JEE Main 2024 Mock Test 6

Time Allotted: 3 Hours Maximum Marks: 300

Please read the instructions carefully. You are allotted 5 minutes specifically for this purpose.

Important Instructions:

- 1. The test is of 3 hours duration.
- 2. This test paper consists of 90 questions. Each subject (PCM) has 30 questions. The maximum marks are 300.
- 3. This question paper contains **Three Parts. Part-A** is Physics, **Part-B** is Chemistry and **Part-C** is Mathematics. Each part has only two sections: **Section-A** and **Section-B**.
- Section A : Attempt all questions.
- 5. **Section B :** Do any 5 questions out of 10 Questions.
- 6. **Section-A (01 20)** contains 20 multiple choice questions which have **only one correct answer**. Each question carries **+4 marks** for correct answer and **–1 mark** for wrong answer.
- 7. **Section-B** (1 10) contains 10 Numerical based questions. The answer to each question is rounded off to the nearest integer value. Each question carries **+4 marks** for correct answer and **–1 mark** for wrong answer.

PART - A (PHYSICS)

SECTION - A

(One Options Correct Type)

This section contains **20 multiple choice questions**. Each question has **four choices** (A), (B), (C) and (D), out of which **ONLY ONE** option is correct.

If the distance of the earth from sun is 1.5×10^6 km. Then the distance of an imaginary planet

| α | from Sun, if its period of revolution is 2.83 years is: | | | | | |
|-----|--|------------------------------------|--|--|--|--|
| | (A) 6×10 ⁶ km | (B) 3×10 ⁶ km | | | | |
| | (C) $6 \times 10^7 \text{km}$ | (D) $3 \times 10^7 \text{km}$ | | | | |
| Q2. | Let γ_1 be the ratio of molar specific heat at constant pressure and molar specific heat at constant volume of a monoatomic gas and γ_2 be the similar ratio of diatomic gas. Considering the diatomic | | | | | |
| | gas molecule as a rigid rotator t | the ratio $\frac{\gamma_1}{1}$ is: | | | | |

| (A) $\frac{27}{35}$ | (B) $\frac{35}{27}$ |
|---------------------|---------------------|
| (C) $\frac{25}{21}$ | (D) $\frac{21}{25}$ |

Q3. Given below are two statements : one is labelled as **Assertion A** and other is labelled as **Reason** R

Assertion A: Steel is used in the construction of buildings and bridges.

Reason R: Steel is more elastic and its elastic limit is high.

In the light of above statements, choose the most appropriate answer from the given below

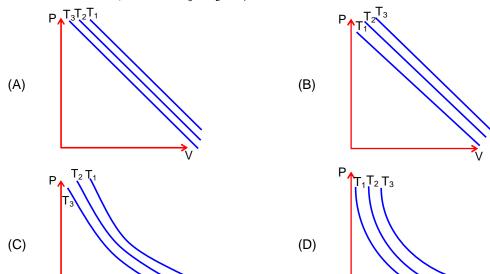
- (A) Both A and R are correct and R is the correct explanation of A
- (B) Both A and R are correct but R is NOT the correct explanation of A
- (C) A is not correct but R is correct

Ω1

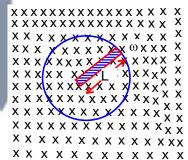
- (D) A is correct but R is not correct
- **Q4.** When a beam of white light is allowed to pass through convex lens parallel to principal axis, the different colours of light converge at different point on the principle axis after refraction. This is called:

(A) Scattering (B) Spherical aberration (C) Polarisation (D) Chromatic aberration

Q5. In an Isothermal change, the change in pressure and volume of a gas can be represented for three different temperature : $T_3 > T_2 > T_1$ as :



Q6. An metallic rod of length 'L' is rotated with an angular speed of 'w' normal to a uniform magnetic field 'B' about an axis passing through one end of rod as shown in figure. The induced emf will be:



(A)
$$\frac{1}{2}BL^2\omega$$

(B)
$$\frac{1}{4}BL^2\omega$$

(C)
$$\frac{1}{4}$$
B²L α

(D)
$$\frac{1}{2}B^2L^2\omega$$

If two vectors $\vec{P} = \hat{i} + 2m\hat{j} + m\hat{k}$ and $\vec{Q} = 4\hat{i} - 2\hat{j} + m\hat{k}$ are perpendicular to each other. Then, the Q7. value of m will be:

$$(A) -1$$

Q8. Given below are two statements: one is labelled as Assertion A and the other is labelled as Reason R.

Assertion A: A pendulum clock when taken to Mount Everest becomes fast.

Reason R: The value of g (acceleration due to gravity) is less at Mount Everest than its value on the surface of earth.

In the light of the above statements, choose the most appropriate answer from the options given below

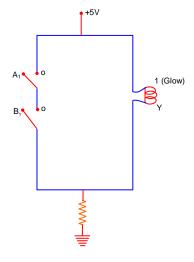
- (A) A is correct but R is not correct
- (B) A is not correct but R is correct
- (C) Both A and R are correct and R is the correct explanation of A
- (D) Both A and R are correct but R is NOT the correct explanation of A

- Q9. An a -particle, a proton and an electron have the same kinetic energy. Which one of the following is correct in case of their de-Broglie wavelength:
 - (A) $\lambda_{\alpha} < \lambda_{p} < \lambda_{e}$

(B) $\lambda_a > \lambda_p < \lambda_e$

(C) $\lambda_{\alpha} = \lambda_{p} = \lambda_{e}$

- (D) $\lambda_{\alpha} > \lambda_{\alpha} > \lambda_{\alpha}$
- Q10. The logic gate equivalent to the given circuit diagram is:
 - (A) OR
 - (B) NOR
 - (C) NAND
 - (D) AND



The electric potential at the centre of two concentric half Q11. rings of radii R₁ and R₂, having same linear charge density λ is:

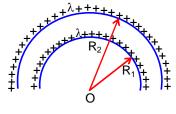


(C)
$$\frac{\lambda}{\epsilon_0}$$

$$\sum \frac{\lambda}{\epsilon_0}$$

(B)
$$\frac{2\lambda}{\epsilon_0}$$

$$(D) \frac{\lambda}{2 \in_{0}}$$



- Q12. A cell of emf 90V is connected across series combination of two resistors each of 100Ω resistance. A voltmeter of resistance 400Ω is used to measure the potential difference across each resistor. The reading of the voltmeter will be:
 - (A) 40 V

(B) 80 V

(C) 90 V

- (D) 45 V
- Q13. A body of mass 200g is tied to a spring constant 12.5 N/m, while the other end of spring is fixed at point O. If the body moves about O in a circular path on a smooth horizontal surface with constant angular speed 5 rad/s. Then the ratio of extension in the spring to its natural length will be:
 - (A) 2:5

(B) 1 : 1

(C) 1:2

- (D) 2:3
- Q14. The frequency (v) of an oscillating liquid drop may depend upon radius (r) of the drop, density (ρ) of liquid and the surface tension (s) of the liquid as $: v = r^a \rho^b s^c$. The value of a, b, c respectively are
 - (A) $\left(\frac{3}{2}, \frac{1}{2}, -\frac{1}{2}\right)$

(B) $\left(-\frac{3}{2}, -\frac{1}{2}, \frac{1}{2}\right)$

(C) $\left(-\frac{3}{2}, \frac{1}{2}, \frac{1}{2}\right)$

(D) $\left(\frac{3}{2}, -\frac{1}{2}, \frac{1}{2}\right)$

Q15. Given below are two statements:

Statement I: Acceleration due to earth's gravity decreases as you go 'up' or 'down' from earth's surface

Statement II: Acceleration due to earth's gravity is same at a height 'h' and depth 'd' from earth's surface, if h = d.

In the light of above statements, choose the most appropriate answer from the options given below

- (A) Statement I is incorrect but statement II is correct
- (B) Both Statement I and Statement II are incorrect
- (C) Statement I is correct but statement II is incorrect
- (D) Both Statement I and II are correct
- **Q16.** The electric field and magnetic field components of an electromagnetic wave going through vacuum is described by

$$E_x = E_o \sin(kz - \omega t)$$

$$B_v = B_o \sin(kz - \omega t)$$

Then the correct relation Eo and Bo is given by

(A)
$$E_0 B_0 = \omega k$$

(B)
$$\omega E_0 = kB_0$$

(C)
$$E_0 = kB_0$$

(D)
$$kE_0 = \omega B_0$$

Q17. A photon is emitted in transition from n = 4 to n = 1 level in hydrogen atom.

The corresponding wavelength for this transition is (given, $h = 4 \times 10^{-15} \, \text{eVs}$):

(A) 94.1 nm

(B) 974 nm

(C) 99.3 nm

(D) 941 nm

Q18. Match List I with List II

List - I

List – II I. 88 – 108 MHz

A. AM Broadcast

II. 540 – 1600 kHz

B. FM Broadcast

III. 3.7 – 4.2 GHz

C. TelevisionD. Satellite Communication

IV. 54 MHz – 890 MHz

Choose the correct answer from the options given below:

(A) A-IV, B-III, C-I, D-II

(B) A-II, B-III, C-I, D-IV

(C) A-II, B-I, C-IV, D-III

- (D) A-I, B-III, C-II, D-IV
- **Q19.** A long solenoid is formed by winding 70 turns cm⁻¹. If 2.0A current flows, then magnetic field produced inside the solenoid is $\mu_0 = 4\pi \times 10^{-7} \, \text{TmA}^{-1}$
 - (A) 176×10^{-4} T

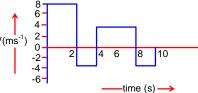
(B) 88×10^{-4} T

(C) 352×10^{-4} T

- (D) 1232×10^{-4} T
- **Q20.** The velocity time graph of body moving in a straight line is shown in figure.

The ratio of displacement to distance travelled by the body in time 0 to 10s is :





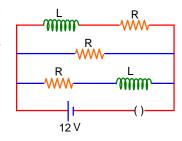
- (A) 1:1
- (B) 1:4
- (C) 1:3
- (D) 1:2

SECTION - B

(Numerical Answer Type)

This section contains **10** Numerical based questions. The answer to each question is rounded off to the nearest integer value.

Q1. Three identical resistors with resistance $R = 12\Omega$ and two identical inductors with self inductance L = 5 mH are connected to an ideal battery with emf of 12 V shown in figure. The current through the battery long after the switch has been closed will be ______ A.



- Q2. A parallel plate capacitor with air between the plate has a capacitance of 15pF. The separation between the plate become twice and the space between them is filled with a medium of dielectric constant 3.5. Then the capacitance becomes $\frac{x}{4}$ pF. The value of x is _____.
- Q3. A Spherical ball of radius 1mm and density 10.5g/cc is dropped in glycerine of coefficient of viscosity 9.8 poise and density 1.5 g/cc. Viscous force on the ball when it attains constant velocity is 3696×10^{-x} N. The value of x is (Given, g = 9.8 m/s² and $\pi = \frac{22}{7}$)
- Q4. A uniform solid cylinder with radius R and length L has moment inertia I_1 , about the axis of the cylinder. A concentric solid cylinder of radius $R' = \frac{R}{2}$ and length $L' = \frac{L}{2}$ is carved out of the original cylinder. If I_2 is the moment of inertia of the carved out portion of the cylinder then $\frac{I_1}{I_2}$ = (Both I_1 and I_2 are about the axis of the cylinder)
- Q5. A convex lens of refractive index 1.5 and focal length 18cm in air is immersed in water. The change of focal length of the lens will be _____cm.

 (Given refractive index of water = $\frac{4}{3}$)
- **Q6.** A body of mass 1kg begins to move under the action of a time dependent force $\vec{F} = (t\hat{i} + 3t^2\hat{j})N$, where \hat{i} and \hat{j} are the unit vectors along x and y axis. The power developed by above force, at the time t = 2s, will be ______W.
- Q7. If a copper wire is stretched to increase its length by 20%. The percentage increase in resistance of the wire is _____%.
- Q8. A single turn current loop in the shape of a right angle triangle with sides 5cm, 12cm, 13cm is carrying a current of 2A. The loop is in a uniform magnetic field of magnitude 0.75 T whose direction is parallel to the current in the 13cm side of the loop. The magnitude of the magnetic force on the 5cm side will be $\frac{x}{130}$ N. The value of x is _____.

- **Q9.** The energy released per fission of nucleus of 240 X is 200 MeV. The energy released if all the atoms in 120g of pure 240 X undergo fission is _____x10 25 MeV.
- Q10. A mass m attached to free end of a spring executes SHM with a period of 1s. If the mass is increased by 3kg the period of oscillation increases by one second, the value of mass m is ____kg.



PART - B (CHEMISTRY)

SECTION - A

(One Options Correct Type)

This section contains **20 multiple choice questions**. Each question has **four choices** (A), (B), (C) and (D), out of which **ONLY ONE** option is correct.

Q1. The number of s-electrons present in an ion with 55 protons in its unipositive state is

(A) 8

(B) 9

(C) 12

(D) 10

Q2. K₂Cr₂O₇ paper acidified with dilute H₂SO₄ turns green when exposed to

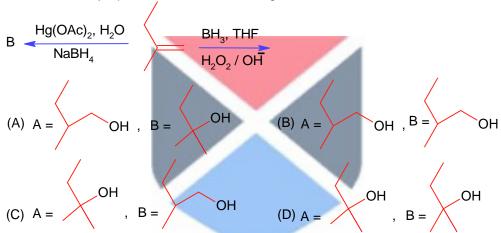
(A) Hydrogen sulphide

(B) Sulphur trioxide

(C) Carbon dioxide

(D) Sulphur dioxide

Q3. Find out the major products from the following reactions.



- **Q4.** Identify the correct statements about alkali metals.
 - A. The order of standard reduction potential ($M^{\dagger}|M$) for alkali metal ions is Na > Rb > Li.
 - B. Csl is highly soluble in water.
 - C. Lithium carbonate is highly stable to heat.
 - D. Potassium dissolved in concentrated liquid ammonia is blue in colour and paramagnetic.
 - E. All the alkali metal hydrides are ionic solids.

Choose the correct answer from the options given below:

(A) C and E only

(B) A, B and E only

(C) A and E only

(D) A, B, D only

Q5. What is the number of unpaired electron(s) in the highest occupied molecular orbital of following species: N₂; N₂⁺; O₂; O₂⁺?

(A) 0,1,2,1

(B) 2,1,2,1

(C) 2,1,0,1

(D) 0,1,0,1

Q6. Which one amongst the following are good oxidizing agents?

A. Sm²⁺

- B. Ce²⁺
- C. Ce⁴⁺
- D. Tb⁴⁺

Choose the most appropriate answer from the options given below:

(A) C only

(B) D only

(C) C & D only

- (D) A & B only
- **Q7.** Which of the following cannot be explained by crystal field theory?
 - (A) The order of spectrochemical series
 - (B) Colour of metal complexes
 - (C) Stability of metal complexes
 - (D) Magnetic properties of transition metal complexes
- **Q8.** Given below are two statements:

Statement I: Pure Aniline and other arylamines are usually colourless.

Statement II: Arylamines get coloured on storage due to atmospheric reduction

In the light of the above statements, choose the most appropriate answer from the options given below:

- (A) Both Statement I and Statement II are correct
- (B) Statement I is correct but Statement II is incorrect
- (C) Statement I is incorrect but Statement II is correct
- (D) Both statement I and Statement II are incorrect
- **Q9.** The metal which is extracted by oxidation and subsequent reduction from its ore is:
 - (A) Cu
 - (C) Al

- (B) Fe
- (D) Ag
- Q10. Given below are two statements:



In the light of the above statements, choose the correct answer from the options given below:

- (A) Both Statement I and Statement II are false
- (B) Statement I is false but Statement II is true
- (C) Statement I is true but Statement II is false
- (D) Both Statement I and Statement II are true
- Q11. Correct statement is:
 - (A) An average human being consumes 100 times more air than food
 - (B) An average human being consumes more food than air
 - (C) An average human being consumes equal amount of food and air
 - (D) An average human being consumes nearly 15 times more air than food
- **Q12.** In which of the following reactions the hydrogen peroxide acts as a reducing agent?
 - (A) $Mn^{2+} + H_2O_2 \rightarrow Mn^{4+} + 2OH^{-}$
 - (B) PbS + $4H_2O_2 \rightarrow PbSO_4 + 4H_2O$
 - (C) $2Fe^{2+} H_2O_2 \rightarrow 2Fe^{3+} + 2OH^{-}$
 - (D) HOCl + $H_2O_2 \rightarrow H_3O^+ + Cl^- + O_2$

Q13. Which will undergo deprotonation most readily in basic medium?

Q14. Given below are two statements, one is labelled as Assertion A and the other is labelled as Reason R.

Assertion A: Benzene is more stable than hypothetical cyclohexatriene

Reason R: The delocalized π electron cloud is attracted more strongly by nuclei of carbon atoms. In the light of the above statements, choose the correct answer from the options given below:

- (A) A is true but R is false
- (B) Both A and R are correct but R is NOT the correct explanation of A
- (C) Both A and R are correct and R is the correct explanation of A
- (D) A is false but R is true
- **Q15.** A student has studied the decomposition of a gas AB₃ at 25°C. He obtained the following data.

| P(mm Hg) | 50 | 100 | 200 | 400 |
|-------------------------------|----|-----|-----|-----|
| Relative t _{1/2} (s) | 4 | 2 | 1 | 0.5 |

The order of the reaction is

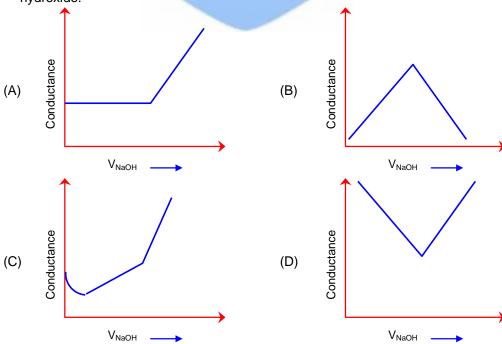
- (A) 0.5
- (C) 1

- (B) 0 (zero)
- (D) 2
- Q16. The hybridization and magnetic behaviour of cobalt ion in [Co(NH₃)₆]³⁺ complex, respectively is
 - (A) d²sp³ and diamagnetic

(B) sp³d² and paramagnetic

(C) sp³d² and diamagnetic

- (D) d²sp³ and paramagnetic
- **Q17.** Choose the correct representation of conductometric titration of benzoic acid vs sodium hydroxide.



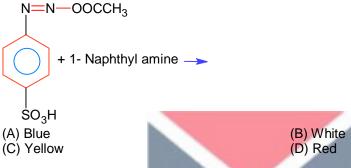
Q18. Given below are two statements, one is labelled as Assertion A and the other is labelled as Reason R.

Assertion A: Beryllium has less negative value of reduction potential compared to the other alkaline earth metals.

Reason R: Beryllium has large hydration energy due to small size of Be²⁺ but relatively large value of atomization enthalpy

In the light of the above statements, choose the most appropriate answer from the options given below

- (A) Both A and R are correct and R is the correct explanation of A
- (B) Both A and R are correct but R is NOT the correct explanation of A
- (C) A is true but R is not correct
- (D) A is not correct but R is correct
- **Q19.** Choose the correct colour of the product for the following reaction.



Q20. Match List I with List II

| | List-I (Type) | | | List (Name) |
|----|--------------------|-----|------|---------------|
| A. | Antifertility drug | 100 | _ | Norethindrone |
| B. | Tranquilizer | | II. | Meprobomate |
| C. | Antihistamine | | III. | Seldane |
| D. | Antibiotic | | IV. | Ampicillin |

Choose the correct answer from the options given below:

(A) A- IV, B-III, C-II, D- I

(B) A-I, B-II, C-III, D-IV

(C) A-I, B-III, C-II, D-IV

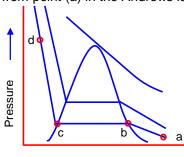
(D) A-II, B-I, C-III, D-IV

SECTION - B

(Numerical Answer Type)

This section contains **10** Numerical based questions. The answer to each question is rounded off to the nearest integer value.

Q1. The number of statement/s, which are **correct** with respect to the compression of carbon dioxide from point (a) in the Andrews isotherm from the following is



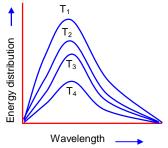
- Volume ____
- A. Carbon dioxide remains as a gas upto point (b)
- B. Liquid carbon dioxide appears at point (c)
- C. Liquid and gaseous carbon dioxide coexist between points (b) and (c)
- D. As the volume decreases from (b) to (c), the amount of liquid decreases
- **Q2.** Maximum number of isomeric monochloro derivatives which can be obtained from 2,2,5,5-tetrametylhexane by chlorination is______
- Q3. The number of units which are used to express concentration of solution from the following is ______.

 Mass percent, Mole, Mole fraction, Molarity, ppm, Molality
- Q4. The number of statement/s which are the characteristics of physisorption is______.
 - A. It is highly specific in nature
 - B. Enthalpy of adsorption is high
 - C. It decreases with increase in temperature
 - D. It results into unimolecular layer
 - E. No activation energy is needed
- **Q5.** Sum of π -bonds present in peroxodisulphuric acid and pyrosulphuric acid is______.
- Q6. The total pressure observed by mixing two liquids A and B is 350 mm Hg when their mole fraction are 0.7 and 0.3 respectively.

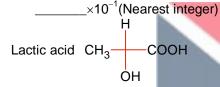
 The total pressure becomes 410 mm Hg if the mole fractions are changed to 0.2 and 0.8

The total pressure becomes 410 mm Hg if the mole fractions are changed to 0.2 and 0.8 respectively for A and B. The vapour pressure of pure A is _____mm Hg. (Nearest integer). Consider the liquids and solutions behave ideally.

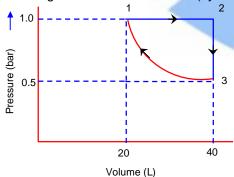
Q7. Following figure shows spectrum of an ideal black body at four different temperatures. The number of **correct** statement/s from the following is_____.



- A. $T_4 > T_3 > T_2 > T_1$
- B. The black body consists of particles performing simple harmonic motion.
- C. The peak of the spectrum shifts to shorter wavelength as temperature increases.
- $D. \ \frac{T_1}{\nu_1} = \frac{T_2}{\nu_2} = \frac{T_3}{\nu_3} \neq \ constant$
- E. The given spectrum could be explained using quantisation of energy
- Q8. If the pKa of lactic acid is 5, then the pH of 0.005 M calcium lactate solution at 25°C is



- Q9. Total number of tripeptides possible by mixing of valine and proline is_____
- Q10. One mole of an ideal monoatomic gas is subjected to changes as shown in the grap. The magnitude of the work done (by the system or on the system) is_____ J (nearest integer)



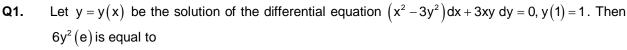
Given: log 2 = 0.3ln 10 = 2.3

PART - C (MATHEMATICS)

SECTION - A

(One Options Correct Type)

This section contains 20 multiple choice questions. Each question has four choices (A), (B), (C) and (D), out of which ONLY ONE option is correct.



(A)
$$\frac{3}{2}e^{2}$$

Q2. The number of real solutions of the equation
$$3\left(x^2 + \frac{1}{x^2}\right) - 2\left(x + \frac{1}{x}\right) + 5 = 0$$
, is

Q3. Let
$$f(x)$$
 be a function such that $f(x+y)=f(x)\cdot f(y)$ for all $x,y\in N$. If $f(1)=3$ and $\sum_{k=1}^n f(k)=3279$, then the value of n is

$$x + 2y + 3z = 3$$

$$4x + 3y - 4z = 4$$

$$8x + 4y - \lambda z = 9 + \mu$$

has infinitely many solutions, then the ordered pair (λ, μ) is equal to :

(A)
$$\left(-\frac{72}{5} \cdot -\frac{21}{5}\right)$$

(B)
$$\left(\frac{72}{5}, -\frac{21}{5}\right)$$

(C)
$$\left(\frac{72}{5}, \frac{21}{5}\right)$$

$$(D)\left(-\frac{72}{5},\frac{21}{5}\right)$$

(A) 48

(B) 168

(C) 120

(D) 220

Q6. The locus of the mid points of the chords of the circle
$$C_1$$
: $\left(x-4\right)^2+\left(y-5\right)^2=4$ which subtend an angle θ_1 at the centre of the circle C_1 , is a circle of radius r_1 . If $\theta_1=\frac{\pi}{3}$, $\theta_3=\frac{2\pi}{3}$ and $r_1^2=r_2^2+r_3^2$, then θ_2 is equal to

(A)
$$\frac{3\pi}{4}$$

(B)
$$\frac{\pi}{6}$$

(C)
$$\frac{\pi}{4}$$

(D)
$$\frac{\pi}{2}$$

Q7. If
$$f(x) = x^3 - x^2 f'(1) + x f''(2) - f'''(3)$$
, $x \in R$, then

(A)
$$2f(0)-f(1)+f(3)=f(2)$$

(B)
$$f(3)-f(2)=f(1)$$

(C)
$$3f(1) + f(2) = f(3)$$

(D)
$$f(1) + f(2) + f(3) = f(0)$$

$$\text{Q8.} \qquad \text{If } \left(\, ^{30}\text{C}_{_1} \right)^2 + 2 \Big(\, ^{30}\text{C}_{_2} \, \Big)^2 + 3 \Big(\, ^{30}\text{C}_{_3} \, \Big)^2 + \ldots + 30 \Big(\, ^{30}\text{C}_{_{30}} \, \Big)^2 = \frac{\alpha 60!}{\big(30! \big)^2} \, \text{then } \, \alpha \, \text{is equal to} : \, \frac{1}{30!} \, \frac{1}{$$

Q9. Let the plane containing the line of intersection of the planes P1: $x + (\lambda + 4)y + z = 1$ and P2: 2x + y + z = 2 pass through the points (0,1,0) and (1,0,1). Then the distance of the point $(2\lambda,\lambda,-\lambda)$ from the plane P2 is

(A)
$$2\sqrt{6}$$

(B)
$$5\sqrt{6}$$

(C)
$$3\sqrt{6}$$

(D)
$$4\sqrt{6}$$

Q10. Let the six numbers $a_1, a_2, a_3, a_4, a_5, a_6$, be in A.P. and $a_1 + a_3 = 10$. If the mean of these six numbers is $\frac{19}{2}$ and their variance is σ^2 , then $8\sigma^2$ is equal to :

Let p and q be two statements. Then $\sim (p \land (p \Rightarrow \sim q))$ is equivalent to Q11.

(A)
$$p \lor (p \land q)$$

(B)
$$p \vee (p \wedge (\sim q))$$

(C)
$$(\sim p) \vee q$$

(D)
$$p \lor ((\sim p) \land q)$$

The set of all values of a for which $\lim_{x\to a} ([x-5]-[2x+2]) = 0$, where $[\alpha]$ denotes the greatest Q12. integer less than or equal to α is equal to

(A)
$$(-7.5, -6.5]$$

(B)
$$[-7.5, -6.5]$$

(C)
$$(-7.5, -6.5)$$

(D)
$$[-7.5, -6.5]$$

$$\textbf{Q13.} \qquad \text{If } \ f\left(x\right) = \frac{2^{2x}}{2^{2x}+2}, \ x \in R \ , \ \text{then } \ f\left(\frac{1}{2023}\right) + f\left(\frac{2}{2023}\right) + \ldots + f\left(\frac{2022}{2023}\right) \text{is equal to}$$

(C) 2011

(D) 2010

The equations of the sides AB and AC of a triangle ABC are $(\lambda + 1)x + \lambda y = 4$ and Q14. $\lambda x + (1 - \lambda)y + \lambda = 0$ respectively. Its vertex A is on the y-axis and its orthocentre is (1,2). The length of the tangent from the point C to the part of the parabola $y^2 = 6x$ in the first quadrant is:

(A) $2\sqrt{2}$

(B) 2

(C) $\sqrt{6}$

(D) 4

Q15. The value of
$$\left(\frac{1+\sin\frac{2\pi}{9}+i\cos\frac{2\pi}{9}}{1+\sin\frac{2\pi}{9}-i\cos\frac{2\pi}{9}}\right)^3$$
 is

(A)
$$\frac{1}{2} (1 - i\sqrt{3})$$

(B)
$$-\frac{1}{2}(1-i\sqrt{3})$$

(C)
$$\frac{1}{2}(\sqrt{3}+i)$$

(D)
$$-\frac{1}{2}(\sqrt{3}-i)$$

Let $\vec{\alpha}=4\hat{i}+3\hat{j}+5\hat{k}$ and $\vec{\beta}=\hat{i}+2\hat{j}-4\hat{k}$. Let $\vec{\beta}_1$ be parallel to $\vec{\alpha}$ and $\vec{\beta}_2$ be perpendicular to $\vec{\alpha}$. If Q16. $\vec{\beta}=\vec{\beta}_1+\vec{\beta}_2$, then the value of $\,5\vec{\beta}_2\cdot\left(\hat{i}+\hat{j}+\hat{k}\right)$ is

Q17. $\int_{\frac{3\sqrt{3}}{4}}^{\frac{3\sqrt{3}}{4}} \frac{48}{\sqrt{9-4x^2}} dx \text{ is equal to}$

(A)
$$\frac{\pi}{3}$$

(C)
$$\frac{\pi}{2}$$

(D)
$$\frac{\pi}{6}$$

Let A be a 3 x 3 matrix such that $\left| adj \left(adj \left(adj \left(A \right) \right) \right| = 12^4$. Then $\left| A^{-1} \ adj A \right|$ is equal to Q18.

(A)
$$2\sqrt{3}$$

(C)
$$\sqrt{6}$$

If the foot of the perpendicular drawn from (1,9,7) to the line passing through the point (3,2,1) and Q19. parallel to the planes x + 2y + z = 0 and 3y - z = 3 is (α, β, γ) , then $\alpha + \beta + \gamma$ is equal to

(A) 1

(C) 5

(D) -1

The number of square matrices of order 5 with entries from the set {0,1}, such that the sum of all Q20. the elements in each row is 1 and the sum of all the elements in each column is also 1, is

(A) 120

(B) 125

(C) 225

(D) 150

SECTION - B

(Numerical Answer Type)

This section contains 10 Numerical based questions. The answer to each question is rounded off to the nearest integer value.

$$\textbf{Q1.} \qquad \text{Let } S = \left\{\theta \in \left[0, 2\pi\right) : tan\left(\pi\cos\theta\right) + tan\left(\pi\sin\theta\right) = 0\right\} \text{ . Then } \sum_{\theta \in s} sin^2\left(\theta + \frac{\pi}{4}\right) \text{is equal to}......$$

- **Q2.** The minimum number of elements that must be added to the relation $R = \{(a,b), (b,c), (b,d)\}$ on the set $\{a,b,c,d\}$ so that it is an equivalence relation, is......
- Q3. The equations of the sides AB, BC and CA of a triangle ABC are : 2x + y = 0, x + py = 21a, $(a \ne 0)$ and x y = 3 respectively. Let P(2,a) be the centroid of $\triangle ABC$. Then $(BC)^2$ is equal to
- **Q4.** If $\frac{1^3 + 2^3 + 3^3 + ... \text{up to n terms}}{1 \cdot 3 + 2 \cdot 5 + 3 \cdot 7 + ... \text{up to n terms}} = \frac{9}{5}$, then the value of n is
- **Q5.** Let f be a differentiable function defined on $\left[0,\frac{\pi}{2}\right]$ such that f(x) > 0 and $f(x) + \int_0^x f(t) \sqrt{1 \left(\log_e f(t)\right)^2} \, dt = e$, $\forall x \in \left[0,\frac{\pi}{2}\right]$. Then $\left(6\log_e f\left(\frac{\pi}{6}\right)\right)^2$ is equal to......
- Q6. If the shortest between the lines $\frac{x+\sqrt{6}}{2} = \frac{y-\sqrt{6}}{3} = \frac{z-\sqrt{6}}{4} \text{ and } \frac{x-\lambda}{3} = \frac{y-2\sqrt{6}}{4} = \frac{z+2\sqrt{6}}{5} \text{ is } 6, \text{ then the square of sum of all possible values of } \lambda \text{ is}$
- **Q7.** If the area of the region bounded by the curves $y^2 2y = -x$, x + y = 0 is A, then 8A is equal to
- Q8. Three urns A, B and C contain 4 red, 6 black; 5 red, 5 black; and λ red, 4 black balls respectively. One of the urns is selected at random and a ball is drawn. If the ball drawn is red and the probability that it is drawn from urn C is 0.4 then the square of the length of the side of the largest equilateral triangle, inscribed in the parabola $y^2 = \lambda x$ with one vertex at the vertex of the parabola, is
- **Q9.** Let the sum of the coefficients of the first three terms in the expansion of $\left(x \frac{3}{x^2}\right)^n$, $x \ne 0$, $n \in \mathbb{N}$, be 376. Then the coefficient of x^4 is.....
- **Q10.** Let $\vec{a} = \hat{i} + 2\hat{j} + \lambda \hat{k}$, $\vec{b} = 3\hat{i} 5\hat{j} \lambda \hat{k}$, $\vec{a} \cdot \vec{c} = 7, 2\vec{b} \cdot \vec{c} + 43 = 0$, $\vec{a} \times \vec{c} = \vec{b} \times \vec{c}$. Then $|\vec{a} \cdot \vec{b}|$ is equal to

Keys to JEE Main 2024 Mock Test 6

PART - A (PHYSICS)

SECTION - A

| 1. | В | 2. | С | 3. | A | 4. | D |
|----|---|-----|---|-----|---|-----|---|
| 5. | D | 6. | Α | 7. | В | 8. | В |
| 9. | Α | 10. | С | 11. | D | 12. | Α |

13. D 14. B 15. C 16. D 17. A 18. C 19. A 20. C

SECTION - B

| 1. | 3 | 2. | 105 | 3. 7 | 4. | 32 |
|----|----|----|-----|-------|----|----|
| 5. | 54 | 6. | 100 | 7. 44 | 8. | 9 |

9. 6 10. 1

PART - B (CHEMISTRY)

SECTION - A

| 1. | D | 2. | D | 3. | Α | 4. | С |
|-----|---|-----|---|-----|---|-----|---|
| 5. | Α | 6. | С | 7. | Α | 8. | В |
| 9. | D | 10. | С | 11. | D | 12. | D |
| 13. | В | 14. | С | 15. | D | 16. | Α |
| 17. | С | 18 | Α | 19. | D | 20. | В |

SECTION - B

| 1. | 2 | 2. | 3 | 3. | 5 | 4. | 2 |
|----|---|-----|-----|----|---|----|----|
| 5. | 8 | 6. | 314 | 7. | 2 | 8. | 85 |
| 9. | 8 | 10. | 620 | | | | |

PART - C (MATHEMATICS)

SECTION - A

1. D 5. В 9. С 13.

В 17. В

2. В 6.

D С 10. 14. Α

18

3. В 7. Α

С 11. 15. D 19.

29

36

С 12. 16. Α 20. Α

В

Α

4.

8.

SECTION - B

2 1. 5. 27 2. 13 6.

384

3. 7. 4. 5 432 8.

9. 405 10. 8

