

Ncert solutions for class 8 maths chapter 9

Question 1. Use a suitable identity to get each of the following products:

(i) $(x + 3)(x + 3)$

(ii) $(2y + 5)(2y + 5)$

(iii) $(2a - 7)(2a - 7)$

(iv) $(3a - 12)(3a - 12)$

(v) $(1.1m - 0.4)(1.1m + 0.4)$

(vi) $(a^2 + b^2)(-a^2 + b^2)$

(vii) $(6x - 7)(6x + 7)$

(viii) $(-a + c)(-a + c)$

(ix) $(x^2 + 3y^4)(x^2 + 3y^4)$

(x) $(7a - 9b)(7a - 9b)$

Solution:

$$\begin{aligned} (i) \quad & (x + 3)(x + 3) \\ &= (x + 3)^2 \\ &= (x)^2 + 2 \times x \times 3 + (3)^2 \\ &= x^2 + 6x + 9 \quad [(a + b)^2 = a^2 + 2ab + b^2] \end{aligned}$$

$$\begin{aligned} (ii) \quad & (2y + 5)(2y + 5) \\ &= (2y + 5)^2 \\ &= (2y)^2 + 2(2y)(5) + (5)^2 \\ & \quad \quad \quad [(a + b)^2 = a^2 + 2ab + b^2] \\ &= 4y^2 + 20y + 25 \end{aligned}$$

$$\begin{aligned} (iii) \quad & (2a - 7)(2a - 7) \\ &= (2a - 7)^2 \\ &= (2a)^2 - 2(2a)(7) + (7)^2 \\ & \quad \quad \quad [(a - b)^2 = a^2 - 2ab + b^2] \\ &= 4a^2 - 28a + 49 \end{aligned}$$

$$\begin{aligned}
(iv) \quad & \left(3a - \frac{1}{2}\right)\left(3a - \frac{1}{2}\right) \\
& = \left(3a - \frac{1}{2}\right)^2 \\
& = (3a)^2 - 2(3a)\left(\frac{1}{2}\right) + \left(\frac{1}{2}\right)^2 \\
& \qquad \qquad \qquad [(a - b)^2 = a^2 - 2ab + b^2] \\
& = 9a^2 - 3a + \frac{1}{4}
\end{aligned}$$

$$\begin{aligned}
(v) \quad & (1.1m - 0.4)(1.1m + 0.4) \\
& = (1.1m)^2 - (0.4)^2 \\
& \qquad \qquad \qquad [(a + b)(a - b) = a^2 - b^2] \\
& = 1.21m^2 - 0.16
\end{aligned}$$

$$\begin{aligned}
(vi) \quad & (a^2 + b^2)(-a^2 + b^2) \\
& = (b^2 + a^2)(b^2 - a^2) \\
& = (b^2)^2 - (a^2)^2 \qquad [(a + b)(a - b) = a^2 - b^2] \\
& = b^4 - a^4 \\
& = -a^4 + b^4
\end{aligned}$$

$$\begin{aligned}
(vii) \quad & (6x - 7)(6x + 7) \\
& = (6x)^2 - (7)^2 \qquad [(a + b)(a - b) = a^2 - b^2] \\
& = 36x^2 - 49
\end{aligned}$$

$$\begin{aligned}
(viii) \quad & (-a + c)(-a + c) \\
& = [(-a) + c]^2 \\
& = (-a)^2 - 2ac + c^2 \\
& = a^2 - 2ac + c^2 \qquad [(a - b)^2 = a^2 - 2ab + b^2]
\end{aligned}$$

$$\begin{aligned}
\text{(ix)} \quad & \left(\frac{x}{2} + \frac{3y}{4}\right)\left(\frac{x}{2} + \frac{3y}{4}\right) \\
& = \left(\frac{x}{2} + \frac{3y}{4}\right)^2 \\
& = \left(\frac{x}{2}\right)^2 + 2\left(\frac{x}{2}\right)\left(\frac{3y}{4}\right) + \left(\frac{3y}{4}\right)^2 \\
& \qquad \qquad \qquad [(a + b)^2 = a^2 + 2ab + b^2] \\
& = \frac{x^2}{4} + \frac{3}{4}xy + \frac{9y^2}{16} \\
\text{(x)} \quad & (7a - 9b)(7a - 9b) \\
& = (7a)^2 - 2(7a)(9b) + (9b)^2 \\
& \qquad \qquad \qquad [(a - b)^2 = a^2 - 2ab + b^2] \\
& = 49a^2 - 126ab + 81b^2
\end{aligned}$$

Question 2. Use the identity $(x + a)(x + b) = x^2 + (a + b)x + ab$ to find the following products.

(i) $(x + 3)(x + 7)$

(ii) $(4x + 5)(4x + 1)$

(iii) $(4x - 5)(4x - 1)$

(iv) $(4x + 5)(4x - 1)$

(v) $(2x + 5y)(2x + 3y)$

(vi) $(2a^2 + 9)(2a^2 + 5)$

(vii) $(xyz - 4)(xyz - 2)$

Solution:

$$\begin{aligned}
(i) \quad & (x + 3)(x + 7) \\
& = x^2 + (3 + 7)x + 3 \times 7 \\
& = x^2 + 10x + 21 \\
(ii) \quad & (4x + 5)(4x + 1) \\
& = (4x)^2 + (5 + 1)(4x) + 5 \times 1 \\
& = 16x^2 + 6(4x) + 5 \\
& = 16x^2 + 24x + 5 \\
(iii) \quad & (4x - 5)(4x - 1) \\
& = (4x)^2 - (5 + 1)(4x) + (-5) \times (-1) \\
& = 16x^2 - 6(4x) + 5 \\
& = 16x^2 - 24x + 5 \\
(iv) \quad & (4x + 5)(4x - 1)^2 \\
& = (4x)^2 + (5 - 1)(4x) + 5 \times (-1) \\
& = 16x^2 + 4(4x) - 5 \\
& = 16x^2 + 16x - 5 \\
(v) \quad & (2x + 5y)(2x + 3y) \\
& = (2x)^2 + (5y + 3y)(2x) + (5y)(3y) \\
& = 4x^2 + (8y)(2x) + 15y^2 \\
& = 4x^2 + 16xy + 15y^2 \\
(vi) \quad & (2a^2 + 9)(2a^2 + 5) \\
& = (2a^2)^2 + (9 + 5)(2a^2) + 5 \times 9 \\
& = 4a^4 + (14)(2a^2) + 45 \\
& = 4a^4 + 28a^2 + 45 \\
(vii) \quad & (xyz - 4)(xyz - 2) \\
& = (xyz)^2 - (4 + 2)(xyz) + (-4)(-2) \\
& = x^2y^2z^2 - (6)(xyz) + 8 \\
& = x^2y^2z^2 - 6xyz + 8
\end{aligned}$$

Question 3. Find the following squares by using the identities.

- (i) $(b - 7)^2$
- (ii) $(xy + 3z)^2$
- (iii) $(6x^2 - 5y)^2$
- (iv) $(23m + 32n)^2$
- (v) $(0.4p - 0.5q)^2$
- (vi) $(2xy + 5y)^2$

Solution:

$$\begin{aligned}
 \text{(i)} \quad (b - 7)^2 &= (b)^2 - 2(b)(7) + (7)^2 \\
 &= b^2 - 14b + 49 \\
 &\quad \text{[using } (a - b)^2 = a^2 - 2ab + b^2\text{]}
 \end{aligned}$$

$$\begin{aligned}
 \text{(ii)} \quad (xy + 3z)^2 & \\
 &= (xy)^2 + 2(xy)(3z) + (3z)^2 \\
 &\quad \text{[using } (a + b)^2 = a^2 + 2ab + b^2\text{]} \\
 &= x^2y^2 + 6xyz + 9z^2
 \end{aligned}$$

$$\begin{aligned}
 \text{(iii)} \quad (6x^2 - 5y)^2 & \\
 &= (6x^2)^2 - 2(6x^2)(5y) + (5y)^2 \\
 &\quad \text{[using } (a - b)^2 = a^2 - 2ab + b^2\text{]} \\
 &= 36x^4 - 60x^2y + 25y^2
 \end{aligned}$$

$$\begin{aligned}
 \text{(iv)} \quad \left(\frac{2}{3}m + \frac{3}{2}n\right)^2 & \\
 &= \left(\frac{2}{3}m\right)^2 + 2\left(\frac{2}{3}m\right)\left(\frac{3}{2}n\right) + \left(\frac{3}{2}n\right)^2 \\
 &\quad \text{[using } (a + b)^2 = a^2 + 2ab + b^2\text{]} \\
 &= \frac{4}{9}m^2 + 2mn + \frac{9}{4}n^2
 \end{aligned}$$

$$\begin{aligned}
 \text{(v)} \quad (0.4p - 0.5q)^2 & \\
 &= (0.4p)^2 - 2(0.4p)(0.5q) + (0.5q)^2 \\
 &\quad \text{[using } (a - b)^2 = a^2 - 2ab + b^2\text{]} \\
 &= 0.16p^2 - 0.4pq + 0.25q^2
 \end{aligned}$$

$$\begin{aligned}
 \text{(vi)} \quad (2xy + 5y)^2 & \\
 &= (2xy)^2 + 2(2xy)(5y) + (5y)^2 \\
 &\quad \text{[using } (a + b)^2 = a^2 + 2ab + b^2\text{]} \\
 &= 4x^2y^2 + 20xy^2 + 25y^2
 \end{aligned}$$

Question 4. Simplify:

$$\text{(i)} \quad (a^2 - b^2)^2$$

$$\text{(ii)} \quad (2x + 5)^2 - (2x - 5)^2$$

$$\text{(iii)} \quad (7m - 8n)^2 + (7m + 8n)^2$$

$$(iv) (4m + 5n)^2 + (5m + 4n)^2$$

$$(v) (2.5p - 1.5q)^2 - (1.5p - 2.5q)^2$$

$$(vi) (ab + bc)^2 - 2ab^2c$$

$$(vii) (m^2 - n^2m)^2 + 2m^3n^2$$

Solution:

$$\begin{aligned}(i) (a^2 - b^2)^2 &= (a^2)^2 - 2a^2b^2 + (b^2)^2 \\ &= a^4 - 2a^2b^2 + b^4 \\ &\quad [\text{using } (a - b)^2 = a^2 - 2ab + b^2]\end{aligned}$$

$$\begin{aligned}(ii) (2x + 5)^2 - (2x - 5)^2 &= [(2x)^2 + 2(2x)(5) + (5)^2] - [(2x)^2 \\ &\quad - 2(2x)(5) + (5)^2] \\ &= (4x^2 + 20x + 25) - (4x^2 - 20x + 25) \\ &= \cancel{4x^2} + 20x + \cancel{25} - \cancel{4x^2} + 20x - \cancel{25} \\ &= 20x + 20x = 40x\end{aligned}$$

Alternately:

$$\begin{aligned}(2x + 5)^2 - (2x - 5)^2 &= [(2x + 5) + (2x - 5)] (2x + 5) - (2x - 5) \\ &\quad [\text{using } a^2 - b^2 = (a + b)(a - b)] \\ &= (2x + \cancel{5} + 2x - \cancel{5}) (\cancel{2x} + 5 - \cancel{2x} + 5) \\ &= (2x + 2x)(5 + 5) \\ &= 4x \times 10 = 40x\end{aligned}$$

$$\begin{aligned}(iii) (7m - 8n)^2 + (7m + 8n)^2 &= (7m)^2 - 2(7m)(8n) + (8n)^2 + (7m)^2 \\ &\quad + 2(7m)(8n) + (8n)^2 \\ &= 49m^2 - \cancel{112mn} + 64n^2 + 49m^2 \\ &\quad + \cancel{112mn} + 64n^2 \\ &= 98m^2 + 128n^2\end{aligned}$$

$$\begin{aligned}
 (iv) \quad & (4m + 5n)^2 + (5m + 4n)^2 \\
 &= (4m)^2 + 2(4m)(5n) + (5n)^2 \\
 &\quad + (5m)^2 + 2(5m)(4n) + (4n)^2 \\
 &= 16m^2 + 40mn + 25n^2 + 25m^2 \\
 &\quad + 40mn + 16n^2 \\
 &= 41m^2 + 80mn + 41n^2
 \end{aligned}$$

$$\begin{aligned}
 (v) \quad & (2.5p - 1.5q)^2 - (1.5p - 2.5q)^2 \\
 &= [(2.5p)^2 - 2(2.5p)(1.5q) + (1.5q)^2] \\
 &\quad - [(1.5p)^2 - 2(1.5p)(2.5q) + (2.5q)^2] \\
 &= (6.25p^2 - 7.5pq + 2.25q^2) \\
 &\quad - (2.25p^2 - 7.5pq + 6.25q^2) \\
 &= 6.25p^2 - \cancel{7.5pq} + 2.25q^2 \\
 &\quad - 2.25p^2 + \cancel{7.5pq} - 6.25q^2 \\
 &= 6.25p^2 - 2.25p^2 + 2.25q^2 - 6.25q^2 \\
 &= 4p^2 - 4q^2
 \end{aligned}$$

$$\begin{aligned}
 (vi) \quad & (ab + bc)^2 - 2ab^2c \\
 &= (ab)^2 + 2(ab)(bc) + (bc)^2 - 2ab^2c \\
 &= a^2b^2 + \cancel{2ab^2c} + b^2c^2 - \cancel{2ab^2c} \\
 &= a^2b^2 + b^2c^2
 \end{aligned}$$

$$\begin{aligned}
 (vii) \quad & (m^2 - n^2m)^2 + 2m^3n^2 \\
 &= (m^2)^2 - 2m^2(n^2m) + (n^2m)^2 + 2m^3n^2 \\
 &= m^4 - \cancel{2m^3n^2} + n^4m^2 + \cancel{2m^3n^2} \\
 &= m^4 + n^4m^2
 \end{aligned}$$

Question 5. Show that:

$$(i) \quad (3x + 7)^2 - 84x = (3x - 7)^2$$

$$(ii) \quad (9p - 5q)^2 + 180pq = (9p + 5q)^2$$

$$(iii) \quad (43m - 34n)^2 + 2mn = 169m^2 + 916n^2$$

$$(iv) \quad (4pq + 3q)^2 - (4pq - 3q)^2 = 48pq^2$$

$$(v) \quad (a - b)(a + b) + (b - c)(b + c) + (c - a)(c + a) = 0$$

Solution:

(i) To Show that:

$$(3x + 7)^2 - 84x = (3x - 7)^2$$

$$\text{LHS} = (3x + 7)^2 - 84x$$

$$= (3x)^2 + 2(3x)(7) + (7)^2 - 84x$$

$$= 9x^2 + 42x + 49 - 84x$$

$$= 9x^2 - 42x + 49$$

$$= (3x)^2 - 2(3x)(7) + (7)^2$$

$$= (3x - 7)^2 = \text{RHS}$$

$$\text{LHS} = \text{RHS}$$

Hence, proved.

(ii) To show that:

$$(9p - 5q)^2 + 180pq = (9p + 5q)^2$$

$$\text{LHS} = (9p - 5q)^2 + 180pq$$

$$= (9p)^2 - 2(9p)(5q) + (5q)^2 + 180pq$$

$$= 81p^2 - 90pq + 25q^2 + 180pq$$

$$= 81p^2 + 90pq + 25q^2$$

$$= (9p)^2 + 2(9p)(5q) + (5q)^2$$

$$= (9p + 5q)^2 = \text{RHS}$$

$$\text{LHS} = \text{RHS}$$

Hence, proved.

(iii) To show that:

$$\left(\frac{4}{3}m - \frac{3}{4}n\right)^2 + 2mn = \frac{16}{9}m^2 + \frac{9}{16}n^2$$

$$\begin{aligned}\text{LHS} &= \left(\frac{4}{3}m - \frac{3}{4}n\right)^2 + 2mn \\ &= \left(\frac{4}{3}m\right)^2 - 2\left(\frac{4}{3}m\right)\left(\frac{3}{4}n\right) + \left(\frac{3}{4}n\right)^2 + 2mn \\ &= \frac{16}{9}m^2 - \cancel{2mn} + \frac{9}{16}n^2 + \cancel{2mn} \\ &= \frac{16}{9}m^2 + \frac{9}{16}n^2 = \text{RHS}\end{aligned}$$

$$\text{LHS} = \text{RHS}$$

Hence, proved.

(iv) To show that:

$$\begin{aligned}(4pq + 3q)^2 - (4p - 3q)^2 &= 48pq^2 \\ \text{LHS} &= (4pq + 3q)^2 - (4pq - 3q)^2 \\ &= [(4pq + 3q) + (4pq - 3q)] \\ &\quad [(4pq + 3q) - (4pq - 3q)] \\ &= (4pq + \cancel{3q} + 4pq - \cancel{3q}) \\ &\quad (\cancel{4pq} + 3q - \cancel{4pq} + 3q) \\ &= (8pq)(6q) \\ &= 48pq^2 = \text{RHS}\end{aligned}$$

$$\text{LHS} = \text{RHS}$$

Hence, proved.

(v) To show that:

$$\begin{aligned}(a - b)(a + b) + (b - c)(b + c) + (c - a)(c + a) \\ &= 0 \\ \text{LHS} &= (a^2 - b^2) + (b^2 - c^2) + (c^2 - a^2) \\ &\quad [\because (x + y)(x - y) = x^2 - y^2] \\ &= \cancel{a^2} - \cancel{b^2} + \cancel{b^2} - \cancel{c^2} + \cancel{c^2} - \cancel{a^2} \\ &= 0 = \text{RHS} \\ \text{LHS} &= \text{RHS} \\ \text{Hence, proved.}\end{aligned}$$

Question 6. Using identities, evaluate:

(i) 712 (ii) 992 (iii) 1022 (iv) 9982 (v) 5.22

(vi) 297×303 (vii) 78×82 (viii) 8.92 (ix) 1.05×9.5

Solution:

$$\begin{aligned} \text{(i) } 71^2 &= (70 + 1)^2 \\ &= (70)^2 + 2(70)(1) + (1)^2 \\ &\quad [(a + b)^2 = a^2 + 2ab + b^2] \\ &= 4900 + 140 + 1 \\ &= 5041 \end{aligned}$$

Hence, $71^2 = 5041$

$$\begin{aligned} \text{(ii) } 99^2 &= (100 - 1)^2 \\ &= (100)^2 - 2(100)(1) + (1)^2 \\ &\quad [(a - b)^2 = a^2 - 2ab + b^2] \\ &= 10000 - 200 + 1 \\ &= 10001 - 200 \\ &= 9801 \end{aligned}$$

Hence, $99^2 = 9801$

$$\begin{aligned} \text{(iii) } 102^2 &= (100 + 2)^2 \\ &= (100)^2 + 2(100)(2) + (2)^2 \\ &\quad [(a + b)^2 = a^2 + 2ab + b^2] \\ &= 10000 + 400 + 4 \\ &= 10404 \end{aligned}$$

Hence, $102^2 = 10404$

$$\begin{aligned} \text{(iv) } 998^2 &= (1000 - 2)^2 \\ &= (1000)^2 - 2(1000)(2) + (2)^2 \\ &\quad [(a - b)^2 = a^2 - 2ab + b^2] \\ &= 1000000 - 4000 + 4 \\ &= 1000004 - 4000 \\ &= 996004 \end{aligned}$$

Hence, $998^2 = 996004$

$$\begin{aligned}
 (v) \quad 5.2^2 &= (5 + 0.2)^2 \\
 &= (5)^2 + 2(5)(0.2) + (0.2)^2 \\
 &\qquad\qquad\qquad [(a + b)^2 = a^2 + 2ab + b^2] \\
 &= 25 + 2 + 0.04 \\
 &= 27 + 0.04 \\
 &= 27.04
 \end{aligned}$$

Hence, $(5.2)^2 = 27.04$

$$\begin{aligned}
 (vi) \quad 297 \times 303 &= (300 - 3)(300 + 3) \\
 &= (300)^2 - (3)^2 \quad [(a + b)(a - b) = a^2 - b^2] \\
 &= 90000 - 9 \\
 &= 89991
 \end{aligned}$$

Hence, $297 \times 303 = 89991$

$$\begin{aligned}
 (vii) \quad 78 \times 82 &= (80 - 2)(80 + 2) \\
 &= (80)^2 - (2)^2 \quad [(a + b)(a - b) = a^2 - b^2] \\
 &= 6400 - 4 \\
 &= 6396
 \end{aligned}$$

Hence, $78 \times 82 = 6396$

$$\begin{aligned}
 (viii) \quad 8.9^2 &= (9 - 0.1)^2 \\
 &= (9)^2 - 2(9)(0.1) + (0.1)^2 \\
 &\qquad\qquad\qquad [(a - b)^2 = a^2 - 2ab + b^2] \\
 &= 81 - 1.8 + 0.01 \\
 &= 81.01 - 1.8 \\
 &= 79.21
 \end{aligned}$$

Hence, $8.9^2 = 79.21$

$$\begin{aligned}
 (ix) \quad 1.05 \times 9.5 &= (1 + 0.5)(10 - 0.5) \\
 &= 1(10 - 0.5) + 0.05(10 - 0.5) \\
 &= 10 - 0.5 + 0.05 \times 10 - 0.05 \times 0.5 \\
 &= 10 - 0.5 + 0.5 - 0.025 \\
 &= 10.5 - 0.525 \\
 &= 9.975
 \end{aligned}$$

Hence, $1.05 \times 9.5 = 9.975$

Question 7. Using $a^2 - b^2 = (a + b)(a - b)$, find

(i) $512 - 492$

(ii) $(1.02)^2 - (0.98)^2$

(iii) $1532 - 1472$

(iv) $12.12 - 7.92$

Solution:

(i) $512 - 492 = (51 + 49)(51 - 49) = 100 \times 2 = 200$

(ii) $(1.02)^2 - (0.98)^2 = (1.02 + 0.98)(1.02 - 0.98) = 2.00 \times 0.04 = 0.08$

(iii) $1532 - 1472 = (153 + 147)(153 - 147) = 300 \times 6 = 1800$

(iv) $12.12 - 7.92 = (12.1 + 7.9)(12.1 - 7.9) = 20.0 \times 4.2 = 84$

Question 8. Using $(x + a)(x + b) = x^2 + (a + b)x + ab$, find

(i) 103×104

(ii) 5.1×5.2

(iii) 103×98

(iv) 9.7×9.8

Solution:

(i) $103 \times 104 = (100 + 3)(100 + 4) = (100)^2 + (3 + 4)(100) + 3 \times 4 = 10000 + 700 + 12 = 10712$

(ii) $5.1 \times 5.2 = (5 + 0.1)(5 + 0.2) = (5)^2 + (0.1 + 0.2)(5) + 0.1 \times 0.2 = 25 + 1.5 + 0.02 = 26.5 + 0.02 = 26.52$

(iii) $103 \times 98 = (100 + 3)(100 - 2) = (100)^2 + (3 - 2)(100) + 3 \times (-2) = 10000 + 100 - 6 = 10100 - 6 = 10094$

(iv) $9.7 \times 9.8 = (10 - 0.3)(10 - 0.2) = (10)^2 - (0.3 + 0.2)(10) + (-0.3)(-0.2) = 100 - 5 + 0.06 = 95 + 0.06 = 95.06$

Q1 : Use a suitable identity to get each of the following products.

(i) $(x + 3)(x + 3)$ (ii) $(2y + 5)(2y + 5)$

(iii) $(2a - 7)(2a - 7)$ (iv) $\left(3a - \frac{1}{2}\right)\left(3a - \frac{1}{2}\right)$

(v) $(1.1m - 0.4)(1.1m + 0.4)$ (vi) $(a^2 + b^2)(-a^2 + b^2)$

(vii) $(6x - 7)(6x + 7)$ (viii) $(-a + c)(-a + c)$

(ix) $\left(\frac{x}{2} + \frac{3y}{4}\right)\left(\frac{x}{2} + \frac{3y}{4}\right)$ (x) $(7a - 9b)(7a - 9b)$

Answer :

The products will be as follows.

$$\begin{aligned} \text{(i)} \quad (x + 3)(x + 3) &= (x + 3)^2 \\ &= (x)^2 + 2(x)(3) + (3)^2 \quad [(a + b)^2 = a^2 + 2ab + b^2] \\ &= x^2 + 6x + 9 \end{aligned}$$

$$\begin{aligned} \text{(ii)} \quad (2y + 5)(2y + 5) &= (2y + 5)^2 \\ &= (2y)^2 + 2(2y)(5) + (5)^2 \quad [(a + b)^2 = a^2 + 2ab + b^2] \\ &= 4y^2 + 20y + 25 \end{aligned}$$

$$\begin{aligned} \text{(iii)} \quad (2a - 7)(2a - 7) &= (2a - 7)^2 \\ &= (2a)^2 - 2(2a)(7) + (7)^2 \quad [(a - b)^2 = a^2 - 2ab + b^2] \end{aligned}$$

$$= 9a^2 - 3a + \frac{1}{4}$$

$$(v) (1.1m - 0.4)(1.1m + 0.4)$$

$$= (1.1m)^2 - (0.4)^2 [(a + b)(a - b) = a^2 - b^2]$$

$$= 1.21m^2 - 0.16$$

$$(vi) (a^2 + b^2)(-a^2 + b^2) = (b^2 + a^2)(b^2 - a^2)$$

$$= (b^2)^2 - (a^2)^2 [(a + b)(a - b) = a^2 - b^2]$$

$$= b^4 - a^4$$

$$(vii) (6x - 7)(6x + 7) = (6x)^2 - (7)^2 [(a + b)(a - b) = a^2 - b^2]$$

$$= 36x^2 - 49$$

$$(viii) (-a + c)(-a + c) = (-a + c)^2$$

$$= (-a)^2 + 2(-a)(c) + (c)^2 [(a + b)^2 = a^2 + 2ab + b^2]$$

$$= a^2 - 2ac + c^2$$

$$(ix) \left(\frac{x}{2} + \frac{3y}{4}\right)\left(\frac{x}{2} + \frac{3y}{4}\right) = \left(\frac{x}{2} + \frac{3y}{4}\right)^2$$

$$= \left(\frac{x}{2}\right)^2 + 2\left(\frac{x}{2}\right)\left(\frac{3y}{4}\right) + \left(\frac{3y}{4}\right)^2 [(a + b)^2 = a^2 + 2ab + b^2]$$

$$= \frac{x^2}{4} + \frac{3xy}{4} + \frac{9y^2}{16}$$

$$(x) (7a - 9b)(7a - 9b) = (7a - 9b)^2$$

$$= (7a)^2 - 2(7a)(9b) + (9b)^2 [(a - b)^2 = a^2 - 2ab + b^2]$$

(v) $(2x+5y)(2x+3y)$ (vi) $(2a^2+9)(2a^2+5)$

(vii) $(xyz-4)(xyz-2)$

Answer :

The products will be as follows.

(i) $(x+3)(x+7) = x^2 + (3+7)x + (3)(7)$

$= x^2 + 10x + 21$

(ii) $(4x+5)(4x+1) = (4x)^2 + (5+1)(4x) + (5)(1)$

$= 16x^2 + 24x + 5$

(iii) $(4x-5)(4x-1) = (4x)^2 + [(-5)+(-1)](4x) + (-5)(-1)$

$= 16x^2 - 24x + 5$

(iv) $(4x+5)(4x-1) = (4x)^2 + [(5)+(-1)](4x) + (5)(-1)$

$= 16x^2 + 16x - 5$

(v) $(2x+5y)(2x+3y) = (2x)^2 + (5y+3y)(2x) + (5y)(3y)$

$= 4x^2 + 16xy + 15y^2$

(vi) $(2a^2+9)(2a^2+5) = (2a^2)^2 + (9+5)(2a^2) + (9)(5)$

$= 4a^4 + 28a^2 + 45$

(vii) $(xyz-4)(xyz-2)$

$= (xyz)^2 + [(-4)+(-2)](xyz) + (-4)(-2)$

$= x^2y^2z^2 - 6xyz + 8$

Answer :

$$(i) (b - 7)^2 = (b)^2 - 2(b)(7) + (7)^2 \quad [(a - b)^2 = a^2 - 2ab + b^2]$$

$$= b^2 - 14b + 49$$

$$(ii) (xy + 3z)^2 = (xy)^2 + 2(xy)(3z) + (3z)^2 \quad [(a + b)^2 = a^2 + 2ab + b^2]$$

$$= x^2y^2 + 6xyz + 9z^2$$

$$(iii) (6x^2 - 5y)^2 = (6x^2)^2 - 2(6x^2)(5y) + (5y)^2 \quad [(a - b)^2 = a^2 - 2ab + b^2]$$

$$= 36x^4 - 60x^2y + 25y^2$$

$$(iv) \left(\frac{2}{3}m + \frac{3}{2}n\right)^2 = \left(\frac{2}{3}m\right)^2 + 2\left(\frac{2}{3}m\right)\left(\frac{3}{2}n\right) + \left(\frac{3}{2}n\right)^2 \quad [(a + b)^2 = a^2 + 2ab + b^2]$$

$$= \frac{4}{9}m^2 + 2mn + \frac{9}{4}n^2$$

$$(v) (0.4p - 0.5q)^2 = (0.4p)^2 - 2(0.4p)(0.5q) + (0.5q)^2$$

$$[(a - b)^2 = a^2 - 2ab + b^2]$$

$$= 0.16p^2 - 0.4pq + 0.25q^2$$

$$(vi) (2xy + 5y)^2 = (2xy)^2 + 2(2xy)(5y) + (5y)^2$$

$$[(a + b)^2 = a^2 + 2ab + b^2]$$

$$= 4x^2y^2 + 20xy^2 + 25y^2$$

Q4 : Simplify.

Answer :

$$\begin{aligned} \text{(i)} \quad (a^2 - b^2)^2 &= (a^2)^2 - 2(a^2)(b^2) + (b^2)^2 \quad [(a - b)^2 = a^2 - 2ab + b^2] \\ &= a^4 - 2a^2b^2 + b^4 \end{aligned}$$

$$\begin{aligned} \text{(ii)} \quad (2x+5)^2 - (2x-5)^2 &= (2x)^2 + 2(2x)(5) + (5)^2 - [(2x)^2 - 2(2x)(5) + (5)^2] \\ &[(a - b)^2 = a^2 - 2ab + b^2] \end{aligned}$$

$$[(a + b)^2 = a^2 + 2ab + b^2]$$

$$= 4x^2 + 20x + 25 - [4x^2 - 20x + 25]$$

$$= 4x^2 + 20x + 25 - 4x^2 + 20x - 25 = 40x$$

$$\text{(iii)} \quad (7m - 8n)^2 + (7m + 8n)^2$$

$$= (7m)^2 - 2(7m)(8n) + (8n)^2 + (7m)^2 + 2(7m)(8n) + (8n)^2$$

$$[(a - b)^2 = a^2 - 2ab + b^2 \text{ and } (a + b)^2 = a^2 + 2ab + b^2]$$

$$= 49m^2 - 112mn + 64n^2 + 49m^2 + 112mn + 64n^2$$

$$= 98m^2 + 128n^2$$

$$\text{(iv)} \quad (4m + 5n)^2 + (5m + 4n)^2$$

$$= (4m)^2 + 2(4m)(5n) + (5n)^2 + (5m)^2 + 2(5m)(4n) + (4n)^2$$

$$[(a + b)^2 = a^2 + 2ab + b^2]$$

$$= 16m^2 + 40mn + 25n^2 + 25m^2 + 40mn + 16n^2$$

$$= 41m^2 + 80mn + 41n^2$$

$$\text{(v)} \quad (2.5p - 1.5q)^2 - (1.5p - 2.5q)^2$$

$$(vi) (ab + bc)^2 - 2ab^2c$$

$$= (ab)^2 + 2(ab)(bc) + (bc)^2 - 2ab^2c \quad [(a + b)^2 = a^2 + 2ab + b^2]$$

$$= a^2b^2 + 2ab^2c + b^2c^2 - 2ab^2c$$

$$= a^2b^2 + b^2c^2$$

$$(vii) (m^2 - n^2m)^2 + 2m^3n^2$$

$$= (m^2)^2 - 2(m^2)(n^2m) + (n^2m)^2 + 2m^3n^2 \quad [(a - b)^2 = a^2 - 2ab + b^2]$$

$$= m^4 - 2m^3n^2 + m^3n^2 + 2m^3n^2$$

Q5 : Show that

$$(i) (3x + 7)^2 - 84x = (3x - 7)^2 \quad (ii) (9p - 5q)^2 + 180pq = (9p + 5q)^2$$

$$(iii) \left(\frac{4}{3}m - \frac{3}{4}n\right)^2 + 2mn = \frac{16}{9}m^2 + \frac{9}{16}n^2$$

$$(iv) (4pq + 3q)^2 - (4pq - 3q)^2 = 48pq^2$$

$$(v) (a - b)(a + b) + (b - c)(b + c) + (c - a)(c + a) = 0$$

Answer :

$$(i) \text{ L.H.S} = (3x + 7)^2 - 84x$$

$$= (3x)^2 + 2(3x)(7) + (7)^2 - 84x$$

$$= 9x^2 + 42x + 49 - 84x$$

$$= 9x^2 - 42x + 49$$

$$\text{R.H.S} = (3x - 7)^2 = (3x)^2 - 2(3x)(7) + (7)^2$$

$$= 9x^2 - 42x + 49$$

$$\text{L.H.S} = \text{R.H.S}$$

$$(ii) \text{ L.H.S} = (9p - 5q)^2 + 180pq$$

$$= (9p)^2 - 2(9p)(5q) + (5q)^2 + 180pq$$

$$= 81p^2 - 90pq + 25q^2 + 180pq$$

$$= 81p^2 + 90pq + 25q^2$$

$$\begin{aligned}
 \text{(iii) L.H.S} &= \left(\frac{4}{3}m - \frac{3}{4}n\right)^2 + 2mn \\
 &= \left(\frac{4}{3}m\right)^2 - 2\left(\frac{4}{3}m\right)\left(\frac{3}{4}n\right) + \left(\frac{3}{4}n\right)^2 + 2mn \\
 &= \frac{16}{9}m^2 - 2mn + \frac{9}{16}n^2 + 2mn \\
 &= \frac{16}{9}m^2 + \frac{9}{16}n^2 = \text{R.H.S.}
 \end{aligned}$$

$$\begin{aligned}
 \text{(iv) L.H.S} &= (4pq + 3q)^2 - (4pq - 3q)^2 \\
 &= (4pq)^2 + 2(4pq)(3q) + (3q)^2 - [(4pq)^2 - 2(4pq)(3q) + (3q)^2] \\
 &= 16p^2q^2 + 24pq^2 + 9q^2 - [16p^2q^2 - 24pq^2 + 9q^2] \\
 &= 16p^2q^2 + 24pq^2 + 9q^2 - 16p^2q^2 + 24pq^2 - 9q^2 \\
 &= 48pq^2 = \text{R.H.S}
 \end{aligned}$$

Q6 : Using identities, evaluate.

(i) 71^2 (ii) 99^2 (iii) 102^2 (iv) 998^2

(v) $(5.2)^2$ (vi) 297×303 (vii) 78×82

(viii) 8.9^2 (ix) 1.05×9.5

Answer :

$$\begin{aligned}
 \text{(i) } 71^2 &= (70 + 1)^2 \\
 &= (70)^2 + 2(70)(1) + (1)^2 \quad [(a + b)^2 = a^2 + 2ab + b^2] \\
 &= 4900 + 140 + 1 = 5041
 \end{aligned}$$

$$\begin{aligned}
 \text{(ii) } 99^2 &= (100 - 1)^2 \\
 &= (100)^2 - 2(100)(1) + (1)^2 \quad [(a - b)^2 = a^2 - 2ab + b^2] \\
 &= 10000 - 200 + 1 = 9801
 \end{aligned}$$

$$\begin{aligned}
 \text{(iii) } 102^2 &= (100 + 2)^2 \\
 &= (100)^2 + 2(100)(2) + (2)^2 \quad [(a + b)^2 = a^2 + 2ab + b^2] \\
 &= 10000 + 400 + 4 = 10404
 \end{aligned}$$

$$\begin{aligned}
 \text{(iv) } 998^2 &= (1000 - 2)^2 \\
 &= (1000)^2 - 2(1000)(2) + (2)^2 \quad [(a - b)^2 = a^2 - 2ab + b^2]
 \end{aligned}$$

$$(vi) 297 \times 303 = (300 - 3) \times (300 + 3)$$

$$= (300)^2 - (3)^2 \quad [(a + b)(a - b) = a^2 - b^2]$$

$$= 90000 - 9 = 89991$$

$$(vii) 78 \times 82 = (80 - 2)(80 + 2)$$

$$= (80)^2 - (2)^2 \quad [(a + b)(a - b) = a^2 - b^2]$$

$$= 6400 - 4 = 6396$$

$$(viii) 8.9^2 = (9.0 - 0.1)^2$$

$$= (9.0)^2 - 2(9.0)(0.1) + (0.1)^2 \quad [(a - b)^2 = a^2 - 2ab + b^2]$$

$$= 81 - 1.8 + 0.01 = 79.21$$

$$(ix) 1.05 \times 9.5 = 1.05 \times 0.95 \times 10$$

$$= (1 + 0.05)(1 - 0.05) \times 10$$

Q7 : Using $a^2 - b^2 = (a + b)(a - b)$, find

(i) $51^2 - 49^2$ (ii) $(1.02)^2 - (0.98)^2$ (iii) 153^2

(iv) $12.1^2 - 7.9^2$

Answer :

(i) $51^2 - 49^2 = (51 + 49)(51 - 49)$

$= (100)(2) = 200$

(ii) $(1.02)^2 - (0.98)^2 = (1.02 + 0.98)(1.02$

$= (2)(0.04) = 0.08$

(iii) $153^2 - 147^2 = (153 + 147)(153 - 147)$

$= (300)(6) = 1800$

Q8 : Using $(x + a)(x + b) = x^2 + (a + b)x + ab$, find

(i) 103×104 (ii) 5.1×5.2 (iii) 103×98 (iv) 9.7×9.8

Answer :

$$(i) 103 \times 104 = (100 + 3)(100 + 4)$$

$$= (100)^2 + (3 + 4)(100) + (3)(4)$$

$$= 10000 + 700 + 12 = 10712$$

$$(ii) 5.1 \times 5.2 = (5 + 0.1)(5 + 0.2)$$

$$= (5)^2 + (0.1 + 0.2)(5) + (0.1)(0.2)$$

$$= 25 + 1.5 + 0.02 = 26.52$$

$$(iii) 103 \times 98 = (100 + 3)(100 - 2)$$

$$= (100)^2 + [3 + (-2)](100) + (3)(-2)$$

$$= 10000 + 100 - 6$$

$$= 10094$$