, Green's theorem, Area as a line integral, Surface integrals, Stokes' theorem, The Gauss divergence theorem. | 15 h |
| Sessional Internal Assessment (SIA) Full Marks - 25 Marks A Internal written Examination - 20 Marks (1 Hr) B Over All Performance including Regularity - 05 Marks | | |
| Books Recommended: <ol style="list-style-type: none"> 1. <i>Advanced Engineering Mathematics</i> (10th edition). Erwin Kreyszig, Wiley 2. <i>Vector Analysis</i>: Lalji Prasad, Paramount | | |

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| Program: Diploma Class: UG | | Year: Second | Semester: IV |
| Subject: Mathematics | | | |
| Course Code: MJ-6 | | Course Title: Real Analysis & Set theory | |
| Course Learning Outcomes: This course will enable the students to: | | | |
| a) Understand the concept of limit & continuity of a function. b) Understand the concept of differentiation and expansion of function with remainder. c) Understand the definition and condition for Riemann Integrability. d) Understand the generalized set operations and relation on sets. | | | |
| Credit: 4 (Theory) | | Compulsory | |
| Full Marks: 75 | | Time: 3 Hours | |
| Unit | Content | | Hours |
| I | Limit and Continuity: Limit, Continuity, Discontinuities, uniform continuity, properties of functions continuous in closed intervals, Functions of bounded variation. | | 15 h |
| II | Derivability, Relationship with continuity, Taylor's theorem, Maclaurin's theorem, remainder after n terms, Power series expansion of $(1+x)^n$, $\sin x$, $\cos x$ and $\log(1+x)$ using suitable remainder after n terms. | | 15 h |
| III | Riemann Integration Definition, Darboux's theorem I & II. Integrability condition, particular classes of bounded integrable function primitive, fundamental theorem, first and second Mean value theorem. | | 15 h |
| IV | Index family of sets, Generalised set operations & De-Morgan Laws, set Bijection mapping: Countable and Uncountable sets, Equivalence relation and related fundamental theorem on partition. Partial order & Total order relation | | 15 h |
| Sessional Internal Assessment (SIA) Full Marks : 25 Marks | | | |
| A Internal written Examination : 20 Marks (1 Hr) | | | |
| B Over All Performance including Regularity : 05 Marks | | | |
| Books Recommended: | | | |
| 1. Real Analysis by Lalji Prasad | | | |
| 2. Real Analysis by K. K. Jha | | | |
| 3. Principle of Real Analysis: S. C. Malik | | | |

Prasad

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Prasad



K. K. Jha

| Program: Diploma Class: UG | Year: Second | Semester: IV |
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| Subject: Mathematics | | |
| Course Code: MJ-7 | Course Title: Ordinary Differential Equation | |
| Course Learning Outcomes: This course will enable the students to: <ol style="list-style-type: none"> solve ordinary differential equation of first order and understand its physical significance. solve higher order differential equation using concept of complimentary function & particular integral. solve ordinary differential equation with variable coefficients. solve simultaneous & total differential equation and understand its geometrical significance. | | |
| Credit: 4 (Theory) | Compulsory | |
| Full Marks: 75 | Time: 3 Hours | |
| Unit | Content | Hours |
| I | First order higher degree ordinary differential equations, Equation solvable for y, solvable for x, Clairaut's form, singular solution orthogonal trajectories. | 15 h |
| II | Linear Differential Equation of higher order with constant coefficients. Homogeneous linear differential equation (Cauchy- Euler's Form) | 15 h |
| III | Second order linear differential equations: Normal forms (removal of first derivative) solution by changing independent variable and by variation of parameters. | 15 h |
| IV | Simultaneous equation $dx/P = dy/Q = dz/R$ and Total differential equation $Pdx+Qdy+Rdz=0$ together with their geometrical significance. | 15 h |
| Sessional Internal Assessment (SIA) Full Marks . 25 Marks A. Internal written Examination . 20 Marks (1 Hr) B. Over All Performance including Regularity . 05 Marks | | |
| Books Recommended: <ol style="list-style-type: none"> Differential Equation by Lalji Prasad Advanced differential equation by M. D. Raisinghania Differential equation by J. N. Sharma | | |



| Program: Diploma | Year: Second | Semester: IV |
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| Class: UG | | |
| Subject: Mathematics | | |
| Course Code: MJ-8 | Course Title: Group Theory | |
| Course Learning Outcomes: This course will enable the students to: | | |
| a) Understand concept of groups & their properties. b) Understand the concept of subgroups and cyclic groups. c) Understand the concept of Factor group, centralizer and normalizer of group. d) Understand the concept of Homomorphism in Group & Isomorphism and related properties. | | |
| Credit: 4 (Theory) | Compulsory | |
| Full Marks: 75 | Time: 3 Hours | |
| Unit | Content | Hours |
| I | Definition and examples of groups including dihedral, permutation and quaternion groups, Elementary properties of groups. | 15 h |
| II | Subgroups and examples of subgroups, Cyclic groups, Properties of cyclic groups, Classification of subgroups of cyclic groups, Order of group, Lagrange's theorem, | 15 h |
| III | Properties of cosets, Normal subgroups, Simple groups, Factor groups, Cauchy's theorem for finite abelian groups; Centralizer, Normalizer, Center of a group, Cycle notation for permutations, Properties of permutations, Even and odd permutations, alternating groups. | 15 h |
| IV | Group homomorphisms, Properties of homomorphisms, Group isomorphisms, Properties of isomorphisms; Fundamental theorem of homomorphism. Cayley's theorem and its applications. | 15 h |
| Sessional Internal Assessment (SIA) Full Marks: 25 Marks | | |
| A. Internal written Examination: 20 Marks (1 Hr) | | |
| B. Over All Performance including Regularity: 05 Marks | | |
| Books Recommended: | | |
| 1. Modern Algebra: Surjeet Singh Quazi Zameeruddin | | |
| 2. Modern Algebra: A R Vasistha | | |
| 3. Topics in Algebra: I. N. Herstein | | |
| 4. A First Course in Abstract Algebra: J. B. Fraleigh | | |

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| Program: Bachelor's Degree | | Year: Third | Semester: V |
| Class: UG | | | |
| Subject: Mathematics | | | |
| Course Code: MJ-9 | | Course Title: Mechanics | |
| Course Learning Outcomes: This course will enable the students to: | | | |
| a) Understand necessary conditions for the equilibrium of particles acted upon by various forces and learn the principle of virtual work for a system of coplanar forces acting on a rigid body. b) Understand the concept of friction and laws of friction. Student will be able to solve problems related to friction. c) Deal with the kinematics of the rectilinear and planar motions of a particle including the constrained oscillatory motions of particles. d) Understand concept work and energy and related laws. | | | |
| Credit: 4 (Theory) | | Compulsory | |
| Full Marks: 75 | | Time: 3 Hours | |
| Unit | Content | | Hours |
| I | Reduction of system of coplanar forces, equation of resultant. Condition for equilibrium, astatic centre. Work and potential energy, Principle of virtual work for a system of coplanar forces acting on a particle or at different points of a rigid body, Forces which can be omitted in forming the equations of virtual work. | | 15 h |
| II | Laws, Angles and cone of friction, equilibrium on a rough inclined plane, particle constrained to move on a rough curve under any given forces. | | 15 h |
| III | Kinematics in two dimensions: tangential, normal, radial, transverse velocities and acceleration. Angular Velocity and acceleration. Rectilinear motion and simple pendulum: S.H.M., compounding of two S.H.M., Repulsive motion, motion under inverse square law. | | 15 h |
| IV | Rectilinear Motion (Kinetics): Newton's Law, work, KE, work Energy principle, impulse, Torque and angular momentum, conservation of energy, momentum and angular momentum, Hooke's law. Extension of an elastic string: horizontal & vertical case. | | 15 h |
| Sessional Internal Assessment (SIA) Full Marks . 25 Marks A Internal written Examination . 20 Marks (1 Hr) B Over All Performance including Regularity . 05 Marks | | | |
| Books Recommended: | | | |
| 1. Mechanics: Singh & Sen 2. Statics and Dynamics. A. R. Vashishtha Krishna. 3. Statics. S. Ramsey Cambridge University Press. 4. Dynamics. S. Ramsey Cambridge University Press. | | | |


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| Program: Bachelor's Degree | | Year: Third | Semester: V |
| Class: UG | | | |
| Subject: Mathematics | | | |
| Course Code: MJ-10 | | Course Title: Theory of Equation & Higher Arithmetic | |
| Course Learning Outcomes: This course will enable the students to: | | | |
| a) solve polynomial equation using relation of roots and coefficients b) solve cubic equation by Cardon's method. c) understand the concept of congruences and their properties. d) solve simultaneous linear congruences. | | | |
| Credit: 4 (Theory) | | Compulsory | |
| Full Marks: 75 | | Time: 3 Hours | |
| Unit | Content | | Hours |
| I | Relations of root and their symmetric functions with coefficients. Transformation of equations, Descarte's rule of signs. | | 15 h |
| II | Cardon's solution of a cubic equation, Descarte's solution of a bi-quadratic equation, Discriminant and nature of roots. | | 15 h |
| III | Divisibility, H.C.F. Primes & Unique factorization in N & Z the Diophantine equation $ax+by=c$. Residue class, complete and reduced residue system, congruences and their properties, Fermat's theorem, Euler's theorem, and Wilson's theorem. | | 15 h |
| IV | Algebraic congruences, Solution by inspection. Solution of $ax \equiv b \pmod{m}$, Chinese remainder theorem, non-linear algebraic congruency with respect to the modulus. | | 15 h |
| Sessional Internal Assessment (SIA) Full Marks . 25 Marks | | | |
| A Internal written Examination . 20 Marks (1 Hr.) | | | |
| B Over All Performance including Regularity . 05 Marks | | | |
| Books Recommended: | | | |
| 1. Theory of equation: Lalji Prasad | | | |
| 2. Theory of Equation - Burnside & Penton | | | |
| 3. Basic Number theory : S. B. Malik | | | |
| 4. Introduction to Number Theory : Niven & Zukerman | | | |




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| Program: Bachelor's Degree | | Year: Third | Semester: V |
| Class: UG | | | |
| Subject: Mathematics | | | |
| Course Code: MJ-11 | | Course Title: Complex Analysis | |
| Course Learning Outcomes: This course will enable the students to: | | | |
| a) apply the concept of continuity & differentiability of function of two variables. b) apply the concept of analytic function & form analytic function. c) understand standard transformations. d) understand the concept of conformal mapping. | | | |
| Credit: 4 (Theory) | | Compulsory | |
| Full Marks: 75 | | Time: 3 Hours | |
| Unit | Content | | Hours |
| I | Real Functions for two variables. Simultaneous and iterated limits; continuity, partial derivatives, differentiability, and related necessary and sufficient conditions. | | 15 h |
| II | Functions of a complex variables: Limit, continuity, derivative Cauchy Riemann Equations analytic function, harmonic function, construction of analytic function Miln Thompson Method. | | 15 h |
| III | Geometric Importance of some standard transformations e.g. $w = z + c$ $w = cz$ $w = 1/z$, $w = (az + b) / (cz + d)$ (bilinear). | | 15 h |
| IV | Conformal transformation as transformation effected by analytic functions special conformal transformations $w = z^2$, $w = e^z$, $w = \sin z$ | | 15 h |
| Sessional Internal Assessment (SIA) Full Marks . 25 Marks | | | |
| A Internal written Examination . 20 Marks (1 Hr.) | | | |
| B Over All Performance including Regularity . 05 Marks | | | |
| Books Recommended: | | | |
| 1. Complex Analysis by Lalji Prasad | | | |
| 2. Complex Analysis by J. N. Sharma | | | |

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| Program: Bachelor's Degree | | Year: Third | Semester: VI |
| Class: UG | | | |
| Subject: Mathematics | | | |
| Course Code: MJ-12 | | Course Title: Dynamics & Statics | |
| Course Learning Outcomes: This course will enable the students to: | | | |
| a) apply the condition for equilibrium in problems. b) solve problems related to common catenary. c) solve problems related to gravitation % Newton's laws of motion. d) solve problems related to projectile. | | | |
| Credit: 4 (Theory) | | Compulsory | |
| Full Marks: 75 | | Time: 3 Hours | |
| Unit | Content | | Hours |
| I | Conditions for equilibrium of forces in three dimensions. Wrench pitch, Null Lines. | | 15 h |
| II | Common Catenary, Stable equilibrium, energy test of stability (problems involving one variable only). | | 15 h |
| III | Motion of a particle under a central force, Differential equation of a central orbit in both polar and pedal co-ordinates. Newton's law of gravitation, planetary orbits, Kepler's laws of motion. | | 15 h |
| IV | Motion of projectile under gravity in a non-resisting medium. Motion of the mass centre and motion relative to the mass centre D'Alembert's principle. Two-dimensional motion of a rigid body rotating about a fixed axis, compound pendulum. | | 15 h |
| Sessional Internal Assessment (SIA) Full Marks - 25 Marks | | | |
| A Internal written Examination - 20 Marks (1 Hr.) | | | |
| B Over All Performance including Regularity - 05 Marks | | | |
| Books Recommended: | | | |
| 1. Dynamics Part I & II A. S. Ramsay 2. Dynamics by P.P. Gupta, Sanjay Gupta 3. Statics by Loney 4. Statics by A. R. Vasistha | | | |



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| Program: Bachelor's Degree Class: UG | | Year: Third | Semester: VI |
| Subject: Mathematics | | | |
| Course Code: MJ-13 | | Course Title: LPP & Statistics | |
| Course Learning Outcomes: This course will enable the students to: | | | |
| a) solve problems related to linear programming problems. | | | |
| b) solve problems related to transportation & assignment problems. | | | |
| c) study the nature of curve, fit a suitable curve for bivariate data. | | | |
| d) study correlation and do regression analysis. | | | |
| Credit: 4 (Theory) | | Compulsory | |
| Full Marks: 75 | | Time: 3 Hours | |
| Unit | Content | | Hours |
| I | Convex sets in R^2 and their properties, L.P.P., problem formulation, Graphical Method. Simplex method including Big M-method, Duality: Dual Simplex method. | | 15 h |
| II | Transportation and Assignment. Deterministic replacement models, sequencing problems on two machines and n jobs. | | 15 h |
| III | Measures of Skewness and Kurtosis. Curve fitting and method of least square. | | 15 h |
| IV | Correlation and regression & their expectations and variance. | | 15 h |
| Sessional Internal Assessment (SIA) Full Marks: 25 Marks | | | |
| A Internal written Examination: 20 Marks (1 Hr.) | | | |
| B Over All Performance including Regularity: 05 Marks | | | |
| Books Recommended: | | | |
| 1. Linear Programming Problem: R.K. Gupta | | | |
| 2. Linear Programming Problem: Lalji Prasad | | | |
| 3. Operations Research: S. D. Sharma | | | |
| 4. Mathematical Statistics: Kapur & Saxena | | | |

Dr. R. K. Gupta *Dr. P. K. Singh* *Dr. K. J. Singh*

| Program: Bachelor's Degree | Year: Third | Semester: VI |
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| Class: UG | | |
| Subject: Mathematics | | |
| Course Code: MJ-14 | Course Title: Analysis II & Ring | |
| Course Learning Outcomes: This course will enable the students to: | | |
| a) test the convergence of improper integral. b) solve multiple integrals using theorems like Green's theorem, Stokes theorem. c) understand the concept of ring and Ideals. d) explain the concept of field & homeomorphism. | | |
| Credit: 4 (Theory) | Compulsory | |
| Full Marks: 75 | Time: 3 Hours | |
| Unit | Content | Hours |
| I | Convergence of improper integrals, Comparison Tests, Absolute convergence, Able's and Dirichlet's Tests, Frullani's Integrals, Def. Duplication formula, inter-relation. | 15 h |
| II | Multiple Integrals via Dirichlet's Theorem Liouville's extension. Change of order of integration and change of variables. Vector Integration: Line Integral, Surface Integral, Green's theorem in R^2 , Stoke's theorem, Gauss divergence theorem. | 15 h |
| III | Rings, Preliminary Results, Special Kinds, subrings and Ideals, Quotient rings. | 15 h |
| IV | Fields and Homomorphism. Field for quotient and embedding theorem, polynomial rings, Euclidian ring & Unique factorization in it. | 15 h |
| Sessional Internal Assessment (SIA) Full Marks : 25 Marks | | |
| A Internal written Examination : 20 Marks (1 Hr.) | | |
| B Over All Performance including Regularity : 05 Marks | | |
| Books Recommended: 1. Mathematical Analysis: Shanti Narayan 2. Mathematical Analysis: Mallick Arora 3. Integral Calculus: Williamson 4. Vector Calculus: Shanti Narayan 5. Modern Algebra: A. R. Vasistha 6. Modern Algebra: Goyal & Gupta | | |


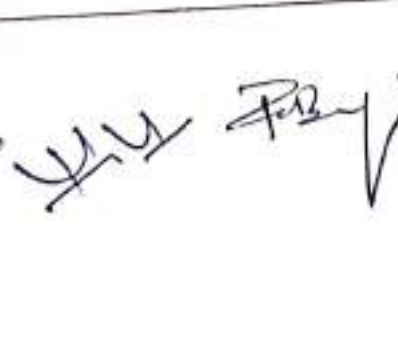
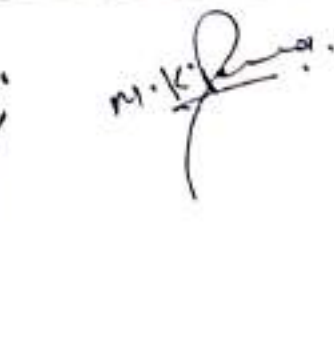


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| Program: Bachelor's Degree Class: UG | | Year: Third | Semester: VI |
| Subject: Mathematics | | | |
| Course Code: MJ-15 | | Course Title: Numerical Analysis & Programming in C | |
| Course Learning Outcomes: This course will enable the students to: a) find roots of equation and interpolate by numerical methods. b) differentiate & integrate by numerical methods. c) know about the logics and algorithms needed for computer programming. | | | |
| Credit: 4 (Theory) | | Compulsory | |
| Full Marks: 75 | | Time: 3 Hours | |
| Unit | Content | | Hours |
| I | Solution of Equations: Bisection, regula-falsi, Newton's method, Root of Polynomials. Interpolation: Lagrange and Hermite Interpolation, divided differences Schemes, Interpolation Formula using Differences. | | 15 h |
| II | Numerical Differentiation: Numerical formulas. Numerical Integration Quadrature Formula Simpsons and Trapezoidal Rule. | | 15 h |
| III | Programmer's model of a computer. Algorithms. Flow Charts. Data Types. Arithmetic and input/output instructions. Decision control structures. Decisions statements. | | 15 h |
| IV | Logical and Conditional operators. Loop. Case control structures. Functions, Recursions, Preprocessors. Arrays, Puppeting of string. Structures. Pointers. File formatting. | | 15 h |
| Sessional Internal Assessment (SIA) Full Marks : 25 Marks A Internal written Examination : 20 Marks (1 Hr.) B Over All Performance including Regularity : 05 Marks | | | |
| Books Recommended: 1. Programming in ANCI in C.E. Balaguru Swamy. 2. Numerical Analysis: J.B. Scarborough 3. Introduction to Numerical Analysis: A. Gupta & S.C. Bose | | | |





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| Program: Bachelor's Degree with Honours/Hons. with Research Class: UG | | Year: Fourth | Semester: VII |
| Subject: Mathematics | | | |
| Course Code: MJ-16 | | Course Title: Fluid Mechanics & Special Function | |
| Course Learning Outcomes: This course will enable the students to: | | | |
| a) understand the nature of fluid, its pressure and centre of pressure. b) explain the fluid motion using equation of continuity and Bernoulli's theorem. c) find series solution of differential equations about ordinary and singular points. d) understand the properties of Legendre polynomials and properties of Hypergeometric functions. | | | |
| Credit: 4 (Theory) | | Compulsory | |
| Full Marks: 75 | | Time: 3 Hours | |
| Unit | Content | | Hours |
| I | Nature and Properties of Fluid pressure, pressure of heavy liquids. Equilibrium of fluids under given system of forces. Centre of pressure. | | 15 h |
| II | Thrust on plane and curved surfaces. Lagrangian and Eulerian methods, Equation of continuity. Euler's equation of motion for perfect fluid, Bernoulli's Theorem. | | 15 h |
| III | Series solution: Ordinary point, singular point (regular), General Methods and forms of series solution (Indicial equation-frobenius method). [N.B. result of analysis regarding validity of series. Solution are to be taken for granted] Bessel's equation: Solution Recurrence formula for $J_n(x)$; generating function for $J_n(x)$, equations reducible to Bessel equation, Orthogonality of Bessel's functions. | | 15 h |
| IV | Legendre equation: Solution, Rodrigue's formula, Legendre polynomials, generating function for $P_n(x)$, Orthogonality of Legendre polynomials. Hypergeometric functions, special cases, Integral representation. Summation theorem. | | 15 h |
| Sessional Internal Assessment (SIA) Full Marks 25 Marks | | | |
| A Internal written Examination 20 Marks (1 Hr.) | | | |
| B Over All Performance including Regularity 05 Marks | | | |
| Books Recommended: | | | |
| 1. Hydrostatics: J.P. Sinha | | | |
| 2. Hydrodynamics: Ramsey / M.D. Raisingania | | | |
| 3. Advance differential equation: M. D. Raisingania | | | |

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| Program: Bachelor's Degree with Honours/Hons. with Research Class: UG | | Year: Fourth | Semester: VII |
| Subject: Mathematics | | | |
| Course Code: MJ-17 | | Course Title: Metric space & Discrete Mathematics | |
| Course Learning Outcomes: This course will enable the students to: | | | |
| a) Develop the concept of metric space and related properties. | | | |
| b) Learn the idea of completeness of a space with its properties. | | | |
| c) Learn the idea of continuous and uniform continuous functions. | | | |
| d) Learn the concept of cardinality & mathematical induction. | | | |
| e) understand the concept of graph and lattices. | | | |
| Credit: 4 (Theory) | | Compulsory | |
| Full Marks: 75 | | Time: 3 Hours | |
| Unit | Content | | Hours |
| I | Definition and example of metric spaces, Open sets, Interior closed Sets closure. | | 15 h |
| II | Convergence, completeness, Bair's theorem, Cantor's Intersection theorem. Continuous maps, Uniform Continuity, and related extensions. | | 15 h |
| III | Sets and Propositions-Cardinality, Mathematical Induction. Principle of Inclusion and exclusion. Relations and Functions – Binary Relations. Equivalence Relations and partitions. Partial. Order Relations and Lattices, chains and Antichains. Pigeon Hole Principle. | | 15 h |
| IV | Graphs and Planar Graph, basic terminology, Multigraphs, Weighted Graphs, Paths and Circuits, Shortest paths, Eulerian Paths and Circuits, Travelling Salesman Problem, Planer Graphs, Boolean Algebras – Lattices and algebraic structures, Duality, Distributive and complemented Lattices, Boolean lattices and Algebras, Boolean Functions and Expression. | | 15 h |
| Sessional Internal Assessment (SIA) Full Marks - 25 Marks | | | |
| A Internal written Examination - 20 Marks (1 Hr.) | | | |
| B Over All Performance including Regularity - 05 Marks | | | |
| Books Recommended: | | | |
| 1. Discrete Mathematics: C.L. Lieu, Elements of Discrete Mathematics: McGraw Hill International Ed. | | | |
| 2. Topology: K.K. Jha / J.N. Sharma | | | |
| 3. Mathematical Analysis: Shanti Narayan / Mallick Arora | | | |
| 4. Metric Space by Lalji Prasad | | | |



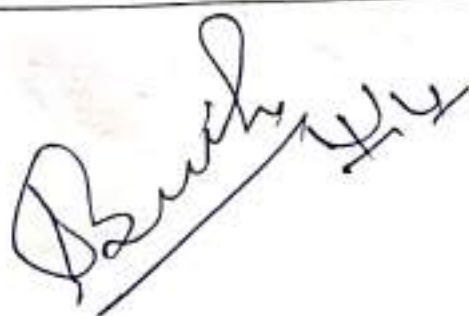


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| Program: Bachelor's Degree with Honours/Hons. with Research Class: UG | | Year: Fourth | Semester: VII |
| Subject: Mathematics | | | |
| Course Code: MJ-18 | | Course Title: Integral Transform | |
| Course Learning Outcomes: This course will enable the students to: | | | |
| a) learn concept of Laplace and inverse Laplace transform. | | | |
| b) solve the differential equation using Laplace transform. | | | |
| c) learn the concept and properties of Fourier transform. | | | |
| d) learn application of Fourier sine & cosine transform. | | | |
| Credit: 4 (Theory) | | Compulsory | |
| Full Marks: 75 | | Time: 3 Hours | |
| Unit | Content | | Hours |
| I | Laplace transform: Def, transformation of elementary functions, properties, inverse transform, transform derivatives and integrals, multiplication by t^n division by t . | | 15 h |
| II | Inverse Laplace Transform, Convolution theorem and application to differential equation. | | 15 h |
| III | Infinite Fourier Transform: Infinite Fourier sine transform, Infinite Fourier cosine transform, Relation between Fourier & Laplace transform. | | 15 h |
| IV | The Finite Fourier Transform & Integral: Finite Fourier sine transform, Finite Fourier cosine transform, Fourier Integral. | | 15 h |
| Sessional Internal Assessment (SIA) Full Marks : 25 Marks | | | |
| A Internal written Examination : 20 Marks (1 Hr.) | | | |
| B Over All Performance including Regularity : 05 Marks | | | |
| Books Recommended: | | | |
| 1. Laplace's & Fourier Transforms J.K. Goyal, K.P. Gupta, G.S. Gupta | | | |
| 2. Integral Transform & Fourier Series: A. N. Srivastava | | | |



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| Program: Bachelor's Degree with Honours/Hons. with Research Class: UG | | Year: Fourth | Semester: VII |
| Subject: Mathematics | | | |
| Course Code: MJ-19 | | Course Title: Partial Differentiation | |
| Course Learning Outcomes: This course will enable the students to: a) apply a range of techniques to solve first & second order partial differential equations. b) apply Monge's method to solve non-linear equation of second order. c) model physical phenomena using partial differential equations such as the heat and wave equations. | | | |
| Credit: 4 (Theory) | | Compulsory | |
| Full Marks: 75 | | Time: 3 Hours | |
| Unit | Content | | Hours |
| I | Partial differential equation, formation, linear p.d.e. of order 1-Lagrange's method. | | 15 h |
| II | Non-linear equation of order 1, four forms Charpits method, Jacobi Method. Homogeneous linear equation with constant co-efficient Rules of C.F. and P.I. | | 15 h |
| III | Non-linear equations of second order, Monge's method. | | 15 h |
| IV | Boundary Value Problem: Derivation and solution of one-dimensional wave equation and one-dimensional heat equation. | | 15 h |
| Sessional Internal Assessment (SIA) Full Marks - 25 Marks A Internal written Examination - 20 Marks (1 Hr.) B Over All Performance including Regularity - 05 Marks | | | |
| Books Recommended: 1. Advanced Differential Equation: M.D. Raisingania 2. Differential equation: J.N. Sharma | | | |



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| Program: Bachelor's Degree with Honours/Hons. with Research Class: UG | | Year: Fourth | Semester: VIII |
| Subject: Mathematics | | | |
| Course Code: MJ-20 | | Course Title: Linear Algebra & Linear Difference equation | |
| Course Learning Outcomes: This course will enable the students to: a) understand concept of basis of vector spaces and construct orthonormal basis. b) understand the concept of rank & nullity. c) construct difference equations and find its general solutions. d) find solution of linear difference equations and homogeneous difference equations. | | | |
| Credit: 4 (Theory) | | Compulsory | |
| Full Marks: 75 | | Time: 3 Hours | |
| Unit | Content | Hours | |
| I | Vector Space: Def. & properties, subspaces, linear dependence, dimension and basis of a finite dimensional vector space, Quotient space, Direct sums and complements matrices and change of basis. Inner product & norm in a I. S., properties of inner product, Schwartz inequality, orthogonal set, orthogonal basis and Gram-schmidt construction for finite dimensional inner product space. | 15 h | |
| II | Linear transformation: Def, Sylvester Law of nullity, algebra of linear transformations, Dual spaces, principal of duality. Matrices and linear transformation, similar matrices, even matrices, diagonalisation Eigen root (Algebraic geometric and multiplicity). | 15 h | |
| III | Difference Equation Order, Solution of Difference Equation, Existence & Uniqueness theorem, solution of the form. $y_{n+1} = Ay_n + C$ | 15 h | |
| IV | Linear Difference Equation with constant coefficient: Basic Definition. Combination of solution, Fundamental set of solution, Homogeneous Difference Equation & their solution (General & Particular), Special operator, variation of parameters. | 15 h | |
| Sessional Internal Assessment (SIA) Full Marks : 25 Marks A Internal written Examination : 20 Marks (1 Hr.) B Over All Performance including Regularity : 05 Marks | | | |
| Books Recommended: 1. Modern Algebra: Surjeet Singh & Quazi Zameeruddin 2. Linear Difference Equation: R.K. Gupta & D.C. Agarwal. | | | |

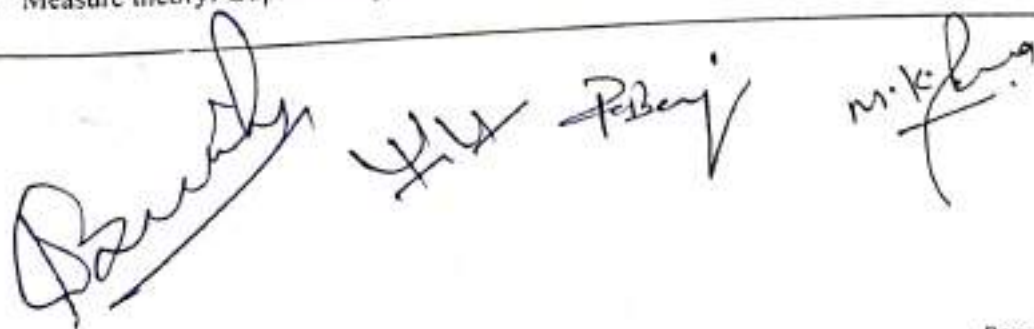
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| Program: Bachelor's Degree with Honours/Hons. with Research Class: UG | | Year: Fourth | Semester: VIII |
| Subject: Mathematics | | | |
| Course Code: AMJ-1 | | Course Title: Topology | |
| Course Learning Outcomes: This course will enable the students to: a) learn about the concept of compactness in metric space. b) define topological space its bases and different types spaces. c) learn different types of compactness in topological spaces. d) learn different types separation axioms in topological spaces and also the connectedness of topological spaces | | | |
| Credit: 4 (Theory) | | Compulsory | |
| Full Marks: 75 | | Time: 3 Hours | |
| Unit | Content | | Hours |
| I | Compactness in metric space, Ascoli's theorem. Topological spaces: | | 15 h |
| II | Definition, examples, base, sub-base, first axiom space, second axiom space, comparison of topologies. | | 15 h |
| III | Compactness: Compact space, Lindeloff space, product space, Tychonoff's theorem, locally compactness. | | 15 h |
| IV | Separation: T_1 - space, T_2 - space, normal & completely regular space, Uryshon's lemma, Tietze extension theorem, Uryshon's metrization theorem. Connectedness: connectedness & its properties. | | 15 h |
| Sessional Internal Assessment (SIA) Full Marks . 25 Marks A Internal written Examination : 20 Marks (1 Hr.) B Over All Performance including Regularity . 05 Marks | | | |
| Books Recommended: 1. Real Analysis: H. L. Royden, P. M. Fitzpatrick 2. Topology: J. N. Sharma, J. P. Chauhan 3. Advanced General Topology: K. K. Jha | | | |



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| Program: Bachelor's Degree with Honours/Hons. with Research Class: UG | | Year: Fourth | Semester: VIII |
| Subject: Mathematics | | | |
| Course Code: AMJ-2 | | Course Title: Complex Analysis II | |
| Course Learning Outcomes: This course will enable the students to: | | | |
| a) apply complex integration in solving problems. | | | |
| b) learn about power series expansion and their convergence. | | | |
| c) apply method of contour integration. | | | |
| d) learn about conformal mapping. | | | |
| Credit: 4 (Theory) | | Compulsory | |
| Full Marks: 75 | | Time: 3 Hours | |
| Unit | Content | | Hours |
| I | Integral: Cauchy's integral theorem, Cauchy's integral formula, Morera's theorem, Liouville's theorem, Taylor's theorem, Laurent's theorem, Rouché's theorem, fundamental theorem of algebra. | | 15 h |
| II | Power series: formula for radius of convergence of power series, absolute & uniform convergence theorem of power series, uniqueness theorem of power series, term by term integration and differentiation theorem. | | 15 h |
| III | Residue & poles, contour integration and problems | | 15 h |
| IV | Conformal mapping: Conformal and bilinear mapping, necessary & sufficient condition for conformal mapping, mapping from half plane to circle, mapping from unit circle to unit circle and related problems. | | 15 h |
| Sessional Internal Assessment (SIA) Full Marks 25 Marks | | | |
| A. Internal written Examination . 20 Marks (1 Hr.) | | | |
| B. Over All Performance including Regularity . 05 Marks | | | |
| Books Recommended: | | | |
| 1. Complex Variable: Churchill | | | |
| 2. Theory of Functions: Titch Marsh | | | |
| 3. Complex Analysis: J. B. Conway | | | |
| 4. Function of a Complex Variable: Goyal & Gupta | | | |

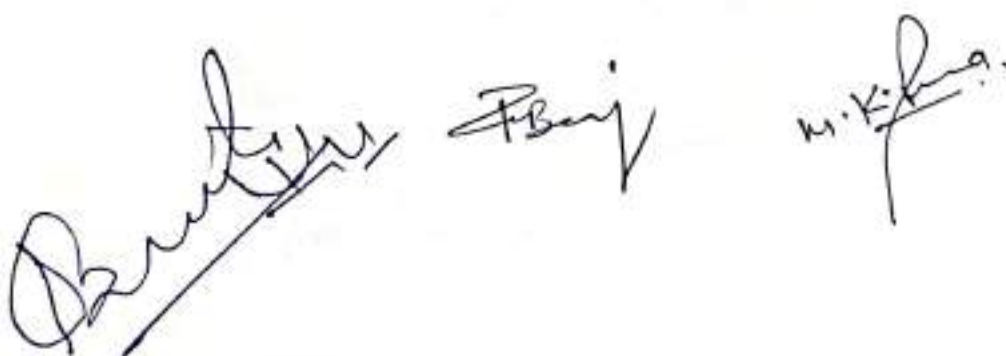


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| Program: Bachelor's Degree with Honours/Hons. with Research Class: UG | | Year: Fourth | Semester: VIII |
| Subject: Mathematics | | | |
| Course Code: AMJ-3 | | Course Title: Real Analysis & Measure Theory | |
| Course Learning Outcomes: This course will enable the students to: | | | |
| a) learn the concept of uniform convergence in sequence & series of functions. b) learn about Fourier series and its applications. c) learn the concept of measure theory and its properties. d) know about the measurable functions & its properties. | | | |
| Credit: 4 (Theory) | | Compulsory | |
| Full Marks: 75 | | Time: 3 Hours | |
| Unit | Content | | Hours |
| I | Sequence and series of function: Uniform convergence of sequence and series of real function. Cauchy's general principle of uniform convergence, continuity of the sum of a series of function. Weierstrass's M-test for uniform convergence. Term by term integration and differentiation. | | 15 h |
| II | Fourier series: Fourier series expansion of a function relative to an orthonormal system. Bessel's inequality, pointwise convergence of trigonometric Fourier series, Dirichlet's integral, Parseval's theorem, Riemann-Lebesgue theorem, Problems on finding trigonometric Fourier series representation of periodic functions. | | 15 h |
| III | Measure theory: Outer measure, measurable sets through Caratheodory approach, arithmetical properties of measurable sets, two fundamental theorems and examples of uncountable sets of zero measure. | | 15 h |
| IV | Measurable Functions: Closure of class of measurable function under all algebraic and limit operations, Littlewood's third principle trigonometric Fourier series representation of periodic functions. Function bounded over a set of finite measure, condition of measurability, Lebesgue integral and its arithmetical properties, comparison with R-integral, bounded convergence theorem. | | 15 h |
| Sessional Internal Assessment (SIA) Full Marks 25 Marks A. Internal written Examination 20 Marks (1 Hr.) B. Over All Performance including Regularity 05 Marks | | | |
| Books Recommended: 1. Principle of Mathematical Analysis: Walter Rudin 2. Mathematical Analysis: Shanti Narayan 3. Real Analysis: H. L. Royden 4. Advanced Real Analysis: K. K. Jha 5. Measure theory: Gupta & Gupta | | | |

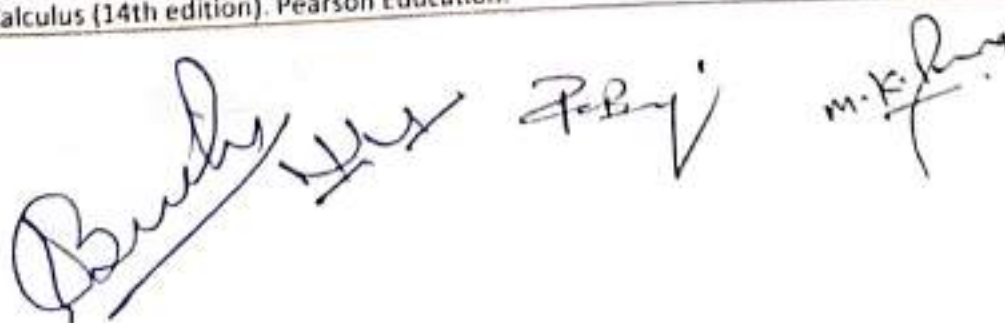


Minor Syllabus

| Semester | Paper | Code | Course Title | Credit |
|----------|----------|-------|-------------------------|--------|
| I | Minor-1A | MN-1A | Calculus | 4 |
| II | Minor-2A | MN-2A | Discrete Mathematics | 4 |
| III | Minor-1B | MN-1B | Real Analysis | 4 |
| IV | Minor-2B | MN-2B | Discrete Mathematics-II | 4 |
| V | Minor-1C | MN-1C | Vectors | 4 |
| VI | Minor-2C | MN-2C | Probability Theory | 4 |
| VII | Minor-1D | MN-1D | Real Analysis-II | 4 |
| VIII | Minor-2D | MN-2D | Operations Research | 4 |



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| Program: Certificate Class: UG | Year: First | Semester: I |
| Subject: Mathematics | | |
| Course Code: MN-1A | Course Title: Calculus | |
| Course Learning Outcomes: This course will enable the students to: <ol style="list-style-type: none"> Understand the concept of functions, limits, and continuity, and apply them to solve mathematical problems. Use differentiation rules, including the chain rule and mean value theorem, to differentiate real-valued functions and apply successive differentiation and Leibnitz's theorem to solve calculus problems. Develop skills in finding antiderivatives, computing definite integrals using Riemann sums and the fundamental theorem of calculus, and using various integration techniques to solve real-world problems. Gain proficiency in integrating various types of functions, analyzing curves, and calculating area and volume of surfaces of revolution using integration techniques. | | |
| Credit: 4 (Theory) | Compulsory | |
| Full Marks: 75 | Time: 3 Hours | |
| Unit | Content | Hours |
| I | Functions and Limits: Definition of functions and their properties, Limits of functions and their properties, Continuity of functions. | 12 h |
| II | Differential calculus: Differentiability of a real valued function, Geometrical interpretation of differentiability, Rules of differentiation, Chain rule of differentiation, Mean value theorem and its applications, Successive differentiation, Leibnitz's theorem. | 18 h |
| III | Integration: Antiderivatives, Indefinite and definite integrals, Riemann sums and the definite integral, Fundamental theorem of calculus, Properties of definite integrals, Integration Techniques. | 12 h |
| IV | Integral Calculus: Integration of rational and irrational functions, Reduction formula, Computing of definite integral, Curve tracing, Length of curve, Computing of double and triple integrals, Area and Volume of surface of revolution. | 18 h |
| Sessional Internal Assessment (SIA) Full Marks – 25 Marks A – Internal written Examination – 20 Marks (1 Hr) B – Over All Performance including Regularity – 05 Marks | | |
| Books Recommended: <ol style="list-style-type: none"> 1. R. K. Dwivedi (2019). Calculus, 1st Edition, Pragati Prakashan, Meerut, India. 2. Howard Anton, I. Bivens & Stephan Davis (2016). Calculus (10th edition). Wiley India. 3. Gabriel Klambauer (1986). Aspects of Calculus. Springer-Verlag. 4. Wieslaw Krawcewicz & Bindhyachal Rai (2003). Calculus with Maple Labs. Narosa. 5. Gorakh Prasad (2016). Differential Calculus (19th edition). Pothishala Pvt. Ltd. 6. George B. Thomas Jr., Joel Hass, Christopher Heil & Maurice D. Weir (2018). Thomas' Calculus (14th edition). Pearson Education. | | |

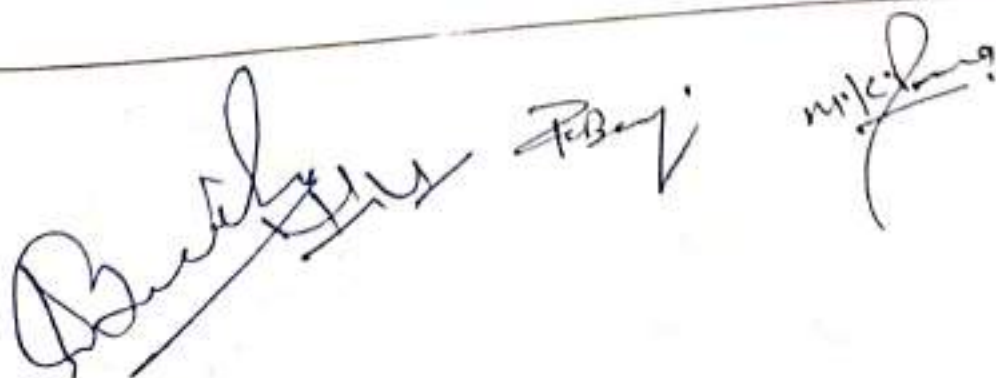


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| Program: Certificate | Year: First | Semester: II |
| Class: UG | | |
| Subject: Mathematics | | |
| Course Code: MN-2A | Course Title: Discrete Mathematics | |
| Course Learning Outcomes: This course will enable the students to: a) Understand the concept equivalence relation & partial order relation. b) Understand the concept of bounds in POSET and able to understand the concept of Lattice. c) Understand mathematical logic and logical operations to various fields. | | |
| Credit: 4 (Theory) | Compulsory | |
| Full Marks: 75 | Time: 3 Hours | |
| Unit | Content | Hours |
| I | Relation: Reflexive, Symmetric, Antisymmetric & transitive relation, Partition, Equivalence relation, Congruence Modulo Relation, Induced relation, Fundamental theorem. | 15 h |
| II | Partial Order Relation: Partial Order Set, <i>l.u.b.</i> & <i>g.l.b.</i> , <i>inf.</i> , <i>sup.</i> , maximal & minimal element. Definition & examples of Lattice, Zorn's lemma | 15 h |
| III | Logic: Introduction, propositions, truth table, negation, conjunction and disjunction. Implications, biconditional propositions, converse, contra positive and inverse propositions, and precedence of logical operators. | 15 h |
| IV | Propositional equivalence: Logical equivalences, Predicates and quantifiers: Introduction, Quantifiers, Binding variables and Negations. Validity of argument by different methods. | 15 h |
| Sessional Internal Assessment (SIA) Full Marks 25 Marks A. Internal written Examination - 20 Marks (1 Hr) B. Over All Performance including Regularity - 05 Marks | | |
| Books Recommended: 1. Set theory by K. K. Jha, 2. R. P. Grimaldi, Discrete Mathematics and Combinatorial Mathematics, Pearson Education, 3. Discrete Mathematics by M. K. Gupta; Krishna Prakashan. 4. Discrete Mathematics by Lipschutz, Lipson & Patil; Schaum's Outlines | | |






| Program: Diploma | Year: Second | Semester: III |
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| Class: UG | | |
| Subject: Mathematics | | |
| Course Code: MN-IB | Course Title: Real Analysis | |
| Course Learning Outcomes: This course will enable the students to: <ol style="list-style-type: none"> Understand many properties of the real line \mathbb{R} and learn to define sequence in terms of functions from \mathbb{R} to a subset of \mathbb{R}. Recognize bounded, convergent, divergent, Cauchy and monotonic sequences and to calculate their limit superior, limit inferior, and the limit of a bounded sequence. Apply the ratio, root, alternating series and limit comparison tests for convergence and absolute convergence of an infinite series of real numbers. Learn some of the properties of Riemann integrable functions, and the applications of the fundamental theorems of integration. | | |
| Credit: 4 (Theory) | Compulsory | |
| Full Marks: 75 | Time: 3 Hours | |
| Unit | Content | Hours |
| I | Real Number System Axioms in \mathbb{R} , Absolute value of a real number, Bounds of a sets, Supremum and infimum of a nonempty subset of \mathbb{R} , The completeness property of \mathbb{R} , Archimedean property, Definition and types of intervals, Neighborhood of a point in \mathbb{R} , Open, closed and perfect sets in \mathbb{R} | 15 h |
| II | Sequences of Real Numbers: Convergent sequence, Limit of a sequence, Bounded sequence, Limit theorems, Monotone sequences, Weierstrass' theorem for-sequences, Monotone convergence theorem, Subsequences, Bolzano sequences, Limit superior and limit inferior of a sequence of real numbers, Cauchy sequence, Cauchy's first theorem on limit, Cauchy's convergence criterion. Completeness property of set of real number. | 15 h |
| III | Infinite Series Convergence and divergence of infinite series of positive real numbers, Necessary condition for convergence, Cauchy criterion for convergence, Tests for convergence of positive term series; Basic comparison test, Limit comparison test, D'Alembert's ratio test, Raabe's test, Logarithmic test, Cauchy's condensation Test, De Morgan & Bertrand's test. | 20 h |
| IV | Alternating series: Alternating series, Leibniz test, Absolute and conditional convergence. Properties of absolutely convergent series. | 10 h |
| Sessional Internal Assessment (SIA) Full Marks 25 Marks A Internal written Examination 20 Marks (1 Hr) B Over All Performance including Regularity 05 Marks | | |
| Books Recommended: <ol style="list-style-type: none"> Real Analysis: Dasgupta & Prasad Real Analysis: Lalji Prasad Real Analysis: K. K. Jha Principle of Real Analysis: S. C. Malik | | |

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|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------|--------------|
| Program: Diploma | | Year: Second | Semester: IV |
| Class: UG | | | |
| Subject: Mathematics | | | |
| Course Code: MN-2B | | Course Title: Discrete Mathematics-II | |
| Course Learning Outcomes: This course will enable the students to: <ul style="list-style-type: none"> a) Understand and explain the basic concepts of graph theory. b) Apply the basic concepts of mathematical logic. c) Analyze the basic concepts of mathematical logic. d) Evaluate some real time problems using concepts of graph theory. | | | |
| Credit: 4 (Theory) | | Compulsory | |
| Full Marks: 75 | | Time: 3 Hours | |
| Unit | Content | | Hours |
| I | Logic: Boolean algebra, Boolean expression, application to switching circuits. | | 15 |
| II | Graph Theory: Basic Terminology, Walks, paths, circuits, connectedness, Handshaking Lemma, Isomorphism, Sub graphs, Reach ability, Union and Intersection of Graphs. Euler Graph, Shortest path problem, Hamiltonian graph, Traveling Salesman Problem, Bipartite graphs. | | 15 |
| III | Trees: Introduction to trees, Rooted trees, path length in rooted trees, spanning trees, Fundamental circuits, spanning trees of a weighted graph, cut sets and cut vertices, Fundamental cut set, Minimum spanning tree. | | 15 |
| IV | Directed Graph: Directed graphs and connectedness, directed trees, Matrix representation of a graph, Planar graphs, Combinational and Geometric Duals, Kuratowski's graphs, Detection of planarity, 5 colour problem. | | 15 |
| Sessional Internal Assessment (SIA) Full Marks: 25 Marks A Internal written Examination: 20 Marks (1 Hr) B Over All Performance including Regularity: 05 Marks | | | |
| Books Recommended: <ol style="list-style-type: none"> 1. C.L. Liu, Elements of Discrete Mathematics, Tata McGraw Hill, 2nd Edition, 2000. 2. N. Deo, Graph Theory with Applications to Engineering and Computer Science, PHI publication, 3rd edition, 2009 3. Harikishan, Shivraj Pundir and Sandeep Kumar, Discrete Mathematics, Pragati Publication, 7th Edition, 2010. 4. Colmun, Busby and Ross, Discrete Mathematical Structure, PHI Publication, 6th Edition, 2009 | | | |



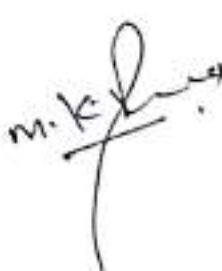


| Program: Bachelor's Degree | Year: Third | Semester: V |
|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------|
| Class: UG | | |
| Subject: Mathematics | | |
| Course Code: MN-1C | Course Title: Vectors | |
| Course Learning Outcomes: This course will enable the students to: <ul style="list-style-type: none"> a) Understand the concepts of scalar & vector products of three and four vectors. b) Understand the concept of vector function of scalar variable t, Scalar point functions, vector point functions, Grad, Curl and Divergence. c) Inter-relationship amongst the line integral, double and triple integral formulations d) Realize importance of Green, Gauss and Stokes' theorems in other branches of mathematics. | | |
| Credit: 4 (Theory) | Compulsory | |
| Full Marks: 75 | Time: 3 Hours | |
| Unit | Content | Hours |
| I | Product of three & four vectors: Product of 3 & 4 vectors, Reciprocal system of vectors, Lami's theorem, $\lambda - \mu$ theorem, work done, Moment of force, Couple. | 15 h |
| II | Vector Differentiation: Vector function of scalar variable t , it's derivative and geometrical meaning, Derivative of product of two and three vectors | 15 h |
| III | Grad, Divergence & Curl: Scalar point function and vector point function, grad, divergence and curl, their expansion formulae and properties. | 15 h |
| IV | Green's, Stoke's & Gauss's Divergence theorem: Line integrals, Applications of line integrals: Mass and Work, Fundamental theorem for line integrals, Conservative vector fields, Green's theorem, Area as a line integral, Surface integrals, Stokes' theorem, The Gauss divergence theorem. | 15 h |
| Sessional Internal Assessment (SIA) Full Marks . 25 Marks A Internal written Examination . 20 Marks (1 Hr) B Over All Performance including Regularity . 05 Marks | | |
| Books Recommended: <ol style="list-style-type: none"> Advanced Engineering Mathematics (10th edition). Erwin Kreyszig, Wiley Vector Analysis: Lalji Prasad, Paramount | | |

| Program: Bachelor's Degree | Year: Third | Semester: VI |
|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------|
| Class: UG | | |
| Subject: Mathematics | | |
| Course Code: MN-2C | Course Title: Probability Theory | |
| Course Learning Outcomes: This course will enable the students to: <ul style="list-style-type: none"> a) Use basic counting techniques (multiplication rule, combinations, permutations) to compute probability and odds. b) Compute conditional probabilities directly and using Bayes' theorem, and check for independence of events. c) Set up and work with discrete random variables. In particular, understand the Bernoulli, binomial, geometric and Poisson distributions. d) Work with continuous random variables. In particular, know the properties of uniform, normal and exponential distributions. | | |
| Credit: 4 (Theory) | Compulsory | |
| Full Marks: 75 | Time: 3 Hours | |
| Unit | Content | Hours |
| I | Random experiment, Sample Space, Algebra of events, Probability of an event, mutually exclusive events, addition theorem, Conditional probability, independent events, multiplication theorem, Total probability, Baye's theorem. | 15 |
| II | Random Variables and Distribution Functions. Introduction, Distribution Functions of Discrete Variables, Distribution Functions of Continuous Variables, Mathematical Expectations, | 15 |
| III | Binomial Distribution, Poisson's Distribution, Hypergeometric distribution, Normal & Negative binomial distribution, | 15 |
| IV | Frequency distribution, graphical and diagrammatic representation of data. Measures of location and dispersion, moments, skewness and kurtosis. Curve fitting, association of attributes. Simple correlation and regression. | 15 |
| Sessional Internal Assessment (SIA) Full Marks 25 Marks A Internal written Examination . 20 Marks (1 Hr) B Over All Performance including Regularity .05 Marks | | |
| Books Recommended: 1. Fundamental of Mathematical Statistics: Gupta & Kapoor 2. Probability and Statistics for Engineering and the Sciences: Jay L. Devore, | | |

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|----------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------|---------------|
| Program: Bachelor's Degree with Honours/Hons. with Research Class: UG | | Year: Fourth | Semester: VII |
| Subject: Mathematics | | | |
| Course Code: MN-1D | | Course Title: Real Analysis-II | |
| Course Learning Outcomes: This course will enable the students to: | | | |
| a) Understand the concept of limit & continuity of a function. | | | |
| b) Understand the concept of differentiation and expansion of function with remainder. | | | |
| c) Understand the definition and condition for Riemann Integrability. | | | |
| d) Understand the generalized set operations and relation on sets. | | | |
| Credit: 4 (Theory) | | Compulsory | |
| Full Marks: 75 | | Time: 3 Hours | |
| Unit | Content | | Hours |
| I | Limit and Continuity: Limit, Continuity, Discontinuities, uniform continuity, properties of functions continuous in closed intervals, Functions of bounded variation. | | 20 h |
| II | Derivability, Relationship with continuity, Taylor's theorem, Maclaurin's theorem, remainder after n terms, Power series expansion of $(1+x)^n$, $\sin x$, $\cos x$ and $\log(1+x)$ using suitable remainder after n terms. | | 20 h |
| III | Riemann Integration Definition, Darboux's theorem I & II. Integrability condition, particular classes of bounded integrable function primitive, fundamental theorem, first and second Mean value theorem. | | 20 h |
| Sessional Internal Assessment (SIA) Full Marks : 25 Marks | | | |
| A. Internal written Examination : 20 Marks (1 Hr) | | | |
| B. Over All Performance including Regularity : 05 Marks | | | |
| Books Recommended: | | | |
| 1. Real Analysis by Lalji Prasad | | | |
| 2. Real Analysis by K. K. Jha | | | |
| 3. Principle of Real Analysis: S. C. Malik | | | |

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|-----------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------|-----------------------------------|----------------|
| Program: Bachelor's Degree with Honours/Hons. with Research Class: UG | | Year: Fourth | Semester: VIII |
| Subject: Mathematics | | | |
| Course Code: MN-2D | | Course Title: Operations Research | |
| Course Learning Outcomes: This course will enable the students to: | | | |
| a) solve problems related to linear programming problems. | | | |
| b) solve problems related to transportation & assignment problems. | | | |
| c) Solve real life problems using replacement model and sequencing. | | | |
| Credit: 4 (Theory) | | Compulsory | |
| Full Marks: 75 | | Time: 3 Hours | |
| Unit | Content | | Hours |
| I | Convex sets in R^2 and their properties, L.P.P., problem formulation, Graphical Method. Simplex method including Big M-method, | | 15 |
| II | Duality: Definition of the dual problem, Primal-dual relationships, Dual simplex Method. | | 15 |
| III | Transportation and Assignment problems | | 15 |
| IV | Deterministic replacement models, sequencing problems on two machines and n jobs. | | 15 |
| Sessional Internal Assessment (SIA) Full Marks : 25 Marks | | | |
| A Internal written Examination : 20 Marks (1 Hr) | | | |
| B Over All Performance including Regularity : 05 Marks | | | |
| Books Recommended: | | | |
| 1. Linear Programming Problem: R.K. Gupta | | | |
| 2. Linear Programming Problem: Lalji Prasad | | | |
| 3. Operations Research: Kanti Swaroop | | | |
| 4. Operations Research: S. D. Sharma | | | |

Dr. Bijay Kumar Sinha

Dr. Md. Moiz Ashraf

Dr. P. C. Banerjee

Mr. Mahendra Kumar Rana

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|-------|------|-----------------------------------------------------------|---------|
| Sem | Code | Papers | Credits |
| V | IAP | Internship/Apprenticeship/Field Work/Dissertation/Project | 04 |



Semester-V

PAPER Title: Internship/Apprenticeship/Field Work/Dissertation/Project
Credits - 04

Learning objective:

- **Foundation in Research Methodologies:** Develop a strong foundation in Mathematical research methodologies, including problem identification, literature review, and the use of mathematical tools and techniques.
- **Data Analysis and Communication:** Demonstrate the ability to analyse data, write research reports, and present findings while adhering to ethical standards and Intellectual Property Rights (IPR)

Course Outcomes:

After completing this course, students will be able to:

- **Design and Structure Research:** Conceptualize and plan a coherent mathematical research project or dissertation, including formulating a robust research problem and executing a thorough literature review.
- **Analytical Tools:** Employ computational, statistical, and numerical techniques using tools like MATLAB, Mathematica, or Python for effective problem-solving and data analysis in mathematics.
- **Communicate Research Effectively:** Produce well-organized research reports and presentations that adhere to academic standards and ethical guidelines, ensuring clear communication of Mathematical concepts and findings.

Guidelines for Project/Dissertation Work Evaluation

The broad guidelines for the distribution of marks are as follows:

1. **Assessment of Project – 75 marks**
2. **Viva-Voce – 25 marks**

Components of the Paper

The paper will consist of the following components:

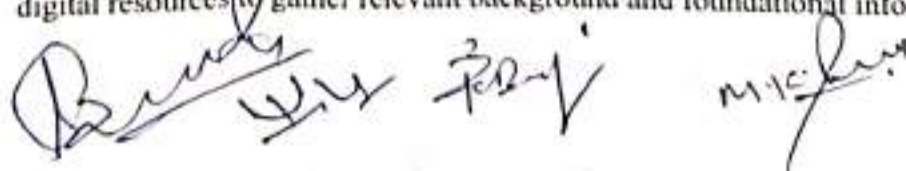
1. Foundations of Research in Mathematics.

a) Introduction to Research in Mathematics:

- **Nature and Scope:** Explore the nature and scope of mathematical research, understanding its role in both pure and applied contexts.
- **Relevance:** Discuss the importance of research in advancing mathematical theories and solving real-world problems.

b) Research Problem and Literature Review:

- **Problem Identification:** Learn techniques for identifying and formulating meaningful mathematical research problems.
- **Characteristics of a Good Problem:** Understand what makes a mathematical problem suitable for research.
- **Conducting a Literature Review:** Review various academic journals, books, and digital resources to gather relevant background and foundational information.



c) Research Design and Methodology:

- **Approaches to Mathematical Research:** Examine theoretical, computational, and experimental approaches to research.
- **Developing Models and Proofs:** Gain skills in creating mathematical models and constructing rigorous proofs as part of the research process.

2. Tools, Analysis, and Presentation.

a) Data Collection and Analysis:

- **Applied Research Data:** Learn methods for collecting data relevant to applied mathematics research.
- **Statistical and Analytical Tools:** Understand and apply statistical techniques and software tools for analyzing mathematical data.

b) Mathematical Tools and Techniques:

- **Software Proficiency:** Develop skills using softwares such as MATLAB, Mathematica, or Python for computational tasks.
- **Numerical Methods and Simulations:** Explore numerical techniques and simulation methods to support research findings.

c) Writing, Presenting, and Ethics in Research:

- **Effective Communication:** Know the art of writing clear, concise, and well-structured research papers and reports.
- **Oral Presentation:** Learn how to prepare presentations and academic posters for dissemination of research findings.
- **Ethical Considerations and IPR:** Discuss ethical scenarios in mathematical research, including plagiarism, authorship, and compliance with Intellectual Property Rights.

References:

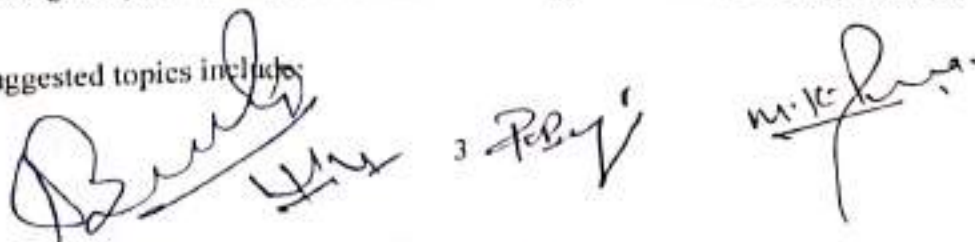
- [1] Pandey, P., & Pandey, M. M. (2015). *Research methodology: Tools and techniques*. Bridge Center.
- [2] Kelly, A.E., & Lesh, R.A. (Eds.). (2000). *Handbook of Research Design in Mathematics and Science Education (1st ed.)*. Routledge. <https://doi.org/10.4324/9781410602725>.
- [3] Mishra, Dr. Shanti Bhushan & Alok, Dr. Shashi. (2017). **HANDBOOK OF RESEARCH METHODOLOGY**. Educareation Publishing

Note: Students must consult with a faculty member in the Department to finalize their project/ dissertation topics.

Suggested Project Topics

Students may undertake projects in various Mathematical science related fields or Mathematical problems, focusing on pure and applied Mathematical application and socially relevant applications.

Some of the suggested topics includes



I. Pure Mathematics

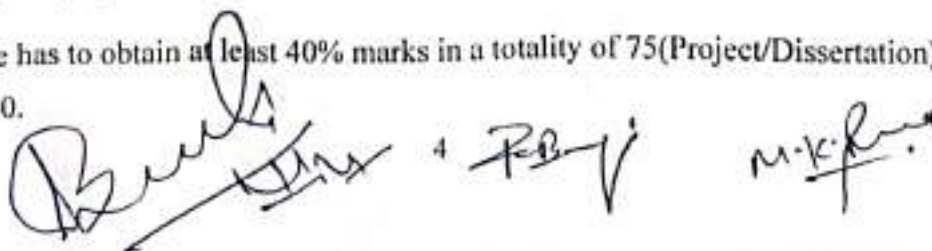
1. **Exploring the Riemann Hypothesis:** Understanding its significance and implications in number theory.
2. **The Mathematics of Fractals:** Investigating their geometry and applications.
3. **Non-Euclidean Geometry:** Applications and its role in modern mathematics.
4. **Prime Numbers in Cryptography:** How prime numbers secure digital communication.
5. **Group Theory in Abstract Algebra:** Exploring its applications in solving equations.
6. **Applications of Group Theory in Cryptography:** Study algebraic structures like groups and rings in the context of securing digital communications.
7. **Symmetries and Group Actions:** Investigate the role of group theory in solving geometric and algebraic problems
8. **Linear Algebra:** Use of eigenvalues and eigenvectors in stability analysis of systems.
9. **Linear Algebra:** Real-life applications of linear transformations in computer graphics.
10. **Linear Algebra:** Principal Component Analysis (PCA) for dimensionality reduction in data science.
11. **Complex Analysis:** Exploring the residue theorem and its applications in evaluating real integrals.
12. **Complex Analysis:** Conformal mappings and their applications in solving fluid flow problems.
13. **Complex Analysis:** Analytic continuation and its use in complex function theory.

II. Applied Mathematics

1. **Mathematical Modeling of Climate Change:** Explore how differential equations can model carbon emissions and their effects on global temperature.
2. **Modeling Traffic Flow Using Differential Equations:** Investigate optimal flow patterns in urban areas.
3. **Mathematical Analysis of Disease Spread:** Use systems of differential equations to model the dynamics of infectious diseases, incorporating vaccination and quarantine strategies
4. **Mathematical Modeling of Epidemics:** Using differential equations to study disease spread.
5. **The Role of Linear Algebra in Machine Learning:** Understanding 3D transformations and algorithms.
6. **Optimization Techniques in Operations Research:** Applications in logistics and supply chain management.
7. **The Mathematics Behind Blockchain Technology:** Exploring cryptographic algorithms.
8. **Population Dynamics in Ecology:** Modeling predator-prey systems with mathematical equations.
9. **Wave Equations in Engineering:** Applications in modeling sound, vibrations, and electromagnetic waves.
10. **Mathematical Analysis of Disease Spread:** Use differential equations to understand and predict epidemic dynamics.
11. **Optimization Problems in Mathematical Models:** Use algebraic techniques and differential equations for resource allocation or logistics.

Submission Guidelines

- Each student must submit their dissertation to the Head of the Department (HOD) after completing the project work.
- A candidate has to obtain at least 40% marks in a totality of 75(Project/Dissertation) + 25(Viva-Voce) = 100.



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|-------|------|-------------------------------------------------|---------|
| Sem | Code | Papers | Credits |
| VIII | RC | Research Internship / Field Work / Dissertation | 12 |

[Signature] February

M. K. Singh

Semester-VIII
PAPER Title: Research Course (RC)
Credits: 12 (FM - 300)

Learning objective:

- Understand the philosophy of research, including epistemology, positivism, interpretivism, and doxology.
- Apply research methodology concepts, formulate research problems, and recognize challenges in research.
- Develop expertise in research design, including experimental, longitudinal, and action research methods.
- Master data collection & presentation techniques using structured methods, statistical tools, and visualization.
- Uphold ethical standards, intellectual honesty, and plagiarism prevention in academic research.
- Develop a strong foundation in Mathematical research methodologies, including problem identification, literature review, and the use of mathematical tools and techniques.
- Demonstrate the ability to analyse data, write research reports, and present findings while adhering to ethical standards and Intellectual Property Rights (IPR)

Course Outcomes:

After completing this course, students will be able to:

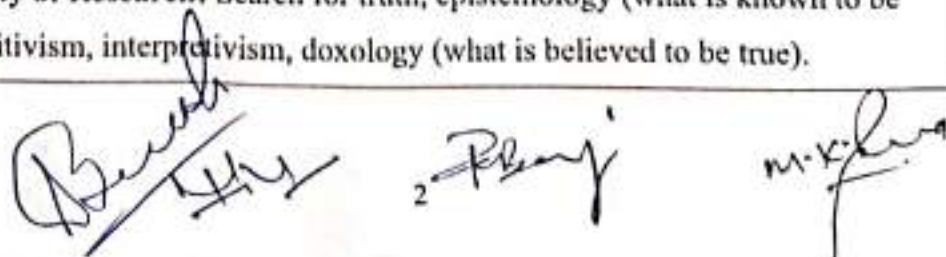
- Gain theoretical and philosophical foundations for scientific inquiry in mathematics research.
- Demonstrate proficiency in research design & methodology using mathematical and statistical tools.
- Collect, analyze, and present research data effectively with software tools like SPSS, R, and Excel.
- Implement hypothesis formulation & testing using statistical techniques for rigorous analysis.
- Maintain academic integrity, ethical research practices, and responsible reporting following IPR guidelines.
- Conceptualize and plan a coherent mathematical research project or dissertation, including formulating a robust research problem and executing a thorough literature review.
- Employ computational, statistical, and numerical techniques using tools like MATLAB, Mathematica, or Python for effective problem-solving and data analysis in mathematics.
- Produce well-organized research reports and presentations that adhere to academic standards and ethical guidelines, ensuring clear communication of Mathematical concepts and findings.

(A) Research Methodology (FM-100 Marks)

Credits: 03+01 (Th +Internal)

1. End Semester University Examination (75)
2. Semester Internal Examination (25)

| Unit | Content | Hours |
|------|---------------------------------------------------------------------------------------------------------------------------------------------------------------|-------|
| 1. | Philosophy of Research: Search for truth, epistemology (what is known to be true), positivism, interpretivism, doxology (what is believed to be true). | 6h |



| | | |
|----|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----|
| 2. | Research Methodology: Introduction, meaning and objective of research, types of research, motivations in research, research methods. Criteria of good research, problems encountered by researcher in India. Selection and formulation of a research problem. | 10h |
| 3. | Research Design: Meaning of research design, need of research design features of good design. Different types of study design viz, cross sectional, longitudinal retrospective, prospective, experimental, action and feminist study and research designs. | 10h |
| 4. | Data Collection and Presentation: Method of data collection, unstructured and structured interviews, questionnaire, open-ended and closed-ended questions. Collection of data using secondary sources. Ungrouped and grouped data, frequency, cumulative frequency, relative frequency, frequency curve, frequency polygon, histogram, pie chart, ogive curve. | 12h |
| 5. | Hypothesis: Definition, functions and characteristics of hypothesis. Types of hypotheses. Errors in testing a hypothesis. | 10h |
| 6. | Statistical Analysis and Ethics in Research: Statistical Techniques- Measures of central tendency (Mean, Median, Mode). Measures of dispersion (Variance, Standard Deviation). Use of SPSS, R, Excel for data analysis. Ethics- Introduction to research ethics. overt and covert research code of ethics. Intellectual honesty and research integrity. Falsification, Fabrication and plagiarism. IPR | 12h |

References:

- [1] Kothari, C. R. (2014). *Research Methodology: Methods and Techniques* (3rd ed.). New Delhi: New Age International (P) Limited.
- [2] Kothari, C.R. (1990). *Research Methodology: Methods and Techniques*. New Age International.
- [3] Sharma, C.K., & Jain, M.K. (2011). *Research methodology*. Shree Publishers & Distributors.
- [4] Harvey, G. (2010). *Excel 2010 for dummies*. Wiley Publication.
- [5] Garg, B.L., Karadia, R., Agarwal, F., & Agarwal, U.K. (2002). *An introduction to Research Methodology*. RBSA Publishers.
- [6] Sinha, S.C., & Dhiman, A.K. (2002). *Research Methodology*. Ess Ess Publications.
- [7] Trochim, W.M.K. (2005). *Research Methods: The concise knowledge base*. Atomic Dog Publishing.
- [8] Cooper, D., & Schindler, P. (2009). *Business Research Methods*. TMGH, 9th Edition.
- [9] Bryman, A., & Bell, E. (2011). *Business Research Methods*. Oxford University Press.
- [10] Pani, P.K. (2015). *Research Methodology: Principles and Practices*. S.K. Book Agency, New Delhi.
- [11] Pani, P.K. (2015). *Statistical Applications in Social Science Research*. Avon Publications, New Delhi.

(B) Synopsis, Thesis & others (F.M.=200)
Credits: 03+04+01 (Project Synopsis +Project Thesis+Viva-Voce)

Guidelines for Project Work Evaluation

The broad guidelines for the distribution of marks are as follows:

1. **Assessment of Project Synopsis** – 75 Marks
2. **Assessment of Project Thesis** – 75 Marks
3. **Viva-Voce** – 50 Marks

Components of the Paper

The paper will consist of the following components:

1. Research Proposal & Literature Review

- **Proposal Writing:** Research objectives, problem statement, significance, expected outcomes.
- **Literature Review:** Reviewing past research, identifying research gaps, and establishing theoretical foundations.

2. Research Methodology & Design

- **Method Selection:** Mathematical modeling, computational methods, statistical approaches.
- **Data Collection & Processing:** Use of mathematical tools, software (MATLAB, R, Python), and numerical techniques.

3. Hypothesis Formulation & Mathematical Analysis

- **Hypothesis Development:** Defining problems, assumptions, and expected mathematical outcomes.
- **Mathematical Proofs & Computation:** Developing algorithms, equations, or models relevant to the study.

4. Data Interpretation & Statistical Validation

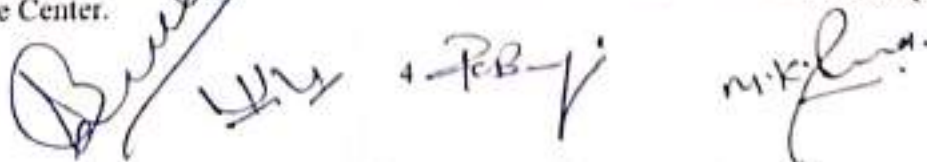
- **Analysis Techniques:** Numerical simulations, statistical tests, optimization methods.
- **Validation:** Comparing results with existing theories, performing sensitivity analysis, and error estimation.

5. Scientific Writing & Thesis Presentation

- **Thesis Structuring:** Abstract, Introduction, Methodology, Results, Discussion, Conclusion.
- **Citation & Referencing:** APA, IEEE, LaTeX formatting styles.
- **Thesis Defense & Viva:** Oral presentation of research, answering questions from faculty and examiners.

References: Recommended books/ suggested reading

- [1] Pandey, P., & Pandey, M. M. (2015). *Research methodology: Tools and techniques*. Bridge Center.



- [2] Kelly, A.E., & Lesh, R.A. (Eds.). (2000). *Handbook of Research Design in Mathematics and Science Education (1st ed.)*. Routledge. <https://doi.org/10.4324/9781410602725>.
- [3] Mishra, Dr. Shanti Bhushan & Alok, Dr. Shashi. (2017). *HANDBOOK OF RESEARCH METHODOLOGY*. Education Publishing
- [4] Cooray, P.G. "Guide to Scientific and technical writing" Hindagala, Sri Lanka (1992)
- [5] Day, R.A. "How to write and publish a scientific paper" Cambridge University press Cambridge (1995)

(Documentation and Presentation of project synopsis/research proposal)

➤ **Documentation:** Format of project synopsis/research proposal in the following sequence.

- (i) Title
- (ii) Introduction
- (iii) Literature survey/ State of art
- (iv) Statement of the problem
- (v) Objective
- (vi) Research question/ Hypothesis (if any)
- (vii) Research Methodology
- (viii) Significance/ Expected contribution of the research to the society
- (ix) Work plan and time line of the proposed work
- (x) Limitations of research
- (xi) References/ Bibliography in oxford latest style like APA or MLA

➤ **Presentation:** Presentation of project synopsis (research proposal) through PPT.

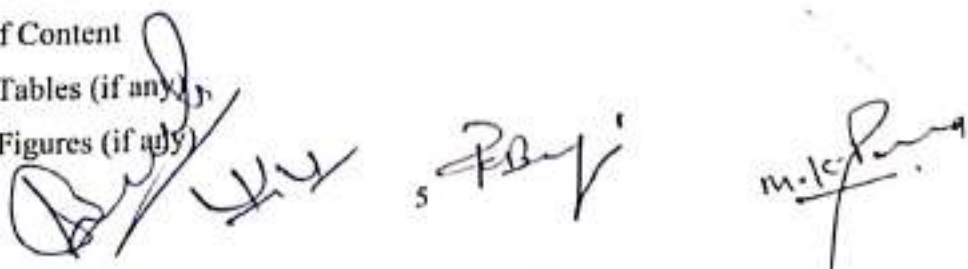
Documentation & Presentation: 55 marks & 20 marks=75 marks

Note: Students must consult with a faculty member in the Department to finalize their project synopsis topics.

(Documentation and Presentation of project Thesis)

➤ **Documentation:** Format of project thesis in the following sequence.

- (i) Title
- (ii) Declaration
- (iii) Certificate
- (iv) Abstract
- (v) Preface/Acknowledgment
- (vi) Table of Content
- (vii) List of Tables (if any)
- (viii) List of Figures (if any)

The bottom of the page features several handwritten signatures and initials in black ink. On the left, there is a large, stylized signature. In the center, there are initials that appear to be 'P.B.' followed by a checkmark. On the right, there is another signature that includes the text 'm.l.c.'.

- (ix) List of Appendices (if any)
- (x) Chapter 1
- (xi) Chapter 2 and continue Chapters
- (xii) References/ Bibliography in oxford latest style

➤ **Presentation:** Presentation of Project Thesis through PPT.

Documentation & Presentation: 60marks & 15marks= 75marks

Note: Students must consult with a faculty member in the Department to finalize their project thesis.

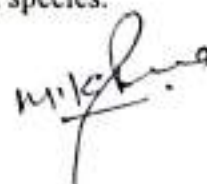
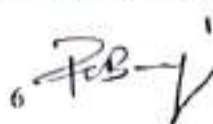
Suggested Project Topics

Students may undertake projects in various Mathematical science related fields or Mathematical research problems or research gaps focusing on pure and applied Mathematical application and socially relevant applications.

Some of the suggested project thesis topics include:

I. Pure Mathematics

1. A Note on Quasi Isometry Groups of Euclidean Spaces.
2. The Distance and Generalized Distance Spectra of Some Graphs.
3. An application on Secure Post Quantum Cryptographic Primitives from Error Correcting Codes and Multivariate Polynomials.
4. Study of some Construction of Hadamard Matrices.
5. A study on Combinatorial Designs and their Applications
6. A Study on Negacyclic Matrices.
7. A Study on Circulant Matrices.
8. The Generalizations of Hadamard Matrices.
9. A Study on Partial Hadamard Matrices.
10. A Study on Complex Hadamard Matrices.
11. A Note on the Eccentricity Matrices of Graphs.
12. A Study on Circulant Partial Hadamard Matrices.
13. Study of Multi Criteria Decision Making (MCDM) and Their Applications
14. A Study on Fuzzy Sets and Application
15. A Study on Laplacian Matrix and Application.
16. Importance of Eigen Value and its Application.
17. Recent Development on Linear Algebra and its Applications of in Different Fields.
18. Least Square Method and Applications.
19. A Study on Fuzzy Graphs and Applications.
20. A Study on Game Theory and Application.
21. A study of Riemann Geometry.
22. Application of concept of tensor on Riemann geometry.
23. Application of Mathematical logic in social science and science.
24. Study of Hilbert space and its effect on convex set.
25. The role of initial stress on elastic wave.
26. Study of pre-open sets, generalized-open sets, semi-open sets in topological space
27. Compactness Separation axioms and connectedness in bitopological species.
28. Integral transforms & their application.



II. Applied Mathematics

1. The Theoretical and Numerical Aspects of the Population Balance Equations.
2. A Study of Fractional Calculus with Application to Characterization of Electrocardiograms.
3. Study of Some Application of Hadamard Matrices.
4. Nonlinear Dynamics of Supply Chain Models.
5. The Spread and Control of Some Infectious Diseases in Patchy Environment Model-Based Studies.
6. A Study of Transition of Information During Major Population.
7. A Study of Transition of Information During Control Population.
8. Impact of National Income During Controlled Governance.
9. Supply Chain Management Under Fuzzy and Stochastic Environment.
10. Mathematical Models on Ecosystem Conservation with Special Emphasis on Fear Factors of Prey or Predator Species.
11. Study of Numerical Solution of Some Classes of Differential Equations.
12. Some Application of Association Scheme.
13. Some Applications of Graph Theory.
14. Some Applications of Difference Equations.
15. A Study on Operation Research and it's Applications.
16. Some Applications of Difference Equations.
17. Investigate how Markov Chains are applied in machine learning, financial forecasting, and decision-making processes.
18. Explore the role of linear algebra in studying social networks, transport systems, and computer science applications.
19. Examine how linear algebra helps model chaotic systems and fractals in physics, biology, and economics.
20. Analyze how linear algebra plays a crucial role in encryption algorithms and modern cybersecurity.
21. Research how spline interpolation techniques improve data smoothing and graphics rendering.
22. Study how linear algebra helps model economic input-output systems and their real-world applications.
23. Investigate how linear algebra shapes the ranking mechanisms behind search engines.
24. Examine the mathematical principles behind tomographic imaging and reconstruction techniques.
25. Analyze how linear algebra helps predict population dynamics and environmental sustainability.
26. Research how linear algebra contributes to game theory and decision-making in economics and artificial intelligence.

Submission Guidelines

- **Word Count:** Typically ranges between 8,000 to 15,000 words.
- **Page Count:** Usually falls between 80 to 150 pages, depending on formatting, content depth, and inclusion of figures, tables, and references.
- Each student must submit their project thesis to the Head of the Department (HOD) after completing the project work before the viva-voce examination.

Note: A candidate has to obtain at least 40% marks in a totality of 75 (Project Synopsis)
75 (Project Thesis) + 50 (Viva-Voce) = 80 marks.

