

## Question 1

**During the phenomenon of resonance**

**Options:**

- A. the amplitude of oscillation becomes large**
- B. the frequency of oscillation becomes large**
- C. the time period of oscillation becomes large**
- D. All of the above**

**Answer: A**

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## Question 2

**If the earth were to spin faster, acceleration due to gravity at the poles**

**Options:**

- A. increases**
- B. decreases**
- C. remains the same**
- D. depends on how fast it spins**

**Answer: C**

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## Question 3

**Maximum amplitude of message signal in amplitude modulation is 20 cm. If the amplitude of carrier wave is 40 cm, then modulation index of modulated wave is**

**Options:**

- A. 1**
- B. 0.5**
- C. 0.25**
- D. 2**

**Answer: B**

**Solution:**

Solution:

Given,

$$A_m = 20\text{cm}$$

$$A_c = 40\text{cm}$$

∴ Modulation index,

$$\mu = \frac{A_m}{A_c} = \frac{20}{40} = 0.5$$

## Question 4

**If heat engine is filled at temperature 27°C and heat of 100kcal is taken from source at temperature 677°C. Work done (in J) is**

**Options:**

- A.  $0.28 \times 10^6$**
- B.  $2.8 \times 10^6$**
- C.  $28 \times 10^6$**
- D.  $0.028 \times 10^6$**

**Answer: A**

**Solution:**

Solution:

Given,

$$T_2 = 27^\circ\text{C} = 300\text{K}$$

$$T_1 = 677^\circ\text{C} = 950\text{K}$$

$$\begin{aligned} \eta &= \frac{W}{Q_1} = \frac{Q_1 - Q_2}{Q_1} \\ &= 1 - \frac{Q_2}{Q_1} = 1 - \frac{T_2}{T_1} \\ \therefore \eta &= 1 - \frac{300}{950} = \frac{13}{19} \end{aligned}$$

$$\therefore \eta W = \eta Q_1 = 100 \times 10^3 \times \frac{13}{19} \text{ cal}$$

Also,  $4.2 \text{ J} = 1 \text{ cal}$

$$\therefore W = 100 \times 10^3 \times \frac{13}{19} \times 4.2$$

$$\Rightarrow W = 2.87 \times 10^5 = 0.28 \times 10^6 \text{ J}$$

## Question 5

**During  $\alpha$ -decay, atomic mass of parent nuclei is**

**Options:**

- A. decreased by 2 units**
- B. increased by 2 units**
- C. decreased by 4 units**
- D. increased by 4 units**

**Answer: C**

**Solution:**

Solution:

During **alpha**-decay, atomic mass of parent nuclei is decreased by 4 units while atomic number is decreased by 2 units.

## Question 6

**A point object is placed on the optic axis of a convex lens of focal length  $f$  at a distance of  $2f$  to the left of it. The diameter of the lens is  $d$ . An eye is placed at a distance of  $3f$  to the right of the lens and a distance  $h$  below the optic axis. The maximum value of  $h$  to see the image is**

**Options:**

- A.  $d$**
- B.  $\frac{d}{2}$**
- C.  $\frac{d}{3}$**
- D.  $\frac{d}{4}$**

**Answer: D**

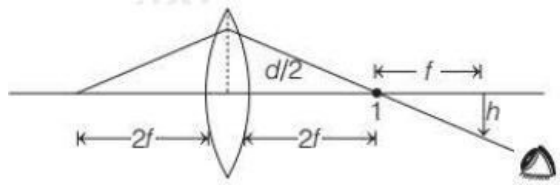
**Solution:**

Solution:

From two similar triangles,

$$\frac{h}{d/2} = \frac{f}{2f}$$

$$h = \frac{d}{4}$$



## Question 7

For CE transistor amplifier, the audio signal voltage across the collector resistance of  $4\text{k}\Omega$  is  $5\text{V}$ . If the current amplification factor of the transistor is 100 and base resistance is  $2\text{k}\Omega$ , then input signal voltage is

Options:

- A.  $75\text{ mV}$
- B.  $25\text{ mV}$
- C.  $20\text{ mV}$
- D.  $50\text{ mV}$

**Answer: B**

**Solution:**

Solution:

Given, collector resistance =  $R_{\text{out}} = 4\text{k}\Omega$

$\beta = 100$

$R_{\text{in}} = 2\text{k}\Omega$

$V_{\text{out}} = 5\text{V}$

$\therefore$  Voltage amplification,

$$A_v = \beta \frac{R_{\text{out}}}{R_{\text{in}}} = \frac{V_{\text{out}}}{V_{\text{in}}}$$

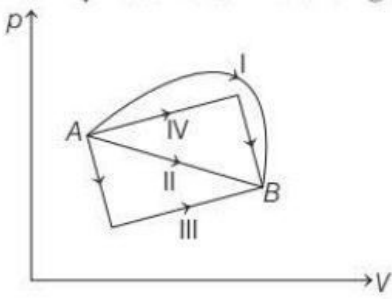
$$V_{\text{in}} = \frac{V_{\text{out}} \times R_{\text{in}}}{\beta \times R_{\text{out}}}$$

$$= \frac{5 \times 2 \times 10^3}{100 \times 4 \times 10^3}$$

$$= \frac{1}{40} = 25\text{mV}$$

## Question 8

From the following  $p - V$  diagram, an ideal gas undergoing a change of state from A to B. Four different processes I, II, III and IV as shown in the figure may lead to same change of stat



**Options:**

- A. Work done is maximum in case I**
- B. Change in internal energy is same in all the four cases**
- C. Change in internal energy is same in IV and III cases, but not in I and II**
- D. Work done is minimum in case II**

**Answer: 0**

**Solution:**

Solution:

(a, b) As work done = area under  $p - V$  curve, work done is maximum in case I. Change in internal energy is independent of the path from **A** to **B**. Therefore, in all cases change in internal energy is same.

## Question 9

**A copper and a steel wire of same diameter are connected end to end. A deforming force  $F_1$  is applied to the wire which causes an elongation of 1 cm. The two wires will have**

**Options:**

- A. the same stress**
- B. different stress**
- C. the same strain**
- D. different strain**

**Answer: 0**

**Solution:**

Solution:

(a, d) As Young's modulus  $Y$  for two wires is different, hence strain is different but stress is same as equal force  $F$  on each wire having same diameter and area of cross-section act on both wires.

## Question 10

**If kinetic energy of a body is increased by 300%, then percentage change in momentum will be**

**Options:**

**A. 100%**

**B. 150%**

**C. 265%**

**D. 73.2%**

**Answer: A**

**Solution:**

Solution:

$$\text{As, } K = \frac{1}{2}mv^2$$

$$\Rightarrow K = \frac{1}{2}mp^2$$

$$\Rightarrow p^2 = \frac{2mK}{1}$$

$$\Rightarrow p = \sqrt{2mK}$$

Suppose,  $p_1$  is the momentum of the body and  $K_1$  = kinetic energy of the body initially. As the kinetic energy of the body is increased by **300%**, new kinetic energy of the body =  $K_1 + 3K_1$

Hence, percentage change in momentum

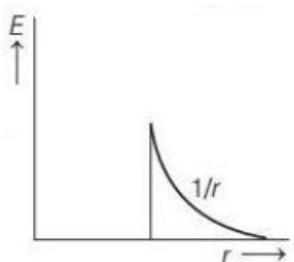
$$\begin{aligned} &= \frac{p_2 - p_1}{p_1} \times 100 \\ &= \frac{\sqrt{2mK_2} - \sqrt{2mK_1}}{\sqrt{2mK_1}} \times 100 \\ &= \frac{\sqrt{2m}(\sqrt{K_2} - \sqrt{K_1})}{\sqrt{2m}\sqrt{K_1}} \times 100 \\ &= \frac{\sqrt{K_1 + 3K_1} - \sqrt{K_1}}{\sqrt{K_1}} \times 100 \\ &= \frac{\sqrt{4K_1} - \sqrt{K_1}}{\sqrt{K_1}} \times 100 = 100\% \end{aligned}$$

## Question 11

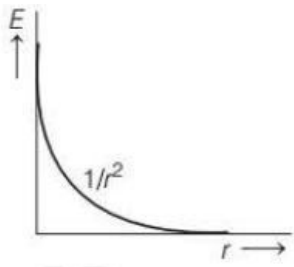
**Which of the following diagram represents the variation of the electric field with distance r from the centre of a uniformly charged non-conducting sphere of radius R ?**

**Options:**

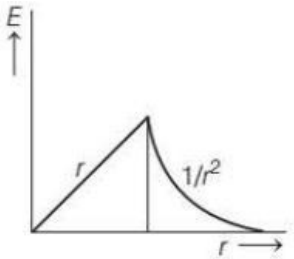
**A.**



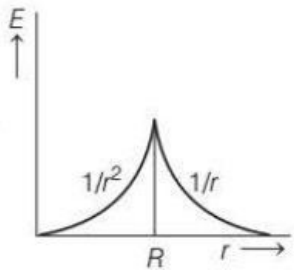
**B.**



C.



D.



**Answer: C**

**Solution:**

Solution:

The electric field intensity at a point lying outside the sphere (non-conducting) is

$$\mathbf{E} = \frac{1}{4\pi\epsilon_0} \cdot \frac{q}{r^2}$$

$$\Rightarrow \mathbf{E} \propto \frac{1}{r^2} \dots\dots\dots \text{(i)}$$

The electric field intensity at the sphere ( $r=R$ ),

$$\mathbf{E} = \frac{1}{4\pi\epsilon_0} \cdot \frac{q}{R^2}$$

$$\Rightarrow \mathbf{E} \propto \frac{1}{R^2}$$

where,  $\mathbf{R}$  being the radius of sphere.

The electric field intensity inside the sphere is

$$\mathbf{E} = \frac{1}{4\pi\epsilon_0} \cdot \frac{q}{R^3}$$

$$\Rightarrow \mathbf{E} \propto r$$

At the centre of sphere,  $\mathbf{E} = \mathbf{0}$

Hence, option (c) is correct representation.

## Question 12

A DC ammeter and a hot wire ammeter are connected to a circuit in series. When a direct current is passed through circuit, the DC ammeter shows 6A. When AC current flows through circuit, what is the average readings in DC ammeter and the AC ammeter, if DC and AC currents

**flow simultaneously through the circuit?**

**Options:**

**A. DC = 6A, AC = 10A**

**B. DC = 3A, AC = 5A**

**C. DC = 5A, AC = 8A**

**D. DC = 2A, AC = 3A**

**Answer: A**

**Solution:**

Solution:

Resultant current is superposition of two currents,  
i.e.  $I$  (instantaneous total current)

$$= 6 + I_0 \sin \omega t$$

DC ammeter will read average value

$$= 6 + I_0 \sin \omega t$$

$$= 6A (\because I_0 \sin \omega t = 0)$$

AC ammeter will read average value

$$= \sqrt{(6 + I_0 \sin^2 \omega t)^2}$$

$$= \sqrt{36 + 12I_0 \sin \omega t + I_0^2 \sin^2 \omega t} (\because I_0 \sin \omega t = 0)$$

$$\text{Since, } \sin^2 \omega t = \frac{1}{2} \text{ and } I_{\text{rms}} = 8 = \frac{I_0}{\sqrt{2}}$$

$$\therefore \text{AC reading} = \sqrt{36 + \frac{I_0^2}{2}} = \sqrt{36 + 64} \\ = 10A$$

## Question 13

**A bullet of mass  $m$  hits a mass  $M$  and gets embedded in it. If the block rises to a height  $h$  as a result of this collision, the velocity of the bullet before collision is**

**Options:**

**A.  $a \cdot v = \sqrt{2gh}$**

**B.  $v = \sqrt{2gh} \left[ 1 + \left( \frac{m}{M} \right) \right]$**

**C.  $v = \sqrt{2gh} \left( 1 + \sqrt{\frac{M}{m}} \right)$**

**D.  $v = \sqrt{2gh} \left[ 1 - \left( \frac{m}{M} \right) \right]$**

**Answer: C**

**Solution:**



**Solution:**

Let the velocity of the bullet before collision be  $\mathbf{v}$ , then according to law of conservation of linear momentum,

$$m\mathbf{v} = (m + M)\mathbf{v}' \dots\dots\dots (i)$$

As the mass  $m$  of the bullet gets embedded in the wall, hence velocity of bullet + target just after collision will be same,

$$\frac{1}{2}(M + m)v'^2 = (m + M)gh$$

$$\Rightarrow v' = \sqrt{2gh}$$

Putting the value of  $v'$  in Eq.(i), we get

$$\Rightarrow v = \sqrt{2gh} \frac{(m + M)}{m} = \sqrt{2gh} \left( 1 + \frac{M}{m} \right)$$

## Question 14

A particle of mass  $m$  is moving in a horizontal circle of radius  $r$  under a centripetal force given by  $\left( \frac{-K}{r^2} \right)$ , where  $K$  is a constant. Then

**Options:**

- A. the total energy of the particle is  $\left( \frac{-K}{2r} \right)$
- B. the kinetic energy of the particle is  $\left( \frac{K}{r} \right)$
- C. the potential energy of the particle is  $\left( \frac{K}{2r} \right)$
- D. the kinetic energy of the particle is  $\left( \frac{-K}{r} \right)$

**Answer: A**

**Solution:**

**Solution:**

The potential energy is given by

$$U = \int \mathbf{F} \cdot d\mathbf{r} = \int \frac{K}{r^2} d\mathbf{r} = K \int r^{-2} d\mathbf{r}$$

$$= K \left[ \frac{r^{-1}}{-1} \right] = \frac{-K}{r}$$

The kinetic energy is given by

$$K = \frac{1}{2}mv^2 = \frac{1}{2} \left( \frac{K}{r} \right) \left[ \because \frac{mv^2}{4} = \frac{K}{r^2} \right]$$

Total energy,  $E = U + K$

$$= -\frac{K}{r} + \frac{K}{2r} = \frac{-K}{2r}$$

## Question 15

The height at which the acceleration due to gravity becomes  $\frac{g}{16}$  (where,  $g$  = acceleration due to gravity on the surface of the earth) in terms of  $R$  is, if  $R$  is the radius of earth.

**Options:**

- A.  $2R$
- B.  $3R$
- C.  $\sqrt{2}R$
- D.  $\sqrt{3}R$

**Answer: B**

**Solution:**

Solution:

As, acceleration due to gravity at height  $h$ ,

$$g' = \frac{GM}{(R + h)^2}$$

$$\Rightarrow \frac{g}{16} = \frac{GM}{R^2} \left( \frac{R^2}{(R + h)^2} \right) = g \frac{R^2}{(R + h)^2} \left( \because g' = \frac{g}{16} \right)$$

$$\Rightarrow \frac{1}{4} = \frac{R}{R + h} \Rightarrow h = 3R$$

## Question 16

**Which of the following series spectrum of hydrogen atom lies in ultraviolet region?**

**Options:**

- A. Paschen series
- B. Brackett series
- C. Pfund series
- D. Lyman series

**Answer: D**

**Solution:**

Solution:

Lyman series lies in the ultraviolet region whereas Paschen, Brackett and Pfund series lie in the infrared region.

## Question 17

**Speed of electromagnetic wave in a medium having relative permittivity  $\epsilon_r$  and relative permeability  $\mu_r$  is (speed of light in air,  $c = 3 \times 10^8 \text{ m / s}$ )**

**Options:**

A.  $\sqrt{\frac{1}{\mu_r \epsilon_r}}$

B.  $\frac{c}{\sqrt{\mu_r \epsilon_r}}$

C.  $c \sqrt{\frac{\mu_r}{\epsilon_r}}$

D.  $\frac{c}{\mu_r \epsilon_r}$

**Answer: B**

**Solution:**

Solution:

Speed of EM wave in medium is given as

$$v = \frac{c}{\sqrt{\mu_r \epsilon_r}}$$


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## Question 18

**The wavelength of the second line of Balmer series is 486.4 nm. What is the wavelength of the first line of Lyman series?**

**Options:**

A. 78.8 nm

B. 121.6 nm

C. 418.2 nm

D. 610.5 nm

**Answer: B**

**Solution:**

Solution:

Wavelength in Balmer series for hydrogen are given by

$$\begin{aligned} \frac{1}{\lambda} &= R_H \left( \frac{1}{2^2} - \frac{1}{n^2} \right) \\ &= R_H \left( \frac{1}{4} - \frac{1}{n^2} \right), n = 3, 4, 5, \dots \end{aligned}$$

The second line in Balmer series corresponds to n=4

$$\text{Hence, } \frac{1}{\lambda_2} = R_H \left( \frac{1}{4} - \frac{1}{16} \right) = \frac{3R_H}{16}$$

$$\text{or, } \lambda_2 = \frac{16}{3R_H}$$

The wavelength of the first line (n=2) in Lyman series is

$$\frac{1}{\lambda_1} = R_H \left( \frac{1}{2^2} - \frac{1}{\infty} \right) = \frac{R_H}{4}$$

$$\text{or, } \lambda_1 = \frac{4}{R_H}$$

$$\therefore \frac{\lambda_1}{\lambda_2} = \frac{4}{3R_H} \times \frac{3R_H}{16} = \frac{1}{4}$$

$$\Rightarrow \lambda_1 = \frac{\lambda_2}{4} = \frac{486.4}{4} = 121.6 \text{ nm}$$

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## Question 19

A bat emitting an ultrasonic wave of frequency  $4.5 \times 10^4$  Hz at speed of 6m / s between two parallel walls. The two frequencies heard by the bat will be

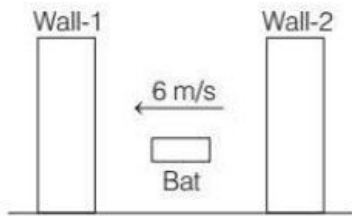
Options:

- A.  $4.67 \times 10^4$  Hz,  $4.34 \times 10^4$  Hz
- B.  $4.34 \times 10^4$  Hz,  $4.67 \times 10^4$  Hz
- C.  $4.5 \times 10^4$  Hz,  $5.4 \times 10^4$  Hz
- D.  $4.67 \times 10^3$  Hz,  $4.34 \times 10^4$  Hz

Answer: A

Solution:

Solution:



Frequency received by bat after reflection from wall - 1,

$$f_1 = f \left[ \frac{v+u}{v-u} \right] = 4.5 \times 10^4 \left[ \frac{330+6}{330-6} \right]$$

Given,  $f = 4.5 \times 10^4$  H Z

$$\Rightarrow f_1 = 4.67 \times 10^4 \text{ H Z}$$

Frequency received by bat after reflection from wall - 2

$$\begin{aligned} f_2 &= f \left[ \frac{v-u}{v+u} \right] \\ &= 4.5 \times 10^4 \left[ \frac{330-6}{330+6} \right] \\ &= 4.34 \times 10^4 \text{ H Z} \end{aligned}$$

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## Question 20

A disc of moment of inertia  $4 \text{ kg} - \text{m}^2$  revolving with  $16 \text{ rad} / \text{s}$  is placed on another disc of moment of inertia  $8 \text{ Kg} - \text{m}^2$  revolving  $4 \text{ rad} / \text{s}$ . The angular frequency of composite disc

Options:

- A.  $4 \text{ rad} / \text{s}$
- B.  $\frac{3}{16} \text{ rad} / \text{s}$
- C.  $8 \text{ rad} / \text{s}$

D.  $\frac{16}{3} \text{ rad/s}$

**Answer: C**

**Solution:**

Solution:

Given that, moment of inertia of disc,  $I_1 = 4 \text{ kg} - \text{m}^2$

$$I_2 = 8 \text{ kg} - \text{m}^2$$

Angular velocities of discs,

$$\omega_1 = 16 \text{ rad/s}$$

$$\omega_2 = 4 \text{ rad/s}$$

From angular momentum conservation principle,

$$I_1 \omega_1 + I_2 \omega_2 = (I_1 + I_2) \omega$$

$$\Rightarrow 4 \times 16 + 8 \times 4 = (4 + 8) \omega$$

$$\Rightarrow 64 + 32 = 12 \omega$$

$$\Rightarrow \omega = \frac{96}{12} = 8 \text{ rad/s}$$

## Question 21

An electric current  $I$  enters and leaves a uniform circular wire of radius  $r$  through diametrically opposite points. A charged particle  $q$  moves along the axis of circular wire passes through its centre with speed  $v$ . The magnetic force on the particle when it passes through the centre has a magnitude

Options:

A.  $\frac{qv\mu_0 I}{2\pi r}$

B.  $qv \frac{\mu_0 I}{\pi r}$

C.  $\frac{qv\mu_0 I}{r}$

D. 0

**Answer: D**

**Solution:**

Solution:

From a moving charged p[article in uniform magnetic field,

$$\mathbf{F} = \mathbf{B}q\mathbf{v}\sin\theta \dots\dots (i)$$

Since, charge particle moves along the axis of circular current carrying loop, therefore,  $\theta = 0^\circ \text{ or } 180^\circ$ .

When  $\theta = 0^\circ$ ,  $\mathbf{F} = \mathbf{B}q\mathbf{v}\sin 0^\circ$  [From Eq. (i)]

$$\mathbf{F} = \mathbf{0}$$

When  $\theta = 180^\circ$ ,  $\mathbf{F} = \mathbf{B}q\mathbf{v}\sin 180^\circ$

$$\mathbf{F} = \mathbf{0}$$

## Question 22

**Television frequencies are of the order of 100 MHz, while radio frequencies are of the order of 1 MHz. Using these as typical frequencies, the ratio of the emf generated in a loop antenna by a television wave to that generated by a radio wave, if both have equal electric field intensities.**

**Options:**

- A. 1**
- B. 10**
- C. 100**
- D. 66.6**

**Answer: C**

**Solution:**

Solution:

As we know that, emf induced  $\mathbf{e} = \frac{d\phi_B}{dt}$   
**ore**  $= \frac{dB}{dt}$  (When area is constant  $\phi_B \propto B$ )

Now for television wave,  $\mathbf{e}_1 = \frac{d}{dt}(B)$   
 $= \frac{d}{dt}(B \sin(2\pi f_1 t + \phi))$

$\mathbf{e}_1 = B_{01} 2\pi f_1 \cos(2\pi f_1 t + \phi)$

For radiowave,  $\mathbf{e}_2 = \frac{d}{dt}(B)$   
 $= \frac{d}{dt}(B \sin(2\pi f_2 t + \phi))$

The ratio of emf induced  
 $= \frac{e_1}{e_2} = \frac{B_{01} 2\pi f_1 \cos(2\pi f_1 t + \phi)}{B_{02} 2\pi f_2 \cos(2\pi f_2 t + \phi)}$

Since,  $f_1 = 100 \text{ MHz}$ ,  $f_2 = 1 \text{ MHz}$

and  $\cos(2\pi f_1 t + \phi) = \cos(2\pi f_2 t + \phi) = \cos\phi$  (For complete cycle)

We get,  $\frac{e_1}{e_2} = \frac{100}{1} = 100$

## Question 23

**A particle is performing simple harmonic motion. Equation of its motion**

**is  $x = 5\sin\left(4t - \frac{\pi}{6}\right)$ , x being the displacement from mean position.**

**Velocity (in  $\text{ms}^{-1}$ ) of the particle at the instant when its displacement is 3, will be**

**Options:**

- A.  $\frac{2\pi}{3}$**
- B.  $\frac{5\pi}{6}$**

C. 20

D. 16

**Answer: D**

**Solution:**

Solution:

According to the question,

$$x = 5\sin\left(4t - \frac{\pi}{6}\right)$$

When  $x = 3$

$$\Rightarrow \frac{3}{5} = \sin\left(4t - \frac{\pi}{6}\right)$$

$$\Rightarrow 4t - \frac{\pi}{6} = 37^\circ$$

$$\text{Hence, velocity} = \frac{dx}{dt} = 5 \times 4\cos\left(4t - \frac{\pi}{6}\right)$$

$$= 5 \times 4\cos\left(4t - \frac{\pi}{6}\right)$$

$$= 5 \times 4 \times \cos 37^\circ$$

$$= 16\text{ms}^{-1} \left( \because \cos 37^\circ = \frac{4}{5} \right)$$

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## Question 24

A raft of density  $600\text{g} / \text{m}^3$  and mass  $120\text{ kg}$  floats in water. How much weight can be put on the raft to make it just sink?

Options:

A. 120 kg

B. 200 kg

C. 40 kg

D. 80 kg

**Answer: D**

**Solution:**

Solution:

$$\text{Volume of wood} = \frac{\text{Mass}}{\text{Density}}$$

$$= \frac{120}{600} = 0.2\text{m}^3$$

Weight of displaced water,

$$vd\text{ g} = 0.2 \times 1000 \times 10 = 2000\text{N}$$

$$M\text{ g} = vd\text{ g}$$

$$\Rightarrow (120 + m)g = 2000$$

$$\Rightarrow m = 80\text{kg}$$

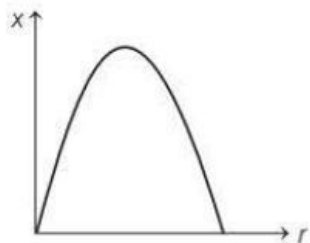
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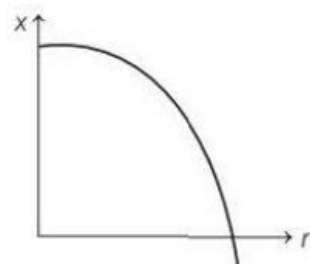
The displacement  $x$  of a particle in a straight line motion is given by  $x = 1 - t - t^2$ . The correct representation of the motion is

Options:

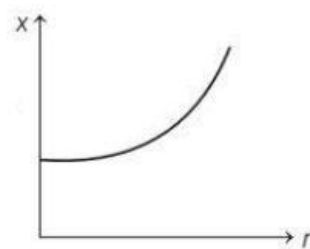
A.



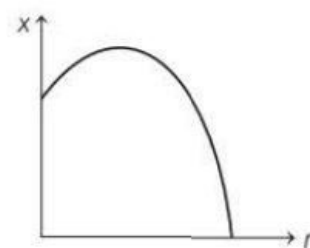
B.



C.



D.



**Answer: B**

**Solution:**

Solution:

If we differentiate the equation of motion,  
 $x = 1 - t - t^2$  w.r.t. time, we get velocity.

$$v = \frac{dx}{dt} = -1 - 2t$$

Comparing with  $v = u + at$ , we have  $u = -1 \text{ ms}^{-1}$  and  
 $a = -2 \text{ ms}^{-2}$

At  $t = 0$ ,  $x = 1 \text{ m}$ . Then,  $u$  and  $a$  both are negative.

Hence, x-coordinate of particle will go on decreasing.

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## Question 26

A galvanometer having a resistance of  $4\Omega$  is shunted by a wire of resistance  $2\Omega$ . If the total current is  $1.5\text{A}$ , the current passing through shunt is

Options:

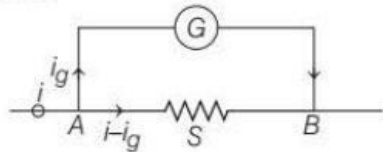
- A.  $1.25\text{A}$
- B.  $1\text{A}$
- C.  $0.75\text{A}$
- D.  $0.5\text{A}$

Answer: B

Solution:

Solution:

From figure,



Shunt current =  $i - i_g$

galvanometer current =  $i_g$

$i$  = total current

$\therefore i = 1.5\text{A}$

By KVL,

$$i_g - G = (i - i_g)S$$

Putting  $G = 4\Omega$  and  $S = 2\Omega$  and  $i = 1.5\text{A}$

$$\therefore i_g \times 4 = (1.5 - i_g) \times 2$$

$$4i_g = 3 - 2i_g$$

$$6i_g = 3 \Rightarrow i_g = 0.5\text{A}$$

$\therefore$  Current passing through shunt =  $i - i_g$

$$= 1.5 - 0.5 = 1\text{A}$$

---

## Question 27

In Young's double slit experiment, the two slits are separated by  $0.2\text{ mm}$  and they are  $1\text{m}$  from the screen. The wavelength of the light used is  $500\text{ nm}$ . The distance between 6 th maxima and 10th minima on the screen is closest to

Options:

- A.  $12\text{ mm}$
- B.  $10\text{ mm}$
- C.  $14\text{ mm}$
- D.  $8\text{ mm}$

Answer: D

## Solution:

Solution:

Given,  $d = 0.2\text{mm} = 2 \times 10^{-4}\text{m}$

$D = 1\text{m}, \lambda = 500\text{nm} = 5 \times 10^{-7}\text{m}$

The distance between 6th maxima and 10th minima is given as

$$\Delta x = (x_{10})_{\text{dark}} - (x_6)_{\text{bright}}$$

$$= \frac{(2 \times 10 - 1)D\lambda}{2d} - \frac{6D\lambda}{d}$$

$$= \frac{D\lambda}{d} \left[ \frac{19}{2} - 6 \right]$$

$$= \frac{1 \times 5 \times 10^{-7}}{2 \times 10^{-4}} \left[ \frac{7}{2} \right] = \frac{35}{4} \times 10^{-3}\text{m}$$

$$= 8.75 \times 10^{-3}\text{m}$$

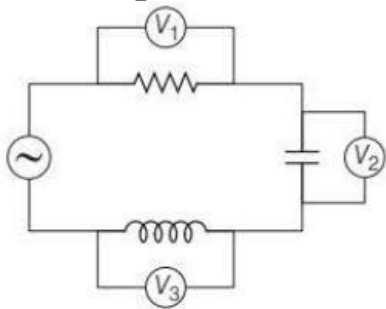
$$= 8.75\text{nm}$$

Hence, **8mm** is closest to **8nm**.

---

## Question 28

A series  $L - C - R$  circuit is connected to an AC source of 220V and 50 Hz shown in figure. If the readings of the three voltmeters  $V_1$ ,  $V_2$  and  $V_3$  are 65V, 415V and 204V respectively, the value of inductance and capacitance will be



Options:

A. 2.0H, 5 $\mu$ F

B. 1.0H, 5 $\mu$ F

C. 4.0H, 6 $\mu$ F

D. 1.0H, 2 $\mu$ F

**Answer: B**

## Solution:

Solution:

As  $V = I_{\text{rms}} R$

$$I_{\text{rms}} = \frac{V_R}{R} = \frac{65}{100} = 0.65\text{A}$$

$$V_L = I_{\text{rms}} \times X_L$$

$$X_L = \frac{V_L}{I_{\text{rms}}} = \frac{204}{0.65} = 313.85\Omega$$

$$X_L = \omega L = 2\pi f L$$

$$\text{or } L = \frac{X_L}{2\pi f}$$

$$L = \frac{313.85}{2 \times \pi \times 50} = 1.0 \text{ H}$$

$$X_c = \frac{V_c}{I_{ms}} = \frac{415}{0.65} = 638.46 \Omega$$

$$X_c = \frac{1}{\omega C} = \frac{1}{2\pi f C}$$

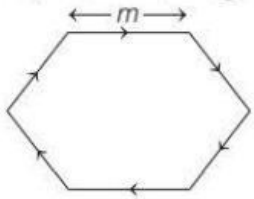
$$C = \frac{1}{2 \times \pi \times 50 \times 638.46}$$

$$= 5 \times 10^{-6} = 5 \mu\text{F}$$


---

## Question 29

A regular hexagon of side  $m$  which is a wire of length  $24\text{m}$  is coiled on that hexagon. If current in hexagon is  $I$ , then the magnetic moment,



Options:

A.  $6\sqrt{3}Im^2$

B.  $3\sqrt{3}Im^2$

C.  $\frac{3\sqrt{3}}{2}Im^2$

D.  $6Im^2$

Answer: A

Solution:

Solution:

Let number of turns of the regular hexagon =  $n$

Now,  $n \times 6m = 24m$

$\therefore n = 4$

Magnetic moment,  $M = nIA = 4IA$

$\therefore$  Area of hexagon

$$= \frac{1}{2}m^2 \sin 120^\circ + m \cdot 2m \sin 60^\circ + \frac{1}{2}m^2 \sin 120^\circ$$

$$= \frac{\sqrt{3}}{4}m^2 + \sqrt{3}m^2 + \frac{\sqrt{3}}{4}m^2$$

$$= \frac{6\sqrt{3}m^2}{4} = \frac{3\sqrt{3}m^2}{2}$$

$$\text{Hence, magnetic moment} = 4I \left( 3\sqrt{3} \frac{m^2}{2} \right)$$

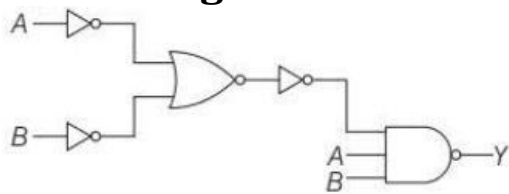
$$= 6\sqrt{3}Im^2$$


---

## Question 30

Which of the following gate give the similar output as the output of

circuit diagram shown in the figure?



Options:

- A. AND gate
- B. OR gate
- C. NOR gate
- D. NAND gate

**Answer: A**

**Solution:**

Solution:

From the given circuit diagram, output **Y** is given as

$$\begin{aligned} Y &= (A + B)AB \\ &= (A \cdot B)AB \text{ [By De Morgan's law, } A + B = A \cdot B] \\ &= (AB)(AB) [\because A \cdot A = A] \\ &= AB \\ &= \text{output of AND gate.} \end{aligned}$$

## Question 31

Water is poured in a tank through a cylindrical tube of area of cross-section  $A$  and ejecting water at a constant speed  $4\text{ m/s}$ . The tank contains a hole of area  $\frac{A}{2}$  at bottom. Level of water in the tank will not go up beyond

Options:

- A. 5.6m
- B. 4.8m
- C. 3.2m
- D. 1.8m

**Answer: C**

**Solution:**

Solution:

According to fluid dynamics, for maximum level of water in tank,

$$A_1 v_1 = A_2 v_2$$

Given,  $A_1 = A$ ,

velocity,  $v_1 = 4\text{ ms}^{-1}$

$$\begin{aligned} \text{area of hole } A_2 &= \frac{A}{2} \\ \Rightarrow A \times 4 &= \frac{A}{2} \times \sqrt{2gh} \\ \Rightarrow 16 &= \frac{2gh}{4} \\ \Rightarrow h &= \frac{16 \times 4}{2 \times 10} = 3.2\text{m} \end{aligned}$$


---

## Question 32

If R and C denote resistance and capacitance of a material, then the dimension of CR will be :

Options:

- A.  $[ML^0T]$
- B.  $[M^0L^0T]$
- C.  $[M^0L^0T^2]$
- D.  $[M^2L^0T]$

**Answer: B**

**Solution:**

Solution:

The capacitance of a conductor is defined as the ratio of the charge given to the rise in the potential of the conductor.

$$C = \frac{q}{V} = \frac{q}{\frac{W}{q}}$$

$$C = \frac{\text{ampere}^2 - \text{second}^2}{\text{kg}^2 - \text{metre}^2 \text{second}^{-2}}$$

Hence, dimensionally  $[M^{-1}L^{-2}T^4A^2]$

From Ohm's law,  $V = IR$ ,

$$\text{Hence, } R = \frac{V}{I} = \frac{\frac{W}{q}}{\frac{q}{t}} = \frac{W}{q} \times \frac{t}{q}$$

$$\begin{aligned} R &= \frac{F \times s \times t}{q^2} = \text{kg} \frac{\text{m}}{\text{s}^2} \times \frac{\text{m} \times \text{s}}{\text{A}^2 \times \text{s}^2} \\ &= \text{kgm}^2\text{s}^{-3}\text{A}^{-2} \end{aligned}$$

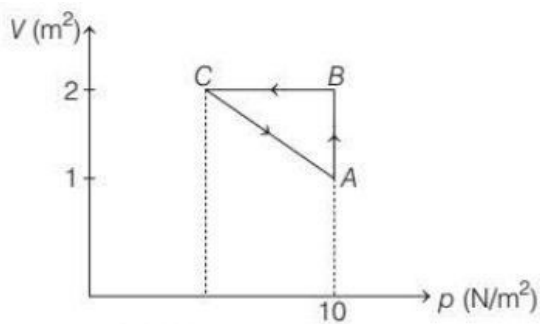
Dimensionally,  $R = [M L^2 T^{-3} A^{-2}]$

$$\begin{aligned} \text{Hence, } CR &= [M^{-1}L^{-2}T^4A^2][M L^2 T^{-3} A^{-2}] \\ &= [M^0 L^0 T] \end{aligned}$$


---

## Question 33

An ideal gas is taken through the cycle  $A \rightarrow B \rightarrow C \rightarrow A$ , as shown in the figure. If the net heat supplied to the gas in the cycle is 5J, the work done by the gas in the process  $C \rightarrow A$  is,



Options:

A.  $-5\text{J}$

B.  $-10\text{J}$

C.  $-15\text{J}$

D.  $-20\text{J}$

**Answer: A**

**Solution:**

Solution:

Net work done by a gas,

$$\Delta W_{AB} = p \cdot \Delta V = 10 \times (2 - 1) = 10\text{J}$$

$$\Delta W_{BC} = 0 \text{ (as } V = \text{constant)}$$

From first law of thermodynamics,

$$\text{we have, } \Delta Q = \Delta W + \Delta U$$

$$U = 0$$

(process **ABCA** is cyclic)

$$\text{Therefore, } \Delta Q = \Delta W_{AB} + \Delta W_{BC} + \Delta W_{CA}$$

$$\therefore \Delta W_{CA} = (\Delta Q - W_{AB} - W_{BC})$$

$$= (5 - 10 - 0)\text{J} = -5\text{J}$$

## Question 34

From a circular disc of radius  $R$ , a square is cut out with a radius as its diagonal. The centre of mass of remaining portion is at a distance (from the centre)

Options:

A.  $\frac{R}{(4\pi - 2)}$

B.  $\frac{R}{2\pi}$

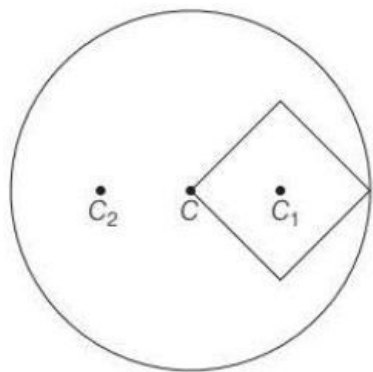
C.  $\frac{R}{\pi - 2}$

D.  $\frac{R}{2\pi - 2}$

**Answer: A**

**Solution:**

Solution:



Radius of the circular disc =  $R$

Suppose, centre of mass of remaining portion is at a distance  $CC_2$  from the  $C$ .

Now,  $A_1(CC_1) = A_2(CC_2)$

For square,  $(\text{side})^2 + (\text{side})^2 = (\text{radius})^2$

$$2(\text{side})^2 = R^2$$

$$(\text{side})^2 = \frac{R^2}{2}$$

$$\text{side} = \frac{R}{\sqrt{2}}$$

Now,  $A_1(CC_1) = A_2(CC_2)$

$$\therefore CC_2 = \frac{A_1(CC_1)}{A_2}$$

$$A_1 = \text{area of the square} = \left(\frac{R}{\sqrt{2}}\right)^2$$

$A_2$  = area of the remaining part of the circle

$$= \pi R^2 - \left(\frac{R}{\sqrt{2}}\right)^2$$

$$CC_2 = \frac{\left(\frac{R}{\sqrt{2}}\right)^2}{\pi R^2 - \left(\frac{R}{\sqrt{2}}\right)^2} \cdot \left(\frac{R}{2}\right)$$

$$= \frac{R^2}{2\pi R^2 - R^2} \cdot \frac{R}{2}$$

$$= \frac{R \cdot R \cdot R}{R^2(2\pi - 1)2} = \frac{R}{4\pi - 2}$$

## Question 35

A bar magnet of length 6 cm, is placed in the magnetic meridian with N pole, pointing towards the geographical north. Two neutral points, separated by a distance of 8 cm are obtained on the equatorial axis of the magnet. If  $B_H = 1.2 \times 10^{-5}$  T. Then the pole strength of the magnet is

Options:

A.  $0.75A - m^2$

B.  $0.25A - m^2$

C.  $0.50A - m^2$

D.  $1.50A - m^2$

Answer: B

Solution:

Solution:

At neutral point

$$\mathbf{B} = \mathbf{B}_H$$

$$\Rightarrow \frac{\mu_0}{4\pi} \times \frac{M}{(r^2 + l^2)^{\frac{3}{2}}} = B_H$$

$$\Rightarrow 10^{-7} \times \frac{m \times 2l}{3} = 1.2 \times 10^{-5}$$

$$\Rightarrow 10^{-7} \times \frac{m \times 2 \times 3 \times 10^{-2}}{[(4 \times 10^{-2})^2 + (3 \times 10^{-2})^2]^{\frac{3}{2}}} = 1.2 \times 10^{-5}$$

$$\Rightarrow \frac{6m \times 10^{-4}}{3} = 1.2$$

$$\Rightarrow \frac{6m \times 10^{-4}}{125 \times 10^{-6}} = 1.2$$

$$\Rightarrow m = \frac{1.2 \times 125 \times 10^{-2}}{6}$$

$$= 0.25A - m^2$$

## Question 36

A force  $F$  applied on the wire of radius  $r$  and length  $L$  and change in the length of the wire is  $l$ . If the same force  $F$  is applied on the wire of the same material and radius  $4r$  and length  $4L$ , then change in length of the other wire is,

Options:

A.  $\frac{l}{4}$

B.  $2l$

C.  $\frac{l}{2}$

D.  $4l$

**Answer: A**

**Solution:**

Solution:

As per formula, the Young's modulus,  $\gamma = \frac{\text{stress}}{\text{strain}}$

$$= \frac{\frac{F}{A}}{\frac{\Delta l}{L}}$$

$$\Rightarrow F = \frac{\gamma A \Delta l}{L}$$

In first case,  $\gamma = \frac{F}{\frac{A_1}{\frac{L_1}{L}}}$

$$\Rightarrow F = \frac{\gamma L_1 A_1}{L} \dots \dots \dots (i)$$

Similarly, for the second case,



$$F = \frac{\gamma I_2 A_2}{\Delta l} \dots\dots\dots (ii)$$

From Eqs. (i) and (ii), we get

$$\frac{\gamma I_1 A_1}{L} = \frac{\gamma I_2 A_2}{4L}$$

As  $\gamma$  is same, as the same material is taken,  $I_1 A_1 = \frac{I_2 A_2}{4}$

$$I_1 \pi r^2 = \frac{I_2 \pi (4r)^2}{4}$$

$$I_1 = \frac{I_2}{4} \cdot \frac{4r^2}{r^2} = 4I_2 \Rightarrow I_1 = \frac{I_2}{4}$$

$$\text{Hence, } I_1 = I, I_2 = \frac{I}{4}$$

## Question 37

A 30 mW laser beam has a cross-sectional area of 15mm<sup>2</sup>. The magnitude of the maximum electric field in this electromagnetic wave is

given by  $\left[ \begin{array}{l} \text{Permittivity of space, } \epsilon_0 = 9 \times 10^{-12} \\ \text{Speed of light, } c = 3 \times 10^8 \text{m/s} \end{array} \right]$

Options:

A. 1.22 kV/m

B. 12 kV/m

C. 10 kV/m

D. 201 kV/m

**Answer: A**

**Solution:**

Solution:

Given, power of laser beam,

$$P = 30\text{mW} = 30 \times 10^{-3}\text{W}$$

$$\text{Area of cross section, } A = 15\text{mm}^2 = 15 \times 10^{-6}\text{m}^2$$

$$\text{Permittivity of free space, } \epsilon_0 = 9 \times 10^{-12} \text{ SI unit}$$

$$\text{Speed of light, } c = 3 \times 10^8 \text{m/s}$$

Intensity of electromagnetic wave is given by

$$I = \frac{1}{2} n c \epsilon_0 E^2$$

where,  $n$  is refravctive index for air,  $n = 1$

$$I = \frac{1}{2} c \cdot \epsilon_0 E^2 \dots\dots\dots (i)$$

$$I = \frac{P}{A} \dots\dots\dots (ii)$$

From Eqs. (i) and (ii), we get

$$\frac{1}{2} c \epsilon_0 E^2 = \frac{P}{A}$$

$$E^2 = \frac{2P}{A c \epsilon_0}$$

$$E = \sqrt{\frac{2 \times 30 \times 10^{-3}}{15 \times 10^{-6} \times 3 \times 10^8 \times 9 \times 10^{-12}}} \\ = 1.22 \times 10^3 \text{V/m} = 1.22 \text{kV/m}$$

---

## Question 38

The average kinetic energy of a molecule in air at room temperature of  $20^{\circ}\text{C}$

Options:

- A.  $6 \times 10^{-22}\text{J}$
- B.  $7.06 \times 10^{-21}\text{J}$
- C.  $6.07 \times 10^{-21}\text{J}$
- D.  $6.70 \times 10^{-21}\text{J}$

Answer: C

Solution:

Solution:

The average molecular kinetic energy is expressed as

$$K = \frac{1}{2}mv^2 = \frac{3}{2}kT$$

Given,  $T = 20^{\circ}\text{C} = 20 + 273 = 293\text{K}$

$k = 1.38 \times 10^{-23}\text{J/K}$  = Boltzmann's constant

Substituting all the values, we get

$$K = \frac{3}{2} \times 1.38 \times 10^{-23} \times 293$$
$$= 6.07 \times 10^{-21}\text{J}$$

---

## Question 39

Two guns P and Q can fire bullets at speeds  $2\text{ km/s}$  and  $4\text{ km/s}$ , respectively. From a point on a horizontal ground, they are fired in all possible directions. The ratio of maximum or areas covered by the bullets fired by the two guns, on the ground is

Options:

- A. 1 : 2
- B. 1 : 4
- C. 1 : 8
- D. 1 : 16

Answer: D

Solution:

Solution:

As for the projectile motion, horizontal range,

$$R = \frac{u^2 \sin 2\theta}{g}$$

$$\therefore \text{Maximum range} = u^2 / g$$

$$\therefore A = \pi R^2$$

$$\therefore A \propto R^2$$

$$\text{i.e., } A \propto u^2$$

$$\therefore \frac{A_1}{A_2} = \frac{u_1^2}{u_2^2} = \left(\frac{2}{4}\right)^2 = \left(\frac{1}{2}\right)^2 = \frac{1}{4}$$

## Question 40

A cell of emf 2V is connected with a load of resistance 1.5Ω. The power delivered by the cell to the load is maximum, then power transferred to the load is

Options:

A. 0.33W

B. 2.67W

C. 1.33W

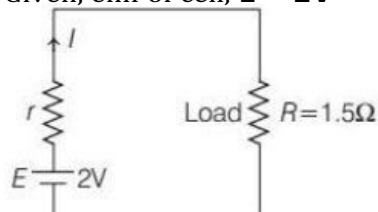
D. 3.25W

**Answer: A**

**Solution:**

Solution:

Given, emf of cell,  $E = 2V$



Load resistance,  $R_L = 1.5\Omega$

Current flowing the circuit is

$$I = \frac{E}{R + r}$$

Power transfered to the load,  $P$ ,

$$P = I^2 R = \left( \frac{E}{R + r} \right)^2 \cdot R = \frac{E^2 R}{(R + r)^2}$$

Power  $P$  will be maximum, if

$$\frac{dP}{dR} = 0$$

$$\Rightarrow \frac{d}{dR} \frac{E^2 R}{(R + r)^2} = 0$$

$$\Rightarrow \frac{E^2 (R + r)^2 - E^2 \cdot R \cdot 2(R + r)}{(R + r)^3} = 0$$

$$\Rightarrow E^2 (R + r) [R + r - 2R] = 0$$

$$\Rightarrow E^2 (R + r) (r - R) = 0$$

$$\Rightarrow r - R = 0$$

$$\Rightarrow r = R$$

$$\therefore \text{Maximum power, } P = \frac{E^2 R}{(R + r)^2} = \frac{E^2 R}{(R + R)^2} = \frac{E^2}{4R}$$

$$\Rightarrow P = \frac{2^2}{4} \times 1.5 = \frac{1}{3} = 0.33W$$

---

## Question 41

A plane glass mirror of thickness 3 cm of material of  $\mu = \frac{3}{2}$  is silvered on the black surface. When a point object is placed 9 cm from the front surface of the mirror, then the position of the brightest image from the front surface is

Options:

- A. 9 cm
- B. 11 cm
- C. 12 cm
- D. 13 cm

**Answer: D**

**Solution:**

Solution:

A thick glass mirror produces a number of images. There is an apparent shift of actual silvered surface towards the unsilvered face.

$$\begin{aligned}\text{Effective distance of the reflecting surface from unsilvered face} &= \frac{d}{\mu} \\ &= \frac{3}{\frac{3}{2}} \text{cm} = 2 \text{cm}\end{aligned}$$

Distance of point object from effective reflecting surface

$$= 9 \text{cm} + 2 \text{cm} = 11 \text{cm}$$

Distance of image from point object

$$= 11 \text{cm} + 11 \text{cm} = 22 \text{cm}$$

Distance of image from unsilvered face

$$= (22 - 9) \text{cm} = 13 \text{cm}$$

---

## Question 42

Ultraviolet light of wavelength 99 nm falls on a metal plate of work function 1.0 eV. If the mass of the electron is  $9.1 \times 10^{-31}$  kg, the wavelength of the fastest photoelectron emitted is

Options:

- A. 0.63 nm
- B. 0.66 nm
- C. 0.33 nm
- D. 0.36 nm

**Answer: D**

**Solution:**

Solution:

Given  $K_{\max} = h\nu - W_0$

$$= \frac{(6.6 \times 10^{-34}) \times (3 \times 10^8)}{99 \times 10^{-9}} - 1.0 \times 1.6 \times 10^{-19}$$

$$= 2 \times 10^{-18} - 1.6 \times 10^{-19}$$

$$= 1.84 \times 10^{-18} \text{ J}$$

Now,  $\lambda = \frac{h}{\sqrt{2mK_{\max}}}$

$$= \frac{6.6 \times 10^{-34}}{\sqrt{2 \times (9.1 \times 10^{-31}) \times 1.84 \times 10^{-18}}}$$

$$= 0.36 \times 10^{-9} \text{ m} = 0.36 \text{ nm}$$

---

## Question 43

In Young's double slit experiment, the fringe width is found to be 0.4 mm. If the whole apparatus is immersed in a liquid of refractive index  $\frac{4}{3}$  without changing geometrical arrangement, the new fringe width will be

Options:

A. 0.45 mm

B. 0.4 mm

C. 0.53 mm

D. 0.30 mm

Answer: D

Solution:

Solution:

If fringe widths of air and water are  $\beta_{\text{air}}$  and  $\beta_{\text{water}}$  respectively, then fringe width,  $\beta_{\text{water}} = \frac{\beta_{\text{air}}}{\mu}$

$$\text{Given, } \mu = \frac{4}{3}, \beta_{\text{water}} = 0.4$$

$$\text{Hence, } \beta_{\text{air}} = \frac{0.4 \times 4}{3} = 0.53 \text{ mm}$$

---

## Question 44

There are two identical containers  $C_1$  and  $C_2$  containing identical gases. Gas in  $C_1$  is reduced to half of its original volume adiabatically, while the gas in container  $C_2$  is also reduced to half of its initial volume isothermally. Find the ratio of final pressure in these containers. ( $\gamma$  be the adiabatic constant).

Options:

A. 2 : 1

B.  $1 : 2$

C.  $2^\gamma : 1$

D.  $2^{\gamma-1} : 1$

**Answer: D**

**Solution:**

Solution:

Since, container are identical, so initial volume and pressure will be same for identical gases. For container  $C_1$ ,

$p_1 V_1^\gamma = p_2 V_2^\gamma$  (adiabatic)

$$p_2 = \left( \frac{V_1}{V_2} \right)^\gamma p_1 = \left( \frac{V_1}{\frac{V_1}{2}} \right)^\gamma p_1 = 2^\gamma p_1 \dots \dots \dots (i)$$

For container  $C_2$ ,

$p_1 V_1 = p_2' V_2$  (isothermal)

$$p_2' = \left( \frac{V_1}{V_2} \right) p_1 = \left( \frac{V_1}{\frac{V_1}{2}} \right) p_1 = 2 p_1 \dots \dots \dots (ii)$$

From Eqs. (i) and (ii), we get

$$\frac{p_2}{p_2'} = \frac{2^\gamma p_1}{2 p_1} = 2^{\gamma-1} : 1$$

## Question 45

If  $K_1$  and  $K_2$  are maximum kinetic energies of photoelectrons emitted when lights of wavelengths  $\lambda_1$  and  $\lambda_2$ , respectively incident on a metallic surface and  $\lambda_1 = 3\lambda_2$ , then

**Options:**

A.  $K_1 > \left( \frac{K_2}{3} \right)$

B.  $K_1 < \left( \frac{K_2}{3} \right)$

C.  $K_1 = 2K_2$

D.  $K_2 = 2K_1$

**Answer: B**

**Solution:**

Solution:

Let  $W_0$  be the work function of the metal, then kinetic energy of photoelectrons emitted when light of wavelength  $\lambda_1$  is incident will be

$$K_1 = \frac{hc}{\lambda_1} - W_0$$

$$\text{Similarly, } K_2 = \frac{hc}{\lambda_2} - W_0$$

$$\begin{aligned}
 \text{Now, } K_1 &= K_2 = \frac{hc}{\lambda_1} - \frac{hc}{\lambda_2} = hc \left[ \frac{1}{\lambda_1} - \frac{1}{\lambda_2} \right] \\
 &= hc \left[ \frac{1}{3\lambda_2} - \frac{1}{\lambda_2} \right] \\
 K_1 - K_2 &= \frac{-2hc}{3\lambda_2} = \frac{-2}{3} (K_2 + W_0) \\
 \Rightarrow K_1 &= K_2 - \frac{2}{3}K_2 - \frac{2}{3}W_0 \\
 &= \frac{K_2}{3} - \frac{2}{3}W_0 \Rightarrow K_1 < \frac{K_2}{3}
 \end{aligned}$$


---

## Question 46

A car is moving with a speed of 54 km / h. If after 3 s, the driver applies brakes and it stops, then how much distance is covered by the car before coming to rest?

Options:

- A. 22.5m
- B. 20m
- C. 25m
- D. 45.2m

**Answer: A**

**Solution:**

Solution:

$$\begin{aligned}
 \text{Given, speed of car, } u &= 54 \text{ km/h} = 54 \times \frac{5}{18} \\
 &= 15 \text{ m/s}
 \end{aligned}$$

Since, car stops in 3 s on applying brakes, so acceleration can be calculated from first equation of motion,

$$v = u + at \Rightarrow 0 = 15 + a(3)$$

$$\Rightarrow a = -\frac{15}{3} = -5 \text{ ms}^{-2}$$

Using second equation of motion,

$$s = ut + \frac{1}{2}at^2$$

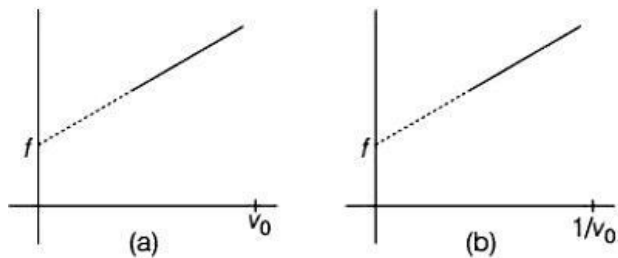
$$= 15 \times 3 + \frac{1}{2} \times (-5) \times (3)^2$$

$$= 45 - 22.5 = 22.5 \text{ m}$$


---

## Question 47

A source of sound emits sound waves at frequency  $f_0$ . It is moving towards an observer with fixed speed  $v_s$  ( $v_s < v$ , where  $v$  is the speed of sound in air.) If the observers were to move towards the source with speed  $v_0$ , one of the following two graphs (A and B) will give the correct variation of the frequency  $f$  heard by the observer as  $v_0$  is change



The variation of  $f$  with  $v_0$  is given correctly by

Options:

A. graph A with slope =  $\frac{f_0}{(v + v_s)}$

B. graph B with slope =  $\frac{f_0}{(v - v_s)}$

C. graph A with slope =  $\frac{f_0}{(v - v_s)}$

D. graph B with slope =  $\frac{f_0}{(v + v_s)}$

**Answer: C**

**Solution:**

Solution:

According to Doppler's effect, the apparent frequency of sound when both source and observer are moving towards each other

$$\Rightarrow f = \frac{(v + v_0)f_0}{(v - v_s)}$$

$$\Rightarrow f = \left( \frac{v}{v - v_s} \right) f_0 + \left( \frac{v_0}{v - v_s} \right) f_0$$

$$\Rightarrow f = \left( \frac{f_0}{v - v_s} \right) v_0 + \left( \frac{f_0}{v - v_s} \right) v$$

Equation of straight line,  $y = mx + c$  which is equation of straight line making an intercept  $c$  on  $Y$ -axis,

Slope of the graph =  $\frac{f_0}{v - v_s}$  and intercept =  $\frac{vf_0}{v - v_s}$

This condition is represented in graph A plotted between  $f$  and  $v_0$ .

Hence, option (c) is correct.

## Question 48

In which mode of transmission, the heat waves travel along straight line with the speed of light?

Options:

A. Thermal radiation

B. Forced convection

C. Natural convection

D. Thermal conduction



**Answer: A**

**Solution:**

Solution:

The energy emitted by a body, in the form of radiation on account of its temperature, is called thermal radiation. These radiations are heat radiations and travel along straight lines with speed of light.

---

## Question 49

**The escape velocity of a projectile on the earth's surface is  $11.2 \text{ km/s}$ . A body is projected out with thrice this speed. The speed of the body far away from the earth will be**

**Options:**

**A.  $22.4 \text{ km/s}$**

**B.  $31.7 \text{ km/s}$**

**C.  $33.6 \text{ km/s}$**

**D. None of these**

**Answer: B**

**Solution:**

Solution:

By the law of conservation of energy,

$$(U + K)_{\text{surface}} = (U + K)_{\infty}$$
$$\Rightarrow \frac{-GM}{R} + \frac{1}{2}m(3v_c)^2 = 0 + \frac{1}{2}mv^2$$

$$\Rightarrow -\frac{GM}{R} + \frac{9v_c^2}{2} = \frac{1}{2}v^2$$

$$\text{Since, } v_c^2 = \frac{2GM}{R}$$

$$\therefore -\frac{v_c^2}{2} + \frac{9v_c^2}{2} = \frac{1}{2}v^2$$

$$\Rightarrow v^2 = 8v_c^2$$

$$v = 2\sqrt{2}v_c = 2\sqrt{2} \times 11.2 = 31.7 \text{ km/s}$$

---

## Question 50

**Consider a compound slab consisting of two different materials having equal lengths, thickness and thermal conductivities  $K$  and  $2K$  respectively. The equivalent thermal conductivity of the slab is**

**Options:**

**A.  $\sqrt{2}K$**

**B.  $3K$**

C.  $\frac{4}{3}K$

D.  $\frac{2}{3}K$

**Answer: C**

**Solution:**

Solution:

Equivalent thermal conductivity of the compound slab,

$$K_{eq} = \frac{l_1 + l_2}{\frac{l_1}{K_1} + \frac{l_2}{K_2}} = \frac{l + l}{\frac{l}{K} + \frac{l}{2K}} = \frac{2l}{\frac{3l}{2K}} = \frac{4K}{3}$$

## Question 51

**A circular coil of 20 turns and radius 10 cm is placed in a uniform magnetic field of 0.10T normal to the plane of the coil. If the current in the coil is 5A, then the average force on each electron in the coil due to the magnetic field is**

**Options:**

**A.  $2.5 \times 10^{-25}N$**

**B.  $4.5 \times 10^{-25}N$**

**C.  $5 \times 10^{-25}N$**

**D.  $5.5 \times 10^{-25}N$**

**Answer: C**

**Solution:**

Solution:

Magnetic Lorentz force acting on each electron,

**$F = evB$  ..... (i)**

As, current,  **$i = neAv$**

**$ev = \frac{i}{nA}$**

Therefore, substituting value of  $ev$  into Eq.(i),

**$F = \frac{i}{nA}B$**

Given,  **$i = 5A$ ,  $n = 20$  turns,  $B = 0.1T$**

**$F = evB = \frac{iB}{nA} = \frac{5 \times 0.1}{10^{29} \times 10^{-5}} = 5 \times 10^{-25}N$**

## Question 52

**With what minimum acceleration can a fireman slide down a rope while breaking strength of the rope is  $\frac{2}{3}$  of the weight?**

**Options:**

A.  $\frac{2}{3}g$

B.  $g$

C.  $\frac{1}{3}g$

D. zero

**Answer: C**

**Solution:**

Solution:

If a man slides down with some acceleration, then its apparent weight decreases. For critical condition, rope can bear only  $\frac{2}{3}$  of his weight. If  $a$  is the minimum acceleration, then tension in the rope

$$= m(g - a) = \text{breaking strength}$$

$$\Rightarrow m(g - a) = \frac{2}{3}mg$$

$$\Rightarrow a = g - \frac{2g}{3} = \frac{g}{3}$$

---

## Question 53

**The string of length 2m is fixed at both ends. If the string vibrates in its fourth normal mode with a frequency of 500 Hz, then the waves would travel on it with a velocity of**

**Options:**

A.  $125\text{m/s}$

B.  $250\text{m/s}$

C.  $500\text{m/s}$

D.  $1000\text{m/s}$

**Answer: C**

**Solution:**

Solution:

In general,  $n$ th mode of a string fixed at ends has frequency,

$$v = \frac{nv}{2l}$$

where,  $n = 1, 2, 3, \dots$

where,  $v$  is the velocity of wave and  $l$  is the length of string.

In fourth normal mode,  $n = 4$

$$v = \frac{4v}{2l}$$

Given,  $v = 500\text{Hz}$ ,  $l = 2\text{m}$

$$\text{Hence, } 500 = \frac{4v}{2 \times 2}$$

$$\text{or, } v = \frac{500 \times 4}{4} = 500\text{m/s}$$

---

## Question 54

An alternating voltage =  $200\sin 100t$  is applied to a series combination of  $R = 30\Omega$  and an inductor of  $400\text{ mH}$ . The power factor of the circuit is,

Options:

- A. 0.01
- B. 0.6
- C. 0.05
- D. 0.042

Answer: B

Solution:

Solution:

As we know,

$$\text{power factor} = \frac{R}{Z}$$

$$= \frac{R}{\sqrt{R^2 + \omega L^2}}$$

Given  $\omega = 100$ ,  $L = 400\text{mH}$

$$= \frac{30}{\sqrt{(30)^2 + (100 \times 400 \times 10^{-3})^2}}$$

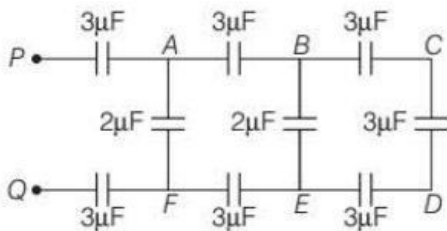
$$= \frac{30}{\sqrt{900 + 160000 \times 10^{-3 \times 2}}}$$

$$= \frac{30}{50} = 0.6$$

---

## Question 55

In the network shown in figure, the equivalent capacitance between points P and Q is



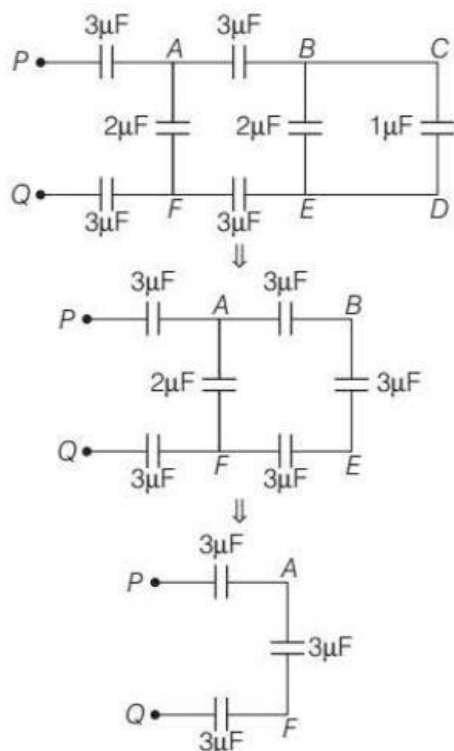
Options:

- A.  $1\mu\text{F}$
- B.  $2\mu\text{F}$
- C.  $3\mu\text{F}$
- D.  $4\mu\text{F}$

**Answer: A**

**Solution:**

Solution:



The equivalent capacitance between P and Q is given by

$$\frac{1}{C_{eq}} = \frac{1}{3} + \frac{1}{3} + \frac{1}{3} = \frac{1}{1\mu F}$$

$$C_{eq} = 1\mu F$$

## Question 56

The resultant of two forces acting at an angle of  $120^\circ$  is 10 kg-W and is perpendicular to one of the forces. That force is

Options:

A.  $\frac{10}{\sqrt{3}}$  kg – W

B. 10 kg – W

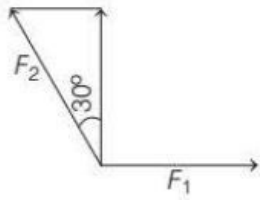
C.  $20\sqrt{3}$  kg – W

D.  $10\sqrt{3}$  kg – W

**Answer: A**

**Solution:**

Solution:



From the diagram we get,

$$\tan 30^\circ = \frac{1}{\sqrt{3}} = \frac{x}{10}$$

$$\Rightarrow x = \frac{10}{\sqrt{3}}$$

## Question 57

**Choose the incorrect statements.**

**Options:**

- A. Silicon is used in the fabrication of LED.**
- B. LED works on the principle of electroluminescenc**
- C. LED is a power efficient device.**
- D. LED is fabricated with direct band gap semiconductor.**

**Answer: A**

**Solution:**

Solution:

The most commonly used material in LEDs is gallium arsenide.

## Question 58

**Charge on electron is**

**Options:**

- A.  $3.2 \times 10^{-19}\text{C}$**
- B.  $1.6 \times 10^{-19}\text{C}$**
- C.  $-1.6 \times 10^{-19}\text{C}$**
- D.  $-3.2 \times 10^{-19}\text{C}$**

**Answer: C**

**Solution:**

Solution:

Charge on electron is negative and its magnitude is

$$1.6 \times 10^{-19}\text{C}$$

---

## Question 59

Two charged spheres of  $-20\mu\text{C}$  and  $60\mu\text{C}$  are kept at a certain distance. They are touched and kept again at the same distance. What is the ratio of force experienced before and after?

Options:

- A. 1 : 3
- B. 3 : 1
- C. 2 : 1
- D. 1 : 2

**Answer: B**

**Solution:**

Solution:

Given,  $q_1 = -20\mu\text{C} = -2 \times 10^{-5} \text{ C}$

$q_2 = 60\mu\text{C} = 6 \times 10^{-5} \text{ C}$

Force of attraction between the both charges, kept at a certain distance  $r$

$$\begin{aligned} F_1 &= \frac{K q_1 q_2}{r^2} \\ &= \frac{K \times 2 \times 10^{-5} \times 6 \times 10^{-5}}{r^2} \\ &= \frac{12 \times 10^{-10} K}{r^2} \end{aligned}$$

When both charges are touched, then new charge on both spheres,

$$\begin{aligned} q_1' &= q_2' = \frac{q_1 + q_2}{2} = \frac{-20 + 60}{2} = 20\mu\text{C} \\ &= 2 \times 10^{-5} \text{ C} \end{aligned}$$

$\therefore$  Force between the two spheres,

$$\begin{aligned} F_2 &= \frac{K q_1' \cdot q_2'}{r^2} \\ &= \frac{K \cdot 2 \times 10^{-5} \times 2 \times 10^{-5}}{r^2} \\ &= \frac{4 \times 10^{-10} K}{r^2} \end{aligned}$$

$$\therefore \frac{F_1}{F_2} = \frac{\frac{12 \times 10^{-10} K}{r^2}}{\frac{4 \times 10^{-10} K}{r^2}} = \frac{12}{4} = \frac{3}{1}$$

$$\therefore F_1 : F_2 = 3 : 1$$

---

## Question 60

The AC voltage across a resistance can be measured using a

Options:

- A. hot wire voltmeter
- B. moving coil galvanometer

- C. potential coil galvanometer
- D. moving magnet galvanometer

**Answer: B**

**Solution:**

Solution:

An AC voltage across a resistance can be measured by using a moving coil galvanometer. It can be used as a voltmeter by inserting a resistor in series with it. It responds only to direct current. Hence, it requires a rectifier, so that coil deflects only in one direction.

-----

## Question 61

**..... is unstable at cooking temperature, whereas the control of sweetness of food is difficult while using .....**

**Options:**

- A. Alitame and aspartame
- B. Aspartame and sucralose
- C. Aspartame and alitame<
- D. Alitame and sucralose

**Answer: C**

**Solution:**

Solution:

Use of aspartame is limited to cold foods because it is unstable at cooking temperature.

Alitame is more stable than aspartame but the control of sweetness of food is difficult while using it.

-----

## Question 62

**The chemical formula of Lucas reagent is**

**Options:**

- A. Anhy.  $\text{ZnCl}_2/\text{HCl}$
- B.  $\text{C}_6\text{H}_5\text{SO}_2\text{Cl}$
- C.  $\text{NaOH} + \text{CaO}$
- D.  $\text{HNO}_2$

**Answer: A**

**Solution:**



Solution:

Lucas reagent: Anhyd.  $\frac{\text{ZnCl}_2}{\text{HCl}}$ . It is used to differentiate **1°**, **2°** and **3°** alcohols.

---

## Question 63

Give the correct order of acidity of

Options:

A.  $\text{HClO}_4 < \text{HClO}_3 < \text{HClO}_2 < \text{HClO}$

B.  $\text{HClO} < \text{HClO}_2 < \text{HClO}_3 < \text{HClO}_4$

C.  $\text{HClO}_4 < \text{HClO}_2 < \text{HClO} < \text{HClO}_3$

D.  $\text{HClO} < \text{HClO}_3 < \text{HClO}_2 < \text{HClO}_4$

Answer: B

Solution:

Solution:

Acidic strength of oxo-acids containing the same halogen are in the order :

$\text{HCl} < \text{HClO}_2 < \text{HClO}_3 < \text{HClO}_4$

This is because  $\text{ClO}_4^-$  is the most stable due to dispersal of negative charge on four O-atoms (O being more electronegative than Cl).

---

## Question 64

The process of aggregation of colloidal particles into an insoluble precipitate by the addition of suitable electrolyte is called

Options:

A. coagulation

B. diffusion

C. peptisation

D. electrolysis

Answer: A

Solution:

Solution:

**Coagulation** The process of aggregation of colloidal particles into an insoluble precipitate by the addition of suitable electrolyte.

**Diffusion** The process of movement of molecules from a region of higher concentration to a region of lower concentration.

**Peptisation** The process of converting a precipitate into colloidal sol by shaking it with dispersion medium in the presence of small amount of electrolyte.

Electrolysis The process by which electric current is passed through a substance to effect a chemical change.

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## Question 65

Alkyl halides undergoing  $S_N2$  reaction do inverse

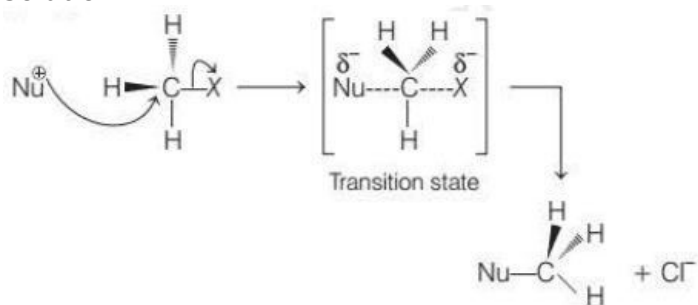
Options:

- A. racemic mixture
- B. retention of configuration
- C. formation of carbocation
- D. inversion of configuration

Answer: D

Solution:

Solution:

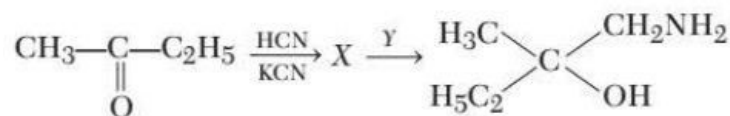


Inversion of configuration takes place. There is no carbocation formation.

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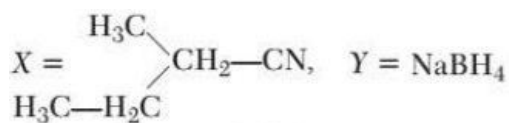
## Question 66

X and Y in the following reactions are

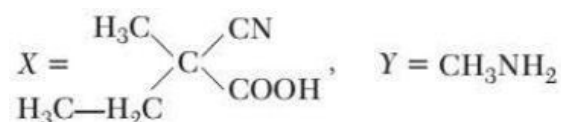


Options:

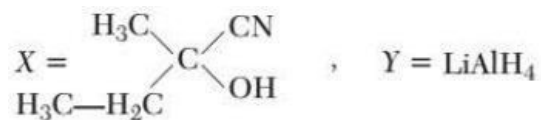
A.



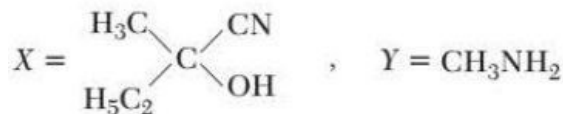
B.



C.



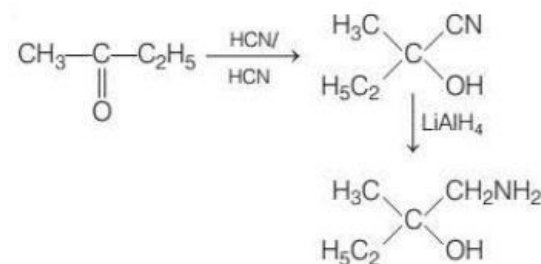
D.



Answer: C

Solution:

Solution:



---

## Question 67

Doping of silicon (Si) with indium (In) leads to the formation of

Options:

- A. n-type semiconductor
- B. metal
- C. p-type semiconductor
- D. insulator

Answer: C

Solution:

Solution:

Doping Si with In or B leads to the formation of **p**-type semiconductors.

In **p**-type semiconductors, trivalent impurities are used for doping, whereas, in **n**-type semiconductors, pentavalent impurities are used for doping.

---

## Question 68

For the reaction,  $\text{H}_2(\text{g}) + \text{I}_2(\text{g}) \rightleftharpoons 2 \text{HI}(\text{g})$  the position of equilibrium can be shifted to the right by

**Options:**

- A. addition of HI**
- B. addition of both  $I_2$  and HI**
- C. increasing temperature**
- D. addition of  $I_2$**

**Answer: D**

**Solution:**

Solution:

According to Le-Chatelier's principle when concentration of reactant increases, the equilibrium shifts in favour of forward reaction.

---

## Question 69

**Which of the following are not path functions?**

- I.  $H - TS$**
- II.  $W$**
- III.  $q$**
- IV.  $q + W$**

**Options:**

- A. I and III**
- B. I, II, IV**
- C. II, III and IV**
- D. I and IV**

**Answer: D**

**Solution:**

Solution:

Thermodynamic parameters which depend only on the initial and final states of system are called state functions, such as enthalpy ( $H = q + W$ ), Gibb's free energy ( $G = H - TS$ ).

Whereas, thermodynamic parameters which depend on the path by which the process is performed and not on initial and final states, are called path functions, such as work done ( $W$ ), heat ( $q$ ) etc.

---

## Question 70

**The system that forms maximum boiling azeotropes is**

**Options:**

- A. acetone-chloroform**

- B. ethyl alcohol-water
- C. benzene-toluene
- D.  $\text{CS}_2$ + acetone

**Answer: A**

**Solution:**

Solution:

When the non-ideal binary solution shows the negative deviation, it is known as a maximum boiling azeotrope e.g. acetone-chloroform. Rest all three options show positive deviation from Raoult's law.

## Question 71

$\text{KMnO}_4$  acts as an oxidising agent in acidic medium. The number of moles of  $\text{KMnO}_4$  that will be required to react with one mole of oxalate ions (to form  $\text{CO}_2$  ) in acidic solution is

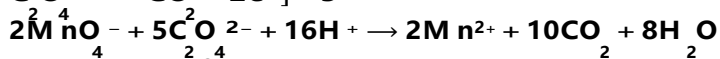
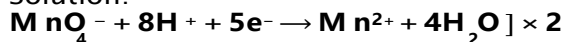
Options:

- A.  $\frac{2}{5}$
- B.  $\frac{5}{2}$
- C. 5
- D.  $\frac{5}{4}$

**Answer: A**

**Solution:**

Solution:



5 moles of  $\text{C}_2\text{O}_4^{2-}$  need 2 moles of  $\text{KMnO}_4$ .

1 mole of  $\text{C}_2\text{O}_4^{2-}$  would need  $= \frac{2}{5}$  mole of  $\text{KMnO}_4$ .

## Question 72

What can be A and B in the following reaction?<

Options:

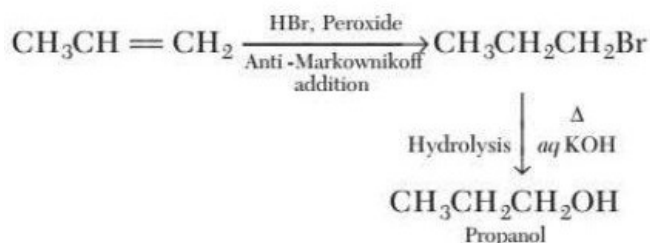
- A. HBr al

- B. KOH
- C. HBr, Peroxide alc. KOH
- D. HBr, Peroxide aq. KOH,  $\Delta$

**Answer: C**

**Solution:**

Solution:



## Question 73

**Which of the following is a false statement?**

**Options:**

- A. Methoxymethane has higher boiling point than ethanol.
- B. Alcohols are more soluble in water than hydrocarbons of comparable molecular mass.
- C. ortho- and para-nitrophenols are more acidic than phenols.
- D. Phenol is more acidic than alcohol.

**Answer: A**

**Solution:**

Solution:

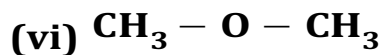
Ethanol undergoes intermolecular H-bonding due to the presence of a hydrogen attached to an electronegative oxygen atom. Hence, ethanol exists as associated molecules and a large amount of energy is required to break these **H**-bonds. Therefore, the boiling point of ethanol is higher than that of methoxy methane which does not form **H**-bonds.

---

## Question 74

**Which of the following molecules does not exhibit dipole moment?**

- (i)  $\text{CCl}_4$
- (ii)  $\text{CO}_2$
- (iii)  $\text{NH}_3$
- (iv)  $\text{CHCl}_3$
- (v)  $\text{H}_2\text{O}$



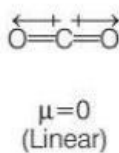
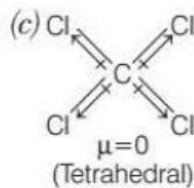
Options:

- A. (ii), (v), (iv)
- B. (i), (iii), (vi)
- C. (i), (ii)
- D. (iii), (iv), (vi)

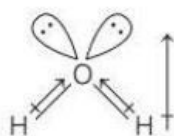
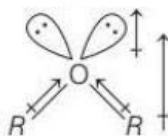
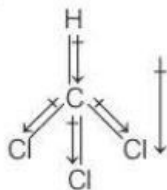
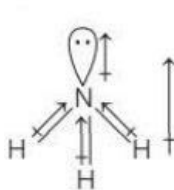
Answer: C

Solution:

Solution:



Dipole moments cancel out reach other in  $\text{CCl}_4$  and  $\text{CO}_2$  resulting in net dipole moment as zero because these are symmetrical structures.



## Question 75

Which of the following is highly basic?

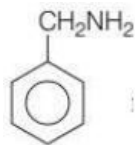
Options:

- A. Diphenylamine
- B. Benzylamine
- C. Aniline
- D. Triphenylamine

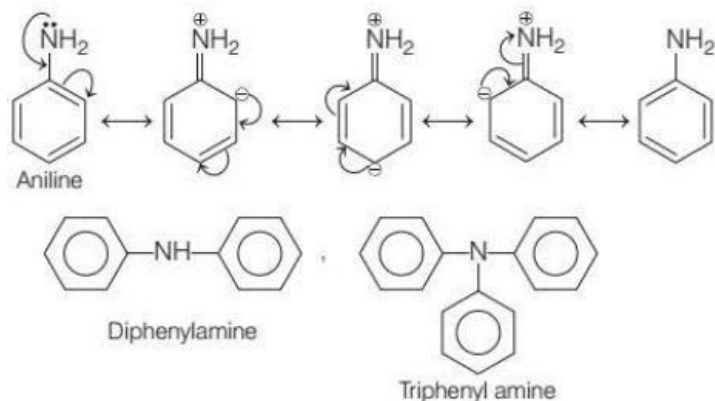
Answer: B

Solution:

Solution:



i.e. benzylamine is the most basic among other given options because lone pairs of **N** are available for donation. whereas lone pair of **N** in aniline, diphenylamine and triphenyl amine are delocalised over the benzene ring, hence are not available for donation, making them weaker bases.



## Question 76

The relation between work done in reversible and irreversible process is

Options:

- A.  $W_{\text{irr}} > W_{\text{rev}}$
- B.  $W_{\text{irr}} < W_{\text{rev}}$
- C.  $W_{\text{irr}} = W_{\text{rev}}$
- D.  $W_{\text{irr}} \neq W_{\text{rev}}$

Answer: B

Solution:

Solution:

All natural processes are generally irreversible and net work done in an irreversible process is some what less than in reversible process.

## Question 77

What is the function platelets?

Options:

- A. It binds to oxygen
- B. It binds to carbon dioxide
- C. It forms cyanide in body



**D. It leads to coagulation of blood**

**Answer: D**

**Solution:**

Solution:

Platelets are pieces of very large cells in bone marrow. They help in forming blood clots to stop bleeding and wounds heal.

---

## Question 78

**The monosaccharides of maltose is**

**Options:**

**A.  $\alpha$ -D-glucose and  $\alpha$ -D-glucose**

**B.  $\beta$ -D-glucose and  $\alpha$ -D-glucose**

**C.  $\alpha$ -D-glucose and  $\alpha$ -D-fructose**

**D.  $\alpha$ -D-glucose and  $\beta$ -D-fructose**

**Answer: A**

**Solution:**

Solution:

Hydrolysis of maltose yields two moles of  $\alpha$ -D-glucose in which **C – 1** of one glucose linked to **C – 4** of another glucose.

---

## Question 79

**Which of the following does not affect solubility of a gas in liquid?**

**Options:**

**A. Nature of gas and liquid**

**B. Pressure**

**C. Concentration**

**D. Temperature**

**Answer: C**

**Solution:**

Solution:

The solubility of any gas in a particular liquid is the volume of gas that can be dissolved in unit volume of liquid. It only depend upon pressure, temperature and nature of gas and liquid.

---

## Question 80

Which of the following statement is incorrect for  $\text{H}_2\text{O}_2$  structure?

Options:

- A. It has an open book structur
- B. Its dihedral angle is  $180^\circ$ .
- C. It O – O bond length is 145.8 and O – H is 98.8 .
- D. Angle between both planes is  $90.2^\circ$  .

Answer: B

Solution:

Solution:

$\text{H}_2\text{O}_2$  has open book structure with O – O spins. Its dihedral angle is  $111^\circ$ .

---

## Question 81

A newly prepared radioactive nuclide has a decay constant of  $6.93 \text{ s}^{-1}$ . What is the half-life of the nuclide?

Options:

- A. 0.1 s
- B. 0.2 s
- C. 0.3 s
- D. 0.4 s

Answer: A

Solution:

Solution:

Radioactive nuclide follow first order kinetics

$$t_{\frac{1}{2}} = \frac{0.693}{\lambda} = \frac{0.693}{6.93} = 0.1 \text{ s}$$

---

## Question 82

Which of the following show both Frenkel and Schottky defect?

Options:

- A. ZnS
- B. AgBr
- C. NaCl
- D. AgCl

**Answer: B**

**Solution:**

Solution:

**ZnS** and **AgCl** show Frenkel defect. **NaCl** show Schottky defect but **AgBr** show both defect.

---

## Question 83

**The essential amino acid are**

- (i) Leucine
- (ii) Glutamic acid
- (iii) Asparagine
- (iv) Valine

**correct option is**

**Options:**

- A. (i), (ii)
- B. (ii), (iii)
- C. (iii), (iv)
- D. (i), (iv)

**Answer: D**

**Solution:**

Solution:

The essential amino acids are histidine, isoleucine, leucine, lysine, methionine, phenylalanine, threonine, tryptophan and valine.

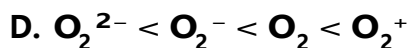
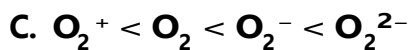
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## Question 84

**Increasing order of bond order of oxygen and its ions is**

**Options:**

- A.  $O_2 < O_2^+ < O_2^{2-} < O_2^-$
- B.  $O_2^- < O_2^{2-} < O_2^+ < O_2$



**Answer: D**

**Solution:**

Solution:

According to MOT, bond order is given by the formula,  $\text{BO} = \frac{N_b - N_a}{2}$  where  $N_a$ ,  $N_b$  are the number of electrons in antibonding and bonding molecular orbital respectively.

$$\text{Bond order for } \text{O}_2 = \frac{10 - 6}{2} = 2$$

$$\text{O}^- = \frac{10 - 7}{2} = 1.5$$

$$\text{O}^{+2} = \frac{10 - 5}{2} = 2.5$$

$$\text{O}^{2-} = \frac{10 - 8}{2} = 1$$

## Question 85

**Minimum number of nodes are present in**

**Options:**

A. 2s

B. 3s

C. 4s

D. 5s

**Answer: A**

**Solution:**

Solution:

Total number of nodes is given by  $(n - 1)$

$$2s = (2 - 1) = 1$$

$$3s = (3 - 1) = 2$$

$$4s = (4 - 1) = 3$$

$$5s = (5 - 1) = 4$$

## Question 86

**pH of  $10^{-3}\text{M}$  solution of KOH is**

**Options:**

A. 7.01

B. 2

C. 11

D. 9

**Answer: C**

**Solution:**

Solution:

As KOH is a base.

$$pOH = -\log[OH^-]$$

$$pOH = -\log[10^{-3}] = 3$$

$$pH + pOH = 14$$

$$pH = 14 - 3 = 11$$

---

## Question 87

**Barbiturates are used to treat**

**Options:**

A. fatigue

B. hallucinations

C. allergies

D. depression

**Answer: D**

**Solution:**

Solution:

Barbiturates are the depressants drug used to treat depression.

---

## Question 88

**Which of the product is not possible in Wurtz reaction?**

**Options:**

A. Methane

B. Ethane

C. Propane

D. Butane

**Answer: A**

**Solution:**

Solution:

Wurtz reaction is kind of reaction in which there is a formation of simple higher alkane from alkyl halides. Minimum two carbon chains should be present to form alkane in this reaction. So, methane cannot be formed.

---

## Question 89

The colour of  $\text{CrO}_4^{2-}$  changes to  $\text{Cr}_2\text{O}_7^{2-}$  is

Options:

- A. yellow to orange
- B. orange to yellow
- C. yellow to blue
- D. orange to blue

Answer: A

Solution:

Solution:

The  $\text{CrO}_4^{2-}$  (yellow) exist in acidic medium with **pH = 6** and changes to orange in basic medium as  $\text{Cr}_2\text{O}_7^{2-}$  with **pH = 8**

---

## Question 90

On treatment of glucose with bromine water the product formed is

Options:

- A. saccharic acid
- B. gluconic acid
- C. glutamic acid
- D. acetic acid

Answer: B

Solution:

Solution:

Bromine acts as mild oxidising agent and oxidation of glucose with bromine water form gluconic acid. This show presence of aldehyde group in glucose.

---

## Question 91

Which among the following forms minimum boiling azeotropes?

(i) Heptane + Octane

- (ii) Water + Nitric acid  
(iii) Ethanol + Water  
(iv) Acetone + Carbon dioxide

Options:

- A. (i), (ii), (iv)  
B. (i), (ii) only  
C. (i), (iii), (iv)  
D. (iv) only

Answer: C

Solution:

Solution:

Those azeotropes which boils at a temperature lower than boiling point of each component forms the minimum boiling azeotrope.

e.g. Heptane + octane, ethanol + water, acetone + carbon dioxide

---

## Question 92

Which of the following statement is incorrect about activation energy?  
**a. Higher the activation energy slower is the rate of reaction.**

Options:

- A. Higher the activation energy slower is the rate of reaction.  
B. Catalyst decreases the activation energy.  
C. SI unit of activation energy is  $\text{J/molK}^{-1}$ .  
D. Activation energy depends upon the rate of reaction.

Answer: C

Solution:

Solution:

The incorrect statement about activation energy is option (c) because the SI unit of activation energy is  $\text{J/mol}$  or  $\text{kJ/mol}$  or  $\text{kcal/mol}$ .

---

## Question 93

The P – O bond order in  $\text{PO}_4^{3-}$  is

Options:

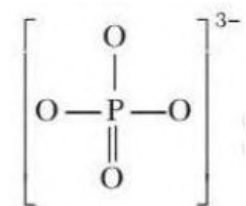
- A. 1
- B. 1.5
- C. 1.45
- D. 1.25

**Answer: D**

**Solution:**

Solution:

The structure of  $\text{PO}_4^{3-}$  is



$$\text{Bond order} = \frac{\text{Number of bonds}}{\text{Number of resonating structure}}$$

$$= \frac{5}{4} = 1.25$$

## Question 94

$\text{O}_2^-$ ,  $\text{F}^-$ ,  $\text{Mg}^{2+}$ ,  $\text{Al}^{3+}$ ,  $\text{O}_2$ ,  $\text{F}_2$  How many of the species given above are isoelectronic?

Options:

- A. 4
- B. 2
- C. 3
- D. 5

**Answer: A**

**Solution:**

Solution:

Those species which have same number of electrons are called isoelectronic species.

$\text{O}_2^-$ ,  $\text{F}^-$ ,  $\text{Mg}^{2+}$ ,  $\text{Al}^{3+}$  have **10** electrons.

Hence, **4** isoelectronic species are present.

## Question 95

How many atoms are present in hcp per unit cell?

Options:



- A. 4
- B. 2
- C. 1
- D. 6

**Answer: D**

**Solution:**

Solution:

The hcp (hexagonal close packing) has a coordination number of 12 and contains 6 atoms per unit cell.

---

## Question 96

The equilibrium constant,  $K_c$  for  $3C_2H_2(g) \rightleftharpoons C_6H_6(g)$  is  $4L^2mol^{-2}$ . If the equilibrium concentration of benzene is  $0.5mol^{-1}$  than what is the value of concentration of ethylene?

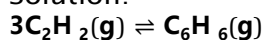
Options:

- A.  $0.05 mol / L$
- B.  $0.5 mol/L$
- C.  $0.25 mol/L$
- D.  $0.025 mol / L$

**Answer: B**

**Solution:**

Solution:



$$K_c = \frac{[C_6H_6]}{[C_2H_2]^3} = \frac{0.5}{[C_2H_2]^3}$$

$$4 = \frac{0.5}{[C_2H_2]^3}$$

$$[C_2H_2] = \sqrt[3]{\frac{0.5}{4}} = \frac{1}{2}$$

$$[C_2H_2] = 0.5 mol/L$$

Therefore, the concentration of ethylene is  $0.5 mol/L$ .

---

## Question 97

Which of the following artificial sweeteners can be used in soft drinks only?

Options:

- A. Alitame
- B. Aspartame
- C. Sucralose
- D. Saccharine

**Answer: B**

**Solution:**

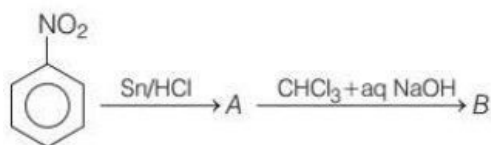
Solution:

Aspartame is used in soft drinks. It is an artificial sweetening agent which is unstable at higher temperatures. It is a compound formed from aspartic acid and phenyl alanine. It is 100 times as sweet as cane sugar.

-----

## Question 98

**Identify the product formed in the given reaction.**



**Options:**

**A.**



**B.**



**C.**



**D.**

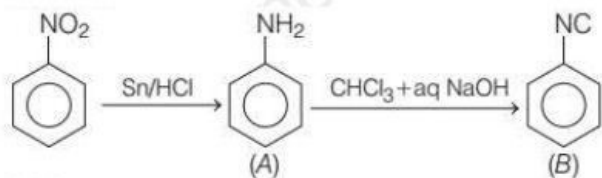


**Answer: B**

**Solution:**

Solution:

Complete reaction of the given reaction is as follows.



---

## Question 99

Which of the following gas readily de-colourises the acidified  $\text{KMnO}_4$  solution?

Options:

A.  $\text{CO}_2$

B.  $\text{SO}_2$

C.  $\text{P}_2\text{O}_5$

D.  $\text{NO}_2$

Answer: B

Solution:

Solution:

Sulphur dioxide gas readily decolourises the purple colour of acidified  $\text{KMnO}_4$  solution. In this case,  $\text{KMnO}_4$  acts as an oxidising agent and sulphur dioxide gas acts as a reducing agent.

---

## Question 100

Which of the following gas readily de-colourises the acidified  $\text{KMnO}_4$  solution?

Options:

A.  $\text{CO}_2$

B.  $\text{SO}_2$

C.  $\text{P}_2\text{O}_5$

D.  $\text{NO}_2$

Answer: B

Solution:

Solution:

Let, the rate of diffusion of gas **X**,  $r_1 = b$ . Therefore, rate of diffusion of methane,  $r_2 = 2b$

According to Graham's law of diffusion,

$$\left(\frac{r_1}{r_2}\right) = \left(\sqrt{\frac{M_2}{M_1}}\right)$$

$M_1$  = molecular mass of gas **X**

$M_2$  = molecular mass of methane = **16g**

$$\therefore \frac{b}{2b} = \sqrt{\frac{16}{M_2}}$$

$$\Rightarrow \left(\frac{1}{4}\right) = \frac{16}{M_2}$$

$$\Rightarrow M_2 = \mathbf{64g}$$

Therefore, molecular mass of **X** is **64g**.

---

## Question 101

Which of the following is used to prepare the inner lining of a blast furnace?

Options:

A. Graphite bricks

B. Silica bricks

C. Fire clay bricks

D. basic bricks

**Answer: C**

**Solution:**

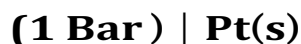
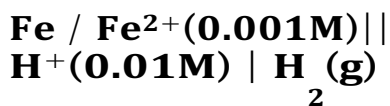
Solution:

Fire clay bricks is used to prepare the inner lining of a blast furnace. It is highly refractory in nature and does not melt, even at huge temperature. Its main components are silica and alumina.

---

## Question 102

What will be the emf of the following cell at 25°C ?



$$E_{(\text{Fe}^{2+} / \text{Fe})}^{\circ} = -0.44\text{V}; E_{(\text{H}^+ / \text{H}_2)}^{\circ} = 0.00\text{V}$$

Options:

A. 0.44V

B. -0.44V

C. 0.41V

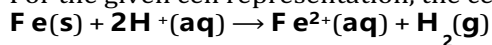
D. -0.41V

**Answer: C**

**Solution:**

Solution:

For the given cell representation, the cell reaction will be,



The standard emf of the cell will be,

$$E^\circ_{\text{cell}} = E^\circ_{\text{H}^+/\text{H}_2} - E^\circ_{\text{Fe}^{2+}/\text{Fe}}$$

$$= 0 - (-0.44) = 0.44\text{V}$$

The Nernst equation for the cell reaction at 25°C,

$$E_{\text{cell}} = E^\circ_{\text{cell}} - \frac{0.0591}{n} \log \frac{[\text{Fe}^{2+}]}{[\text{H}^+]^2}$$

$$= 0.44 - \frac{0.0591}{2} \log \frac{[0.001]}{[0.01]^2}$$

$$= 0.44 - 0.02955(\log 10)$$

$$= 0.44 - 0.02955(1)$$

$$= 0.41045\text{V} = 0.41\text{V}$$

---

## Question 103

**Which of the following vitamin is responsible for beri-beri disease?**

**Options:**

**A. A**

**B. B<sub>1</sub>**

**C. K**

**D. D**

**Answer: B**

**Solution:**

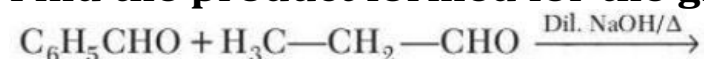
Solution:

Beri-beri disease is caused by the deficiency of vitamin **B<sub>1</sub>**.

---

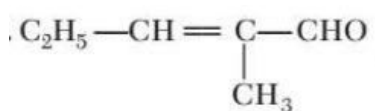
## Question 104

**Find the product formed for the given reaction.**



**Options:**

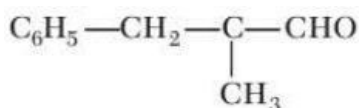
**A.**



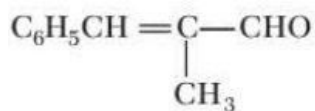
**B.**



**C.**



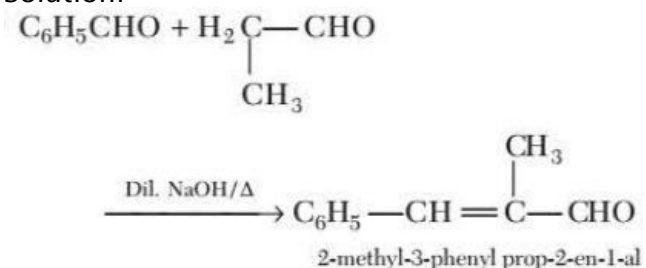
**D.**



**Answer: D**

**Solution:**

Solution:



---

## Question 105

**In which of the following changes, entropy decreases?**

**Options:**

**A. Rusting of iron**

**B. Melting of ice**

**C. Vaporisation of camphor**

**D. Crystallisation of sucrose from solution**

**Answer: D**

**Solution:**

Solution:

Among the given options, entropy decreases during the crystallisation of sucrose from solution. It is because entropy is a measure of randomness and during the process of crystallisation liquid state changes into solid state. Hence, entropy decreases.

---

## Question 106

**Which of the following is added to soaps to impart antiseptic properties?**

**Options:**

- A. Iodine**
- B. Furacine**
- C. Bithional**
- D. Terpineol**

**Answer: C**

**Solution:**

Solution:  
Bithional is an antiseptic which is widely used in medicinal soaps, so that soaps can impart antiseptic properties.

-----

## Question 107

**Which among the following will not liberate nitrogen on reaction with nitrous acid?**

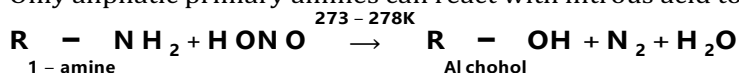
**Options:**

- A. dimethylamine**
- B. 2-aminopropane**
- C. ethylamine**
- D. methylamine**

**Answer: A**

**Solution:**

Solution:  
Only aliphatic primary amines can react with nitrous acid to produce alcohol, water and nitrogen gas.



So, dimethylamine which is a secondary amine cannot liberate  $\text{N}_2$  with  $\text{HONO}$ .

-----

## Question 108

**- The complex which does not show optical isomerism is**

**Options:**

- A. cis -[Co(en)<sub>2</sub> Cl<sub>2</sub>] Cl**



**Answer: D**

**Solution:**

Solution:

Octahedral complex of general formula  $[\text{M}(\text{AA})_2\text{a}]^{n\pm}$  shows optical isomerism. cis-

$[\text{Co}(\text{NH}_3)_4\text{Cl}_2]^+$  does not show optical isomerism due to symmetry, while other three complexes show optical isomerism.

## Question 109

. What will be the density of  $\text{N}_2$  gas at  $230^\circ\text{C}$  and 3 atm pressure?

( $R = 0.082 \text{ L atm K}^{-1} \text{ mol}^{-1}$ )

Options:

A.  $3.41 \text{ g/mL}$

B.  $2.03 \text{ g/mL}$

C.  $4.30 \text{ g/mL}$

D.  $0.27 \text{ g/mL}$

**Answer: B**

**Solution:**

Solution:

We know,  $pV = nRT$

or  $pV = \frac{W}{M}RT$  [ Here,  $n = \frac{\text{Weight of gas taken}(W)}{\text{Molar mass of gas}(M)}$  ]

or  $p = \frac{W}{V}RT$

or  $p = \frac{VM}{dRT}$  [ Here,  $d = \frac{\text{Mass}}{\text{Volume}}$  ]

$\therefore d = \frac{pM}{RT} = \frac{3 \times 28}{0.082 \times 503} = \frac{84}{41.246} = 2.03 \text{ g/mL}$

## Question 110

The solution which have lowest freezing point is

Options:

A.  $0.2 \text{ M K}_2\text{SO}_4$



B. 0.2M KCl

C. 0.2M NaNO<sub>3</sub>

D. 0.2M MgSO<sub>4</sub>

**Answer: A**

**Solution:**

Solution:

Higher the value of van't Hoff factor (i), higher will be depression in freezing point and lower will be the freezing point of solution.

So, 'i' value,  $0.2\text{M K}_2\text{SO}_4 = 3$

$0.2\text{M KCl} = 2$

$0.2\text{M NaNO}_3 = 2$

$0.2\text{M MgSO}_4 = 2$

Hence,  $0.2\text{M K}_2\text{SO}_4$  will have lowest freezing point.

---

## Question 111

Calculate the molar conductance of 0.025M aqueous solution of calcium chloride at 25°C. The specific conductance of calcium chloride is

$12.04 \times 10^{-2} \text{Sm}^{-1}$

Options:

A.  $4.816 \times 10^{-5} \text{Sm}^2 \text{mol}^{-1}$

B.  $3.816 \times 10^{-5} \text{Sm}^2 \text{mol}^{-1}$

C.  $381.6 \times 10^{-5} \text{Sm}^2 \text{mol}^{-1}$

D.  $481.6 \times 10^{-5} \text{Sm}^2 \text{mol}^{-1}$

**Answer: D**

**Solution:**

Solution:

Molar conductance =  $\lambda_m$

$$\lambda_m = \frac{\kappa \times 10^{-3} \text{ mol}^{-1} \text{ m}^3}{\text{M}} = \frac{(12.04 \times 10^{-2} \text{Sm}^{-1}) \times 10^{-3} (\text{mol}^{-1} \text{m}^3)}{0.025 \text{M}}$$
$$= 481.6 \times 10^{-5} \text{Sm}^2 \text{mol}^{-1}$$

---

## Question 112

For the reaction  $2\text{N}_2\text{O}_5 \rightarrow 4\text{NO}_2 + \text{O}_2$ .

If initial pressure is 100 atm and rate constant k is  $3.38 \times 10^{-5} \text{s}^{-1}$ . After 20 min the final pressure of N<sub>2</sub>O<sub>5</sub> will be

**Options:**

**A. 96 atm**

**B. 50 atm**

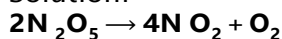
**C. 70 atm**

**D. 60 atm**

**Answer: A**

**Solution:**

Solution:



$$\left[ \begin{array}{ccc} \text{I n i t i a l} & p_0 & 0 \quad 0 \\ \text{F i n a l} & p_0 - 2x & 4x \quad x \end{array} \right]$$

$$k = \frac{2.303}{t} \log \frac{p_0}{p_t}$$
$$3.38 \times 10^{-5} = \frac{2.303}{20 \times 60} \log \frac{100}{p_t}$$

$$0.0176 = \log \frac{100}{p_t}$$

$$p_t = 96 \text{ atm}$$

---

## Question 113

**The difference between heat capacity at constant pressure and heat capacity at constant volume is**

**Options:**

**A. R**

**B.  $\frac{R}{T}$**

**C.  $\frac{R}{V}$**

**D. 1**

**Answer: A**

**Solution:**

Solution:

Heat capacity at constant.

Pressure = **C<sub>p</sub>**

Heat capacity at constant volume = **C<sub>v</sub>**

As we all know,

$$\text{C}_p - \text{C}_v = \text{R}$$

---

## Question 114

Which of the following gas is responsible for acid rain?

Options:

- A. Sulphur dioxide and nitrous oxide
- B. Sulphur dioxide and carbon monoxide
- C. Sulphur dioxide and carbon dioxide
- D. Sulphur dioxide and nitrogen oxide

Answer: D

Solution:

Solution:

Among the given options, sulphur dioxide and nitrogen oxides are responsible for acid rain. It is because sulphur dioxide and nitrogen oxide reacts with water to give sulphuric acid and nitric acid respectively.

---

## Question 115

Which of the following compound does not exists?

Options:

- A.  $\text{NCl}_3$
- B.  $\text{NCl}_5$
- C.  $\text{SbCl}_3$
- D.  $\text{NI}_3$

Answer: B

Solution:

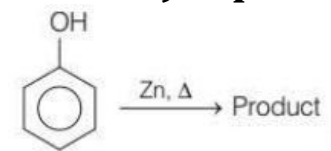
Solution:

N belongs to second period as it has no **d**-orbital. So, five pairs of bonding electrons around nitrogen is not possible. As a result **N Cl<sub>5</sub>** does not exist.

---

## Question 116

The major product in the given reaction is



**Options:**

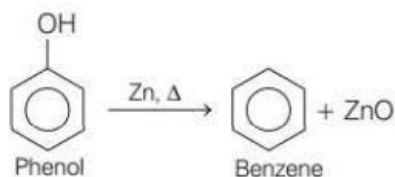
- A. toluene
- B. p-methyl toluene
- C. benzene
- D. o-methyl benzene

**Answer: C**

**Solution:**

Solution:

Phenol is converted to benzene on heating with zine dust.



Hence, benzene is the major product.

---

## Question 117

**The spectrum of  $\text{He}^+$  is similar to**

**Options:**

- A. H
- B.  $\text{Li}^+$
- C. Na
- D.  $\text{He}^+$

**Answer: A**

**Solution:**

Solution:

**As  $\text{H}^+$  and  $\text{He}^+$  contain same number of electron. So, they show same type of spectra.**

---

## Question 118

**The Paschen series of hydrogen spectrum lies in which region?**

**Options:**

- A. UV region
- B. IR region

C. Visible region

D. Microwave region

**Answer: B**

**Solution:**

Solution:

Paschen series of atomic spectrum of hydrogen gas lies in infrared region.

---

## Question 119

The oxidation state of nickel in  $[\text{Ni}(\text{CO})_4]$  is

Options:

A. 1

B. 2

C. 3

D. 0

**Answer: D**

**Solution:**

Solution:

$[\text{Ni}(\text{CO})_4]$

$x + 4(0) = 0$

$x = 0$

Therefore, oxidation state of **Ni** is zero.

---

## Question 120

The correct condition for physical adsorption is

Options:

A. High T and high p

B. High T and low p

C. Low T and high p

D. T and p do not affect

**Answer: C**

**Solution:**

Solution:

Low temperature and high pressure favours physical adsorption because van der Waals' forces of attraction will increase.

---

## Question 121

The value of  $3^{\log_4 5} - 5^{\log_4 3}$  is

Options:

A. 0

B. 1

C. 2

D. 4

Answer: A

Solution:

Solution:

We have,

$$3^{\log_4 5} - 5^{\log_4 3} = 3^{\log_4 5} - 3^{\log_4 5} = 0$$

---

## Question 122

If the tangent to the curve  $xy + ax + by = 0$  at  $(1, 1)$  is inclined at angle  $\tan^{-1} 2$  with X -axis, then

Options:

A.  $a = 1, b = 2$

B.  $a = 1, b = -2$

C.  $a = -1, b = 2$

D.  $a = -1, b = -2$

Answer: B

Solution:

Solution:

Given curve,  $xy + ax + by = 0$  ..... (i)

$(1, 1)$  lie on curve (i)

$\therefore 1 + a + b = 0$  ..... (ii)

From Eq. (i)

$$x \frac{dy}{dx} + y.1 + a + b \frac{dy}{dx} = 0$$

$$\Rightarrow \frac{dy}{dx} = \frac{-(a+y)}{(b+x)}$$

$$\therefore \left( \frac{dy}{dx} \right)_{(1,1)} = \frac{-(a+1)}{b+1} = 2 \text{ (}\because m = \tan \theta \text{)}$$

$\therefore -\frac{(-b)}{b+1} = 2$  [from Eq.(ii)]  
 $\Rightarrow b = 2b + 2$   
 $\therefore b = -2$   
 From Eq.(ii),  $a = 1$   
 Hence,  $a = 1, b = -2$

---

## Question 123

If  $\lim_{x \rightarrow 0} \frac{(1+a^3) + 8e^{1/x}}{1 + (1-b^3)e^{1/x}} = 2$ , then

Options:

- A.  $a = 1, b = 2$
- B.  $a = 1, b = -3^{1/3}$
- C.  $a = 2, b = 3^{1/3}$
- D. None of these

Answer: B

Solution:

Solution:  
 Divide and multiply by  $e^{\frac{1}{x}}$ , then  
 $\lim_{x \rightarrow 0} \frac{(1+a^3) + 8e^{1/x}}{1 + (1-b^3)e^{1/x}} = 2$   
 $\Rightarrow \frac{0+8}{0+1-b^3} = 2 \Rightarrow 1-b^3 = 4 \Rightarrow b^3 = -3$   
 $\Rightarrow b = -3^{1/3}$   
 Then,  $a \in \mathbb{R}$ .

---

## Question 124

If two circles  $(x-1)^2 + (y-3)^2 = r^2$  and  $x^2 + y^2 - 8x + 2y + 8 = 0$

Options:

- A.  $2 < r < 8$
- B.  $r < 2$
- C.  $r = 2$
- D.  $r > 2$

Answer: A

Solution:

Solution:

Centre and radii of the given circles are  $C_1(1, 3)$ ,

$r_1 = r$  and  $C_2(4, -1)$ ,  $r_2 = 3$  respectively. Since, circles intersect in two distinct points, then

$$|r_1 - r_2| < C_1C_2 < r_1 + r_2$$

$$\Rightarrow |r - 3| < 5 < r + 3 \dots\dots\dots (i)$$

From last two relations,  $r > 2$

From first two relations,

$$|r - 3| < 5$$

$$\Rightarrow -5 < r - 3 < 5$$

$$\Rightarrow -2 < r < 8 \dots\dots\dots (ii)$$

$\therefore$  From Eq.(i) and Eq.(ii), we get

$$2 < r < 8$$

## Question 125

The approximate value of  $(0.007)^{1/3}$  is

Options:

A.  $\frac{21}{120}$

B.  $\frac{23}{120}$

C.  $\frac{29}{120}$

D.  $\frac{31}{120}$

Answer: B

Solution:

Solution:

$$\text{Let } \delta(x) = x^{\frac{1}{3}}$$

$$\text{Now, } f(x + \delta x) - f(x) = f'(x)\delta(x) = \frac{\delta x}{3x^{\frac{2}{3}}}$$

We may write  $0.007 = 0.008 - 0.001$

Taking  $x = 0.008$  and  $\delta x = -0.001$

We have,

$$f(0.007) - f(0.008) = \frac{-0.001}{3(0.008)^{\frac{2}{3}}}$$

$$\text{or } f(0.007) - f(0.008) = \frac{-1}{120}$$

$$\therefore f(0.007) = f(0.008) - \frac{1}{120} = 0.2 - \frac{1}{120}$$

$$\Rightarrow (0.007)^{\frac{1}{3}} = \frac{23}{120}$$

## Question 126

The circle  $x^2 + y^2 + 4x - 7y + 12 = 0$  cuts an intercept on Y-axis of length

Options:



- A. 3
- B. 4
- C. 7
- D. 1

**Answer: D**

**Solution:**

Solution:

$$\begin{aligned}\text{Intercept on Y-axis} &= 2\sqrt{f^2 - c} \\ &= 2\sqrt{\frac{49}{4} - 12} = 1\end{aligned}$$

## Question 127

Let  $f(x) = a - (x - 3)^{8/9}$ , then maxima of  $f(x)$  is

Options:

- A. 3
- B.  $a - 3$
- C.  $a$
- D. None

**Answer: C**

**Solution:**

Solution:

$$\begin{aligned}\therefore f(x) &= a - (x - 3)^{\frac{8}{9}} \\ \therefore f'(x) &= 0 - \frac{8}{9}(x - 3)^{-\frac{1}{9}}\end{aligned}$$

At  $x = 3$ ,  $f'(x)$  is not defined.  
Hence,  $x = 3$  is the point of extremum.  
Hence, maximum value of  $f(x) = a$  at  $x = 3$

## Question 128

If the derivative of the function  $f(x) = \begin{cases} bx^2 + ax + 4; & x \geq -1 \\ ax^2 + b; & x < -1 \end{cases}$  is everywhere continuous, then

Options:

**A.  $a = 2, b = 3$**

**B.  $a = 3, b = 2$**

**C.  $a = -2, b = -3$**

**D.  $a = -3, b = -2$**

**Answer: A**

**Solution:**

Solution:

We have,

$$f(x) = \begin{cases} ax^2 + b & x < -1 \\ bx^2 + ax + 4 & x \geq -1 \end{cases}$$

$$\therefore f'(x) = \begin{cases} 2ax & x < -1 \\ 2bx + a & x \geq -1 \end{cases}$$

$\therefore f(x)$  is differentiable at  $x = -1$

$\therefore$  It is continuous at  $x = -1$  and hence

$$\lim_{(x \rightarrow -1^-)} f(x) = \lim_{(x \rightarrow -1^+)} f(x)$$

$$\Rightarrow a + b = b - a + 4$$

$$\Rightarrow a = 2$$

and also,  $\lim_{(x \rightarrow -1^-)} f'(x) = \lim_{(x \rightarrow -1^+)} f'(x)$

$$\Rightarrow -2a = -2b + a$$

$$\Rightarrow 3a = 2b \Rightarrow b = 3 (\because a = 2)$$

$$\text{Hence, } a = 2, b = 3$$

## Question 129

If  $\lim_{x \rightarrow \infty} \left( 1 + \frac{a}{x} + \frac{b}{x^2} \right)^{2x} = e^2$ , then

**Options:**

**A.  $a = 1, b = 2$**

**B.  $a = 2, b = 1$**

**C.  $a = 1, b \in \mathbb{R}$**

**D. None of these**

**Answer: C**

**Solution:**

Solution:

$$\lim_{x \rightarrow \infty} \left( 1 + \frac{a}{x} + \frac{b}{x^2} \right)^{2x} = e^2$$

$$\Rightarrow \lim_{x \rightarrow \infty} \left( 1 + \frac{(ax+b)}{x^2} \right)^2 x = e^2 \dots\dots\dots (i)$$

$\lim_{x \rightarrow \infty} \frac{ax + b}{x^2}$  must be equal to zero.

$$\Rightarrow \lim_{x \rightarrow \infty} \frac{ax + b}{x^2} = 0$$

$$\Rightarrow \lim_{x \rightarrow \infty} \left( \frac{a}{x} + \frac{b}{x^2} \right) = 0$$

$$\therefore a \text{ and } b \in \mathbb{R}$$

$$\text{From Eq. (i), } \lim_{e^{x \rightarrow \infty}} \left( 1 + \frac{ax + b}{x^2} - 1 \right)^{2x} = e^2$$

$$\Rightarrow \lim_{e^{x \rightarrow \infty}} \frac{2(ax + b)}{x} = e^2$$

$$\therefore e^{2a} = e^2$$

$$\Rightarrow a = 1 \text{ and } b \in \mathbb{R}$$

-----

## Question 130

$$S \equiv x^2 + y^2 + 2x + 3y + 1 = 0 \text{ and}$$

$$S' \equiv x^2 + y^2 + 4x + 3y + 2 = 0 \text{ are two circles.}$$

The point  $(-3, -2)$  lies

Options:

A. inside  $S'$  only

B. inside  $S$  only

C. inside  $S$  and  $S'$

D. outside  $S$  and  $S'$

**Answer: A**

**Solution:**

Solution:

$$S(-3, -2) = 9 + 4 - 6 - 6 + 1 = 2 > 0$$

$$\therefore (-3, -2) \text{ outside of } S$$

$$\text{and } S'(-3, -2) = 9 + 4 - 12 - 6 + 2 = -3 < 0$$

$$\therefore (-3, -2) \text{ inside of } S'.$$

-----

## Question 131

The probability of choosing randomly a number  $c$  from the set  $\{1, 2, 3, \dots, 9\}$  such that the quadratic equation  $x^2 + 4x + c = 0$  has real roots, is

Options:

A.  $\frac{1}{9}$

B.  $\frac{2}{9}$

C.  $\frac{3}{9}$

D.  $\frac{4}{9}$

Answer: D

Solution:

Solution:

$$x^2 + 4x + c = 0$$

For real roots,  $D = b^2 - 4ac \geq 0$

$$16 - 4c \geq 0$$

So,  $c = 1, 2, 3, 4$  will satisfy the above inequality.

$$\therefore \text{Required probability} = \frac{4}{9}$$

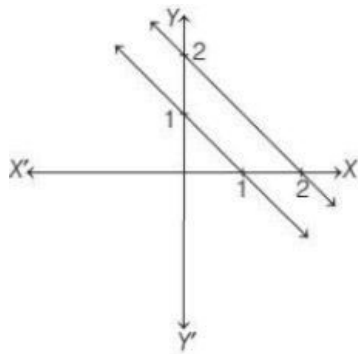
## Question 132

Shade the feasible region for the inequations

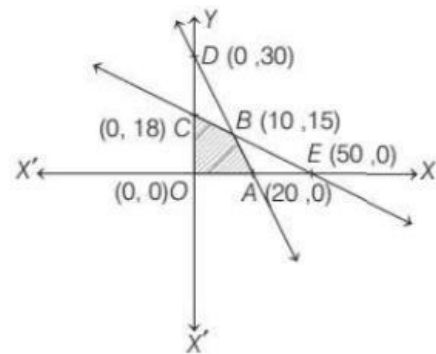
$6x + 4y \leq 120$ ,  $3x + 10y \leq 180$ ,  $x, y \geq 0$  in a rough figure.

Options:

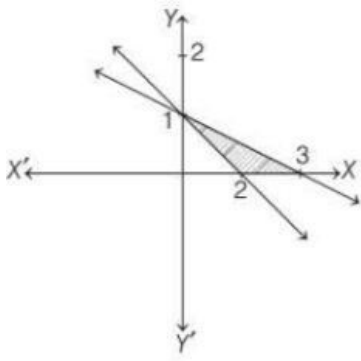
A.



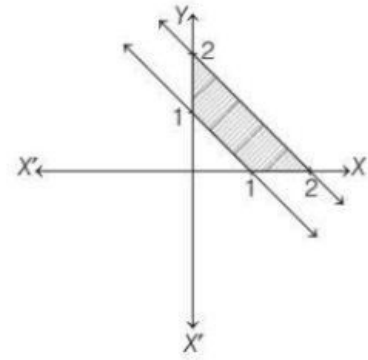
B.



C.



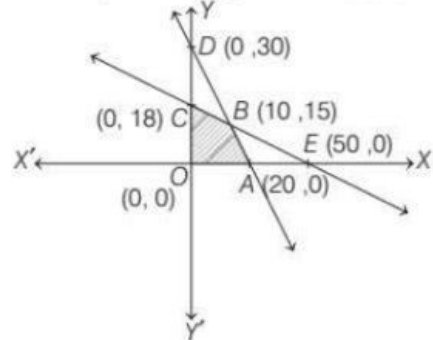
D.



Answer: B

Solution:

Solution:  
 Given constraints are  
 $6x + 4y \leq 120$   
 $3x + 10y \leq 180, x, y > 0$



Here, **OABCO** is the required feasible region whose corner points are **O, A, B** and **C**.

### Question 133

The maximum of  $Z$  is where,  $Z = 4x + 2y$  subject to constraints  $4x + 2y \geq 46, x + 3y \leq 24$  and  $x, y \geq 0$  is

Options:

- A. 46
- B. 96
- C. 52

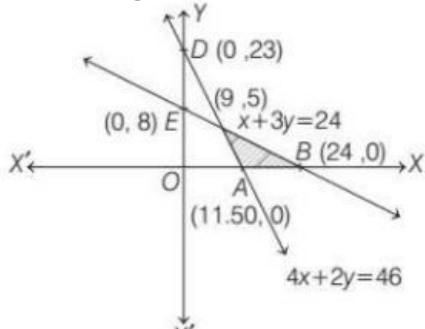
D. None of these

Answer: B

Solution:

Solution:

Feasible region **ABCD** and  **$Z = 4x + 2y$**



At point **C(9, 5)**,  **$Z = 4 \times 9 + 2 \times 5 = 46$**

At point **A(11.5, 0)**  **$Z = 4 \times 11.5 + 2 \times 0 = 46$**

At point **B(24, 0)**,  **$Z = 4 \times 24 + 0 = 26$**

Hence, maximum value of **Z** is **96**.

## Question 134

If for any  $2 \times 2$  square matrix **A**,  **$A(\text{adj } A) = \begin{bmatrix} 8 & 0 \\ 0 & 8 \end{bmatrix}$** , then find the value of **det(A)**.

Options:

A. 6

B. 7

C. 8

D. 5

Answer: C

Solution:

Solution:

$$\text{Given, } A(\text{adj } A) = \begin{bmatrix} 8 & 0 \\ 0 & 8 \end{bmatrix}$$

By using property  **$A(\text{adj } A) = |A| I_n$**

$$\Rightarrow |A| I_n = \begin{bmatrix} 8 & 0 \\ 0 & 8 \end{bmatrix}$$

$$\Rightarrow |A| I_n = 8 \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \Rightarrow |A| = 8$$

---

## Question 135

If  $\mathbf{A} = \begin{bmatrix} a & 0 & 0 \\ 0 & a & 0 \\ 0 & 0 & a \end{bmatrix}$ , then  $|\mathbf{A}| \operatorname{adj} \mathbf{A}|$  is equal to

Options:

A.  $a^{3n}$

B.  $a^{-3n}$

C.  $-a^{3n}$

D.  $2a^{3n}$

**Answer: A**

**Solution:**

Solution:

$$\text{Given, } \mathbf{A} = \begin{bmatrix} a & 0 & 0 \\ 0 & a & 0 \\ 0 & 0 & a \end{bmatrix}$$

Now,  $|\mathbf{A}| = a^3$

$$\therefore |\mathbf{A}| |\operatorname{adj} \mathbf{A}| = |\mathbf{A}| |\mathbf{A}|^{n-1} = (a^3)^n = a^{3n}$$

---

## Question 136

If  $\mathbf{A} = \begin{bmatrix} 2-k & 2 \\ 1 & 3-k \end{bmatrix}$  is a singular matrix, then the value of  $5k - k^2$  is

Options:

A. 0

B. 6

C. -6

D. 4

**Answer: D**

**Solution:**

Solution:

$$\text{Given, } \mathbf{A} = \begin{bmatrix} 2-k & 2 \\ 1 & 3-k \end{bmatrix}$$

Since, the Matrix A is singular

$$\therefore |\mathbf{A}| = 0$$

$$\Rightarrow \mathbf{A} = \begin{bmatrix} 2-k & 2 \\ 1 & 3-k \end{bmatrix} = 0$$

$$\Rightarrow (2-k)(3-k) - 2 = 0$$

$$\Rightarrow 6 - 5k + k^2 - 2 = 0$$

$$\Rightarrow 4 - 5k + k^2 = 0$$

$$\Rightarrow 5k - k^2 = 4$$

---

## Question 137

If  $\theta$  be the angle between the vectors  $\mathbf{a} = 2\hat{i} + 2\hat{j} - \hat{k}$  and  $\mathbf{b} = 6\hat{i} - 3\hat{j} + 2\hat{k}$ , then

Options:

A.  $\cos \theta = \frac{4}{21}$

B.  $\cos \theta = \frac{3}{19}$

C.  $\cos \theta = \frac{2}{19}$

D.  $\cos \theta = \frac{5}{21}$

**Answer: A**

**Solution:**

Solution:

$$\begin{aligned} \cos \theta &= \frac{\mathbf{a} \cdot \mathbf{b}}{|\mathbf{a}| |\mathbf{b}|} \\ &= \frac{(2\hat{i} + 2\hat{j} - \hat{k}) \cdot (6\hat{i} - 3\hat{j} + 2\hat{k})}{\sqrt{2^2 + 2^2 + (-3)^2} \sqrt{6^2 + (-3)^2 + 2^2}} \\ &= \frac{12 - 6 - 2}{\sqrt{4 + 4 + 1} \sqrt{36 + 9 + 4}} = \frac{4}{21} \end{aligned}$$

---

## Question 138

If  $x, y$  and  $z$  are non-zero real numbers and  $\mathbf{a} = x\hat{i} + 2\hat{j}$ ,  $\mathbf{b} = y\hat{j} + 3\hat{k}$  and  $\mathbf{c} = x\hat{i} + y\hat{j} + z\hat{k}$  are such that  $\mathbf{a} \times \mathbf{b} = \mathbf{z}\hat{i} - 3\hat{j} + \hat{k}$ , then  $[abc]$  is equal to

Options:

A. 3

B. 10

C. 9

D. 6

**Answer: C**



## Solution:

Solution:

Given;  $\mathbf{a} = x\hat{i} + 2\hat{j}$ ,  $\mathbf{b} = u\hat{j} + 3\hat{k}$  and  $\mathbf{c} = x\hat{i} + y\hat{j} + z\hat{k}$

$$\begin{aligned}\text{Now, } \mathbf{a} \times \mathbf{b} &= \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ x & 2 & 0 \\ 0 & y & 3 \end{vmatrix} \\ &= \hat{i}(6 - 0) - \hat{j}(3x - 0) + \hat{k}(xy - 0) \\ &= 6\hat{i} - 3x\hat{j} + xy\hat{k} \\ &= 6\hat{i} = 3x\hat{j} + xy\hat{k} = z\hat{i} - 3\hat{j} + \hat{k}\end{aligned}$$

On equating the coefficients of  $\hat{i}$ ,  $\hat{j}$  and  $\hat{k}$ , we get

$$z = 6, x = 1 \text{ and } xy = 1$$

$$\therefore xy = 1, y = 1$$

$$\Rightarrow \mathbf{a} = \hat{i} + 2\hat{j}, \mathbf{b} = \hat{j} + 3\hat{k}$$

$$\text{and } \mathbf{c} = \hat{i} + \hat{j} + 6\hat{k}$$

$$\begin{aligned}\therefore [\mathbf{abc}] &= \begin{vmatrix} 1 & 2 & 0 \\ 0 & 1 & 3 \\ 1 & 1 & 6 \end{vmatrix} \\ [\mathbf{abc}] &= 1(6 - 3) - 2(0 - 3) + 0 = 3 + 6 = 9\end{aligned}$$

---

## Question 139

Maximum value of  $z = 12x + 3y$ , subject to constraints  $x \geq 0$ ,  $y \geq 0$ ,  $x + y \leq 5$  and  $3x + y \leq 9$  is

Options:

A. 15

B. 36

C. 60

D. 40

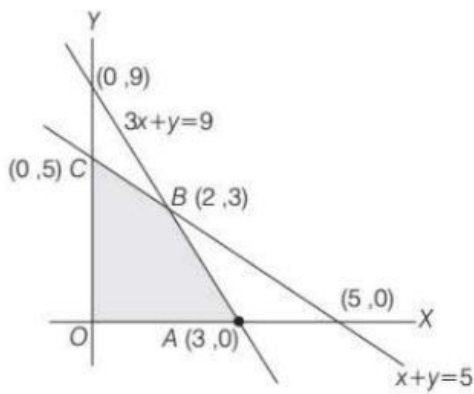
Answer: B

## Solution:

Solution:

Given, constraints are  $x \geq 0$ ,  $y \geq 0$ ,  $x + y \leq 5$  and  $3x + y \leq 9$  and  $z = 12x + 3y$

Here, feasible region is **OABCO**.



At point **O(0, 0)**,  $z = 12(0) + 3(0) = 0$

At point **A(3, 0)**,  $z = 12(3) + 3(0) = 36$

At point **B(2, 3)**,  $z = 12(2) + 3(3) = 33$

At point **C(0, 5)**,  $z = 12(0) + 3(5) = 15$

Hence, maximum value of **z** is **36**.

## Question 140

If  $\mathbf{p} = \hat{i} + \hat{j}$ ,  $\mathbf{q} = 4\hat{k} - \hat{j}$  and  $\mathbf{r} = \hat{i} + \hat{k}$ , then the unit vector in the direction of  $3\mathbf{p} + \mathbf{q} - 2\mathbf{r}$  is

Options:

A.  $\frac{1}{3}(\hat{i} + 2\hat{j} + 2\hat{k})$

B.  $\frac{1}{3}(\hat{i} - 2\hat{j} - 2\hat{k})$

C.  $\frac{1}{3}(\hat{i} - 2\hat{j} + 2\hat{k})$

D.  $\hat{i} + 2\hat{j} + 2\hat{k}$

**Answer: A**

**Solution:**

Solution:

$$3\mathbf{p} + \mathbf{q} - 2\mathbf{r}$$

$$= 2(\hat{i} + \hat{j}) + (4\hat{k} - \hat{j}) - 2(\hat{i} + \hat{k})$$

$$= \hat{i} + 2\hat{j} + 2\hat{k}$$

$\therefore$  Unit vector in the director of

$$3\mathbf{p} + \mathbf{q} - 2\mathbf{r} = \frac{1}{3}(\hat{i} + 2\hat{j} + 2\hat{k})$$

## Question 141

The line  $\frac{x-3}{-4} = \frac{y-4}{5} = \frac{z-5}{6}$  is parallel to the plane

Options:

A.  $3x + 4y + 5z = 7$

**B.  $x + y + z = 2$**

**C.  $x - 2y + z = 0$**

**D.  $2x + 3y + 4z = 0$**

**Answer: C**

**Solution:**

Solution:

Given equation of line is

$$\frac{x-3}{4} = \frac{y-4}{5} = \frac{z-5}{6}$$

So, DR's of line are (4, 5, 6)

Since, line is parallel to the plane, therefore the normal to plane is perpendicular to the line.

$$\therefore a_1a_2 + b_1b_2 + c_1c_2 = 0$$

Consider the plane is

$$x - 2y + z = 0$$

Here,  $a_2 = 1$ ,  $b_2 = -2$ ,  $c_1$

So,  $a_1a_2 + b_1b_2 + c_1c_2$

$$= (4 \times 1) + (5 \times -2) + (6 \times 1) = 4 - 10 + 6$$

$$= 10 - 10 = 0$$

Hence, required plane is

$$x - 2y + z = 0$$

So, option (c) is correct.

## Question 142

$$\int \frac{1}{x\sqrt{ax-x^2}} dx \text{ is}$$

**Options:**

**A.  $\frac{-3}{a} \sqrt{\frac{a-x}{x}} + C$**

**B.  $-\frac{2}{a} \sqrt{\frac{x}{a-x}} + C$**

**C.  $\frac{-2}{a} \sqrt{\frac{a-x}{x}} + C$**

**D. None of these**

**Answer: C**

**Solution:**

Solution:

$$\text{Let } I = \int \frac{1}{x\sqrt{ax-x^2}} dx$$

$$\text{Putting } x = \frac{a}{t}$$

$$\Rightarrow dx = \frac{-a}{t^2} dt$$

$$\begin{aligned}
 \therefore I &= \int \frac{1}{a - \frac{a}{a^2}x - \frac{a}{t}} dt \\
 &= \int \frac{t \sqrt{a - \frac{a}{t^2}}}{t^2 \sqrt{\frac{a^2}{t} - \frac{a^2}{t^2}}} dt \\
 &= \int \frac{-1}{\sqrt{1 - \frac{1}{t^2}}} dt \\
 &\quad \text{at } 1 = 1 \\
 &= -\frac{1}{a} \int \frac{1}{\sqrt{1 - \frac{1}{t^2}}} dt \\
 &= -\frac{1}{a} \int \frac{1}{\sqrt{t-1}} dt = -\frac{1}{a} \int (t-i)^{-\frac{1}{2}} dt \\
 &= -\frac{1}{a} \frac{(t-1)^{\frac{1}{2}}}{\frac{1}{2}} + C = -\frac{2}{a} \left( \frac{a}{x} - 1 \right)^{\frac{1}{2}} + C \\
 I &= -\frac{2}{a} \sqrt{\frac{a-x}{x}} + C
 \end{aligned}$$

Option (c) is correct.

## Question 143

3.  $\int \frac{3^x}{\sqrt{1-9^x}} dx$  is equal to

Options:

A.  $(\log 3) \sin^{-1} 3^x + C$

B.  $\frac{1}{3} \sin^{-1}(3^x) + C$

C.  $\frac{1}{\log 3} \sin^{-1} 3^x + C$

D.  $3 \log 3 \sin^{-1} 3^x + C$

**Answer: C**

**Solution:**

Solution:

We have,  $I = \int \frac{3^x}{\sqrt{1-9^x}} dx = \int \frac{3^x}{\sqrt{1-(3^x)^2}} dx$

Putting  $3^x = t$

$\Rightarrow 3^x \log 3 dx = dt$

$\Rightarrow 3^x dx = \frac{1}{\log 3} dt$

$\therefore I = \frac{1}{\log 3} \int \frac{1}{\sqrt{1-t^2}} dt$

$= \frac{1}{\log 3} \sin^{-1} t + C$

$= \frac{1}{\log 3} \sin^{-1}(3^x) + C$

Option (c) is correct.

## Question 144

$$\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \cos x \, dx$$

Options:

A. 2

B. 0

C. -1

D. 5

**Answer: A**

**Solution:**

Solution:

Here  $f(x) = \cos x$

$f(-x) = \cos(-x) = \cos x = f(x)$

So,  $f$  is even function.

$$\therefore \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \cos x \, dx = 2 \int_0^{\frac{\pi}{2}} \cos x \, dx$$

$$[\because \int_{-a}^a f(x) \, dx = 2 \int_0^a f(x) \, dx, \text{ if } f \text{ is even}]$$

$$= 2 [\sin x]_0^{\frac{\pi}{2}}$$

$$= 2 \left[ \sin \frac{\pi}{2} - \sin 0 \right] = 2[1 - 0] = 2$$

---

## Question 145

The angle between the lines  $\frac{x+4}{-3} = \frac{y-1}{5} = \frac{z+3}{4}$  and  $\frac{x+1}{1} = \frac{y-4}{1} = \frac{z-5}{2}$  is

Options:

A.  $30^\circ$

B.  $\cos^{-1} \left( \frac{3}{2\sqrt{2}} \right)$

C.  $\cos^{-1} \left( \frac{8}{5\sqrt{3}} \right)$

D. None of these

**Answer: C**

**Solution:**

Solution:

The angle between two lines

$$\frac{x-x_1}{a_1} = \frac{y-y_1}{b_1} = \frac{z-z_1}{c_1} \text{ and } \frac{x-x_2}{a_2} = \frac{y-y_2}{b_2} = \frac{z-z_2}{c_2}$$

is given by

$$\begin{aligned}\cos\theta &= \frac{a_1a_2 + b_1b_2 + c_1c_2}{\sqrt{a^2 + b^2 + c^2} \sqrt{a^2 + b^2 + c^2}} \\ &= \frac{3 \times 1 + 5 \times 1 + 4 \times 2}{\sqrt{3^2 + 5^2 + 4^2} \sqrt{1^2 + 1^2 + 2^2}} \\ &= \frac{16}{\sqrt{50}\sqrt{6}} = \frac{16}{\sqrt{300}} \\ \Rightarrow \cos\theta &= \frac{16}{10\sqrt{3}} \\ \Rightarrow \cos\theta &= \frac{8}{5\sqrt{3}} \\ \Rightarrow \theta &= \cos^{-1}\left(\frac{8}{5\sqrt{3}}\right)\end{aligned}$$

So, option (c) is correct.

## Question 146

.The point of intersection of the lines  $\frac{x-1}{-1} = \frac{y-1}{2} = \frac{z-2}{3}$  and  $\frac{x-5}{2} = \frac{y-2}{1} = z$  is

Options:

A. (1, -2, 0)

B. (3, 1, 0)

C. (-2, -5, -7)

D. None of these

**Answer: D**

**Solution:**

Solution:

Given lines are

$$\frac{x-1}{1} = \frac{y-1}{2} = \frac{z-2}{3} = \lambda \text{ (let)}$$

$$\Rightarrow x = \lambda + 1, y = 2\lambda + 1, z = 3\lambda + 2$$

$$\text{and } \frac{x-5}{2} = \frac{y-2}{1} = z = \mu \text{ (let)}$$

$$\Rightarrow x = 2\mu + 5, y = \mu + 2, z = \mu$$

For point of intersection, we have

$$\lambda + 1 = 2\mu + 5 \text{ and } 2\lambda + 1 = \mu + 2 \text{ and } 3\lambda + 2 = \mu$$

$$\lambda - 2\mu = 4 \dots\dots\dots \text{(i)}$$

$$2\lambda - \mu = 1 \dots\dots\dots \text{(ii)}$$

$$3\lambda - \mu = -2 \dots\dots\dots \text{(iii)}$$

On solving Eqs. (ii) and (iii), we get

$$2\lambda - \mu = 1$$

$$3\lambda - \mu = -2$$

$$- \quad + \quad + \quad \text{So, } \mu = -7$$

$$-\lambda = 3$$

$$\lambda = -3$$

Now, put  $\lambda = -3$  and  $\mu = -7$  in Eq. (i), we get

$$-3 + 14 = 11 \neq 4$$

Hence, the lines do not intersect.

Hence, option (d) is correct.

---

## Question 147

Five persons A, B, C, D and E are in queue of a shop. The Probability that A and B are always together is

Options:

A.  $\frac{2}{5}$

B.  $\frac{1}{4}$

C.  $\frac{3}{5}$

D.  $\frac{2}{3}$

Answer: A

Solution:

Solution:

Given, 5 persons are in a queue of a shop. **A** and **B** itself can arrange in two ways therefore number of arrangement for **A** and **B** =  $2! = 2$  So, probability that **A** and **B** are always together

$$= \frac{2! \times 4!}{5!} = \frac{2 \times 4!}{5 \times 4!} = \frac{2}{5}$$

Option (a) is correct.

---

## Question 148

If the probability for A to fail in an examination is 0.2 and that for B is 0.3 , then the probability that either A or B fail is

Options:

A. 0.38

B. 0.44

C. 0.50

D. 0.94

Answer: B

Solution:

Solution:

$$P(A) = 0.2, P(B) = 0.3$$

$$\therefore P(A) = 0.8, P(B) = 0.7$$

$\therefore$  Required probability

$$= P(A)P(B) + P(A)P(B) + P(A)P(B)$$

$$= 0.2 \times 0.7 + 0.8 \times 0.3 + 0.2 \times 0.3$$

$$= 0.44$$

---

## Question 149

Three vertices are chosen randomly from the seven vertices of a regular 7-sided polygon. The probability that they form the vertices of an isosceles triangle is

Options:

A.  $\frac{1}{7}$

B.  $\frac{1}{3}$

C.  $\frac{3}{7}$

D.  $\frac{3}{5}$

**Answer: D**

**Solution:**

Solution:

Number of triangles formed  $= {}^7C_3$

Number of isosceles triangles  $= 7 \times 3 = 21$

$$\text{So, probability} = \frac{21}{{}^7C_3} = \frac{21}{\frac{7!}{3!(7-3)!}}$$

$$= \frac{21 \times 3! \times 4!}{7 \times 6 \times 5 \times 4!} = \frac{3}{5}$$

Option (d) is correct.

---

## Question 150

If A, B and C are three mutually exclusive and exhaustive events such that  $P(A) = 2P(B) = 3P(C)$ . What is  $P(B)$  ?

Options:

A.  $\frac{6}{11}$

B.  $\frac{6}{22}$

C.  $\frac{1}{6}$

D.  $\frac{1}{3}$

**Answer: B**

**Solution:**



Solution:

Given that **A**, **B** and **C** are three mutually exclusive events

$$\Rightarrow P(A) = 2P(B) = 3P(C)$$

$$P(A \cup B \cup C) = P(A) + P(B) + P(C)$$

$$= 2P(B) + P(B) + \frac{2}{3}P(B)$$

$$= \frac{11}{3}P(B)$$

$$\because P(A \cup B \cup C) = 1$$

$$\Rightarrow \frac{11}{3}P(B) = 1 \Rightarrow P(B) = \frac{3}{11}$$

$$\Rightarrow P(B) = \frac{6}{22}$$

## Question 151

If  $U_{n+1} = 3U_n - 2U_{n-1}$  and  $U_0 = 2, U_1 = 3$ , then  $U_n$  is equal to

Options:

A.  $1 - 2^n$

B.  $2^n + 1$

C.  $2^n - 1$

D.  $2^n + 2$

Answer: B

Solution:

Solution:

We know that  $U_{n+1} = 3U_n - 2U_{n-1}$ .....(i)

Step I Given,  $U_1 = 3 = 2 + 1 = 2 + 1$ , which is true for

$n = 1$ , put  $n = 1$  in Eq.(i),

Then  $U_{1+1} = 3U_1 - 2U_{1-1}$

$$\Rightarrow U_2 = 3U_1 - 2U_0$$

$$= 3 \times 3 - 2 \times 2 = 5 = 2^2 + 1$$

Which is true for  $n = 2$

$\therefore$  The result are true for  $n = 1$  and  $n = 2$

Step II Assume it is true for  $n = k$ , then it is also true for

$$n = k - 1$$

Then,  $U_k = 2^k + 1$ .....(ii)

and  $U_{k-1} = 2^{k-1} + 1$ ..... (iii)

Step III On putting  $n = k$  in Eq.(i), we get

$$U_{k+1} = 3U_k - 2U_{k-1}$$

$$= 3(2^k + 1) - 2(2^{k-1} + 1) \text{ [From Eqs. (ii) and (iii)]}$$

$$= 3 \cdot 2^k + 3 - 2 \cdot 2^{k-1} - 2$$

$$= 3 \cdot 2^k + 3 - 2^k - 2$$

$$= (3 - 1)2^k + 1$$

$$= 2 \cdot 2^k + 1 = 2^{k+1} + 1$$

This shows that the result is true for  $n = k + 1$ . Hence by the principle of mathematical induction the result is true for all  $n \in \mathbb{N}$ .

## Question 152

If  $4^n + 15n + P$  is divisible by 9 for all  $n \in \mathbb{N}$ , then the least negative

integral value of P is

Options:

- A. -1
- B. -2
- C. -3
- D. -4

Answer: A

Solution:

Solution:

We have,  $P(n) = 4^n + 15n + P$

For  $n = 1$ ,  $P(1) = 4 + 15 + p = 19 + p$  is divisible by 9.

Thus, P should be -1.

Since,  $19 - 1 = 18$  is divisible by 9.

---

## Question 153

$(2^{3n} - 1)$  is divisible by

Options:

- A. 6
- B. 7
- C. 8
- D. 9

Answer: B

Solution:

Solution:

For  $n = 1$ ,  $2^{3n} - 1$  has value  $2^3 - 1 = 7$

For  $n = 2$ ,  $2^{3n} - 1$  has value  $2^6 - 1 = 63 = 7 \times 9$

which is divisible by 7 not by 6 or 8 or 9.

Hence, option (b) is correct.

---

## Question 154

If  $S = \frac{2^2 - 1}{2} + \frac{3^2 - 2}{6} + \frac{4^2 - 3}{12} + \dots$  upto 10 terms, then S is equal to

Options:

- A.  $\frac{120}{11}$

B.  $\frac{13}{11}$

C.  $\frac{110}{11}$

D.  $\frac{19}{11}$

**Answer: A**

**Solution:**

Solution:  $\frac{(n+1)^2 - n}{n(n+1)}$

We know,  $T_n =$

$$= 1 + \left( \frac{1}{n} - \frac{1}{n+1} \right)$$

$$\therefore S_{10} = 10 + \left( 1 - \frac{1}{11} \right) = \frac{120}{11}$$

## Question 155

$\sum_{n=1}^m n \cdot n!$  is equal to

**Options:**

A.  $m! - 1$

B.  $(m-1)! - 1$

C.  $(m+1)! - 1$

D.  $m!(m-1)!$

**Answer: C**

**Solution:**

Solution:

We have,  $n \cdot n!$

$$= (n+1-1) \cdot n!$$

$$= (n+1)! - n!$$

$$= V(n) - V(n-1)$$

$$\Rightarrow \sum_{n=1}^m n(n!) = V(m) - V(0) = (m+1)! - 1$$

## Question 156

**.The first and fifth terms of an A.P. are -14 and 2 respectively and the sum of its n terms is 40 . The value of n is**

**Options:**

A. 8

- B. 12
- C. 10
- D. 13

**Answer: C**

**Solution:**

Solution:

We have,

$$a = -14 \text{ and } a + 4d = 2$$

$$\Rightarrow -14 + 4d = 2 \Rightarrow 4d = 14 + 2$$

$$\Rightarrow 4d = 16$$

$$\therefore d = 4$$

$$\text{Now, } S_n = \frac{n}{2}[2a + (n-1)d]$$

$$\Rightarrow 40 = \frac{n}{2}[-28 + (n-1)4]$$

$$\Rightarrow n^2 - 8n - 20 = 0$$

$$\Rightarrow (n-10)(n+2) = 0$$

$$\Rightarrow n = 10$$

## Question 157

The solution of the differential equation  $\frac{d^2y}{dx^2} = 0$  represents

**Options:**

- A. all circles in a plane
- B. all straight lines in a plane
- C. all parabolas in a plane
- D. all ellipses in a plane

**Answer: B**

**Solution:**

Solution:

$$\text{Given, differential equation is } \frac{d^2y}{dx^2} = 0$$

On integrating, we get

$$\frac{dy}{dx} = c, \text{ where } c \text{ is a constant}$$

$$\Rightarrow dy = c dx$$

Again integrating,

$$\Rightarrow \int dy = c \int dx$$

$$\Rightarrow y = cx + d, \text{ where } d \text{ is constant.}$$

$\therefore$  The solution of differential equation represents all straight lines in a plane.

## Question 158

.The solution of the differential equation  $\frac{dy}{dx} + \sqrt{\frac{1-y^2}{1-x^2}} = 0$  is

Options:

A.  $\cos^{-1}x + \cos^{-1}y = c$

B.  $\sin^{-1}x + \sin^{-1}y = c$

C.  $\cosh^{-1}x + \cosh^{-1}y = c$

D.  $\sinh^{-1}x + \sinh^{-1}y = c$

Answer: B

Solution:

Solution:

Given,  $\frac{dy}{dx} + \frac{\sqrt{1-y^2}}{\sqrt{1-x^2}} = 0$

$\Rightarrow \frac{dy}{\sqrt{1-y^2}} + \frac{dx}{\sqrt{1-x^2}} = 0$

On integrating, we get

$\Rightarrow \int \frac{dy}{\sqrt{1-y^2}} + \int \frac{dx}{\sqrt{1-x^2}} = 0$

$\Rightarrow \sin^{-1}y + \sin^{-1}x = c$

## Question 159

.The solution of the differential equation  $x \frac{dy}{dx} = \cot y$  is

Options:

A.  $y \cos x = c$

B.  $x \cos y = c$

C.  $\log(x \cos y) = c$

D.  $\log(y \cos x) = c$

Answer: B

Solution:

Solution:

Given,  $x \frac{dy}{dx} = \cot y$

$\Rightarrow \tan y \, dy = \frac{dx}{x}$

On integrating, we get

$\Rightarrow \int \tan y \, dy = \int \frac{dx}{x}$

$\Rightarrow \log \sec y = \log x + \log c_1$

$\Rightarrow \log \sec y = \log x \cdot c_1$

$\Rightarrow \sec y = x \cdot c_1$

$$\Rightarrow x \cos y = c,$$

Where  $c = \frac{1}{c_1}$

---

## Question 160

If  ${}^nC_3 = 220$ , then  $n = ?$

Options:

- A. 11
- B. 12
- C. 10
- D. 9

**Answer: B**

**Solution:**

Solution:

We have,  ${}^nC_3 = 220$

$$\Rightarrow \frac{n(n-1)(n-2)}{6} = 220$$

$$\Rightarrow n(n-1)(n-2) = 1320$$

$$\Rightarrow n = 12 [\because 12 \times 11 \times 10 = 1320]$$


---

## Question 161

A multiple choice examination has 5 questions. Each question has three alternative answers of which exactly one is correct. The probability that a student will get 4 or more correct answer just by guessing, is

Options:

- A.  $\frac{13}{3^5}$
- B.  $\frac{11}{3^5}$
- C.  $\frac{10}{3^5}$
- D.  $\frac{17}{3^5}$

**Answer: B**

**Solution:**

Solution:

Total number of questions,  $n = 5$

Probability of correct answer,  $p = \frac{1}{3}$   
 Probability of incorrect answer,  $q = \frac{2}{3}$

$$\begin{aligned}\text{Required probability} &= P(x \geq 4) \\ &= P(x = 4) + P(x = 5) \\ &= {}^5C_4 \times \left(\frac{1}{3}\right)^4 \times \left(\frac{2}{3}\right)^1 + {}^5C_5 \times \left(\frac{1}{3}\right)^5 \times \left(\frac{2}{3}\right)^0 \\ &= \frac{10}{3^5} + \frac{1}{3^5} = \frac{11}{3^5}\end{aligned}$$

## Question 162

If  $\sin A + \sin B = a$  and  $\cos A + \cos B = b$ , then  $\cos(A + B)$  equals?

Options:

- A.  $\frac{a^2 + b^2}{b^2 - a^2}$
- B.  $\frac{2ab}{a^2 + b^2}$
- C.  $\frac{b^2 - a^2}{a^2 + b^2}$
- D.  $\frac{a^2 - b^2}{a^2 + b^2}$

**Answer: C**

**Solution:**

Solution:

Given,  $\sin A + \sin B = a$  ..... (i)

$\cos A + \cos B = b$  ..... (ii)

Dividing Eq.(i) by Eq. (ii), we get

$$\begin{aligned}\frac{\sin A + \sin B}{\cos A + \cos B} &= \frac{a}{b} \\ \Rightarrow \frac{2\sin\left(\frac{A+B}{2}\right)\cos\left(\frac{A-B}{2}\right)}{2\cos\left(\frac{A+B}{2}\right)\cos\left(\frac{A-B}{2}\right)} &= \frac{a}{b} \\ \Rightarrow \tan\frac{A+B}{2} &= \frac{a}{b} \text{ ..... (iii)}\end{aligned}$$

$$\text{Now, } \cos(A+B) = \frac{1 - \tan^2\left(\frac{A+B}{2}\right)}{1 + \tan^2\left(\frac{A+B}{2}\right)} \left( \because \cos \theta = \frac{1 - \tan^2\frac{\theta}{2}}{1 + \tan^2\frac{\theta}{2}} \right)$$

$$\Rightarrow \cos(A+B) = \frac{1 - \frac{a^2}{b^2}}{1 + \frac{a^2}{b^2}} \text{ [using Eq.(iii)]}$$

$$\therefore \cos(A+B) = \frac{b^2 - a^2}{b^2 + a^2}$$

## Question 163

What is  $\frac{\cos \theta}{1 - \tan \theta} + \frac{\sin \theta}{1 - \cot \theta}$  equal to?

Options:

A.  $\sin \theta - \cos \theta$

B.  $2 \sin \theta$

C.  $\sin \theta + \cos \theta$

D.  $2 \cos \theta$

**Answer: C**

**Solution:**

Solution:

$$\begin{aligned} \frac{\cos \theta}{1 - \tan \theta} + \frac{\sin \theta}{1 - \cot \theta} &= \frac{\cos \theta}{1 - \frac{\sin \theta}{\cos \theta}} + \frac{\sin \theta}{1 - \frac{\cos \theta}{\sin \theta}} \\ &= \frac{\cos^2 \theta}{\cos^2 \theta - \sin \theta} + \frac{\sin^2 \theta}{\sin^2 \theta - \cos \theta} \\ &= \frac{\cos \theta - \sin \theta}{\cos^2 \theta} + \frac{\sin \theta - \cos \theta}{\sin^2 \theta} \\ &= \frac{\cos \theta - \sin \theta}{\cos^2 \theta - \sin^2 \theta} - \frac{\cos \theta - \sin \theta}{\cos^2 \theta - \sin^2 \theta} \\ &= \frac{\cos \theta - \sin \theta}{\cos^2 \theta - \sin^2 \theta} \\ &= \frac{(\cos \theta + \sin \theta)(\cos \theta - \sin \theta)}{(\cos \theta - \sin \theta)} \end{aligned}$$

[Using identity  $a^2 - b^2 = (a + b)(a - b)$ ]  
 $= \sin \theta + \cos \theta$

## Question 164

Find the general solution of  $\sin 2x + \cos x = 0$ .

Options:

A.  $(n \pm 1) \frac{\pi}{2}$

B.  $n\pi \pm \frac{\pi}{2}$

C.  $n\pi + (-1)^n \frac{7\pi}{6}$  or  $(2n \pm 1) \frac{\pi}{2}$

D. None of the above

**Answer: C**

**Solution:**

Solution:

$$\begin{aligned} \sin 2x + \cos x &= 0 \\ \Rightarrow 2 \sin x \cos x + \cos x &= 0 \\ \Rightarrow \cos x (2 \sin x + 1) &= 0 \\ \Rightarrow \cos x = 0 \text{ or } 2 \sin x + 1 &= 0 \\ \Rightarrow \cos x = \cos \frac{\pi}{2} \Rightarrow x = n\pi \pm \frac{\pi}{2}, n \in \mathbb{Z} \end{aligned}$$



$$\begin{aligned}\text{or } \sin x &= -\frac{1}{2} = -\sin\left(\frac{\pi}{6}\right) \\ &= \sin\left(\pi + \frac{\pi}{6}\right) \\ \Rightarrow \sin x &= \sin\left(\frac{7\pi}{6}\right) \\ \therefore x &= n\pi + (-1)^n \frac{7\pi}{6}, n \in \mathbb{Z}\end{aligned}$$


---

## Question 165

If  $f(x) + 2f(1 - x) = x^2 + 5 \forall$  real values of  $x$  then  $f(x)$  is given by

Options:

- A.  $x^2 - 5$
- B. 2
- C.  $\frac{(x-2)^2 + 3}{3}$
- D. None of these

**Answer: C**

**Solution:**

$$\begin{aligned}\text{Solution:} \\ \text{Given, } f(x) + 2f(1 - x) &= x^2 + 5 \dots\dots\dots (i) \\ \text{Replace } x &\rightarrow 1 - x \\ \therefore f(1 - x) + 2f(x) &= (1 - x)^2 + 5 \dots\dots\dots (ii) \\ \text{Multiplying Eq. (ii) by 2 and subtracting Eq. (i) from it} \\ \Rightarrow 2f(1 - x) + 4f(x) - f(x) - 2f(1 - x) \\ &= 2(10x)^2 + 5 \times 2 - x^2 - 5 \\ \Rightarrow 3f(x) &= \frac{2(x^2 - 2x + 1) - x^2 + 5}{(x-2)^2 + 3} = x^2 - 4x + 7 \\ \therefore f(x) &= \frac{\quad}{3}\end{aligned}$$


---

## Question 166

If  $A = \{3, 5, 7\}$  and  $B = \{1, 2, 3, 5\}$ , then  $A \times B \cap B \times A$  is equal to

Options:

- A.  $\{(3, 3), (5, 3), (2, 7), (7, 2)\}$
- B.  $\{(3, 3), (3, 5), (5, 3), (5, 5)\}$
- C.  $\{(3, 3), (5, 5)\}$
- D.  $\{(3, 5), (5, 5), (5, 3)\}$

**Answer: B**

**Solution:**

Solution:

$$\begin{aligned}\mathbf{A} \times \mathbf{B} &= \{ (3, 1), (3, 2), (3, 3), (3, 5), (5, 1), (5, 2), (5, 3), (5, 5), (7, 1), (7, 2), (7, 3), (7, 5) \} \\ \mathbf{B} \times \mathbf{A} &= \{ (1, 3), (1, 5), (1, 7), (3, 3), (3, 5), (2, 7), (3, 3), (3, 5), (3, 7), (5, 3), (5, 5), (5, 7) \} \\ \therefore \mathbf{A} \times \mathbf{B} \cap \mathbf{B} \times \mathbf{A} &= \{ (3, 3), (3, 5), (5, 3), (5, 5) \}\end{aligned}$$

---

## Question 167

Total number of elements in the power set of A containing 17 elements is

Options:

- A.  $2^{17+1}$
- B.  $2^{17-1}$
- C.  $17^2 - 1$
- D.  $2^{17}$

Answer: D

Solution:

Solution:

For a given set **A** with **n** elements, number of elements in power set **P(A)** is  **$2^n$** .  
Here, **n = 17**

$\therefore$  Power set constant  **$2^{17}$**  elements.

---

## Question 168

-The argument of  $\frac{1-i\sqrt{3}}{1+i\sqrt{3}}$  is

Options:

- A.  $\frac{\pi}{3}$
- B.  $\frac{2\pi}{3}$
- C.  $\frac{4\pi}{3}$
- D.  $\frac{-2\pi}{3}$

Answer: D

Solution:

Solution:

$$\frac{1 - i\sqrt{3}}{1 + i\sqrt{3}} = \frac{1 - i\sqrt{3}}{1 + i\sqrt{3}} \times \frac{1 - i\sqrt{3}}{1 - i\sqrt{3}} = \frac{(1 - i\sqrt{3})^2}{4}$$

[ Using identity  $(a + b)(a - b) = a^2 - b^2$  ]

$$= \frac{1 - 2\sqrt{3}i - 3}{4} = \frac{-2 - 2\sqrt{3}i}{4}$$

$$= \frac{-1}{2} - \frac{\sqrt{3}}{2}i$$

$$\therefore \arg\left(\frac{-1}{2} - \frac{\sqrt{3}}{2}i\right) = -(\pi - \tan^{-1}\sqrt{3}) = \frac{-2\pi}{3}$$

## Question 169

Evaluate  $\left[ i^{22} + \left( \frac{1}{i} \right)^{25} \right]^3$

Options:

A.  $4(i - 1)$

B.  $2 - 7i$

C.  $i - 1$

D.  $2(1 - i)$

**Answer: D**

**Solution:**

Solution:

$$\left[ i^{22} + \left( \frac{1}{i} \right)^{25} \right]^3 = \left[ (i^2)^{11} + \frac{1}{(i^2)^{12}i} \right]^3$$

$$= \left[ (-1)^{11} + \frac{1}{i} \right]^3 = \left( -1 + \frac{1}{i} \right)^3 \quad [\because i^2 = -1]$$

$$= (-1)^3 + \left( \frac{1}{i} \right)^3 + 3(-1) \left( \frac{1}{i} \right) \left( -1 + \frac{1}{i} \right)$$

[Using  $(a + b)^3 = a^3 + b^3 + 3ab(a + b)$ ]

$$= -1 + \frac{1}{i^2} - \frac{3}{i} \left( -1 + \frac{1}{i} \right)$$

$$= -1 - \frac{1}{i} + \frac{3}{i} - \frac{3}{i^2}$$

$$= -1 + \frac{2}{i} + 3 (\because i^2 = -1)$$

$$= 2 + \frac{2i}{1 \times 1} = 2 - 2i = 2(1 - i)$$

## Question 170

$(i + \sqrt{3})^{100} + (i - \sqrt{3})^{100} + 2^{100}$  is equal to

Options:

A. 0

B. 1

C. -1

D.  $2^{101}$

Answer: A

Solution:

Solution:

$$(1 + \sqrt{3})^{100} = 1 \times (1 + \sqrt{3})^{100} = i^{100}(1 + \sqrt{3})^{100}$$

$$(As i^{4m} = 1, \text{ where } m = 25 \therefore i^{100} = 1)$$

$$= (i^2 + i\sqrt{3})^{100} = (-1 + i\sqrt{3})^{100} = (2\omega)^{100}$$

$$\text{Similarly, } (i - \sqrt{3})^{100} = (-1 + i\sqrt{3})^{100} = (2\omega^2)^{100}$$

$$\therefore (1 + \sqrt{3})^{100} + (i - \sqrt{3})^{100} + 2^{100}$$

$$= (2\omega)^{100} + (2\omega^2)^{100} + 2^{100}$$

$$= 2^{100}(\omega^{100} + \omega^{200} + 1)$$

$$= 2^{100}(0) = 0$$

$$\therefore (1 + \sqrt{3})^{100} + (i - \sqrt{3})^{100} + 2^{100} = 0$$

## Question 171

There are 12 points in a plane out of which 3 points are collinear. How many straight lines can be drawn by joining any two of them?

Options:

A. 60

B. 64

C. 72

D. 84

Answer: B

Solution:

Solution:

From 12 given points  ${}^{12}C_2$  straight lines can be drawn.

But 3 points are collinear, using 3 points  ${}^3C_2$  straight lines can be drawn.

So, total straight lines without the straight line using three points  $= {}^{12}C_2 - {}^3C_2$

From 3 collinear points 1 straight line can be drawn

So, total number of straight lines  $= {}^{12}C_2 - {}^3C_2 + 1$

$$\begin{aligned} &= \frac{12!}{2! \times 10!} - \frac{3!}{2! \times 1!} + 1 \\ &= \frac{12 \times 11 \times 10!}{2 \times 1 \times 10!} - \frac{3 \times 2!}{2! \times 1} + 1 \\ &= 66 - 3 + 1 = 64 \end{aligned}$$

## Question 172

How many numbers greater than 50000 can be formed by using digits 2, 5, 5, 6, 7 ?

Options:

- A. 60
- B. 48
- C. 52
- D. 42

**Answer: B**

**Solution:**

Solution:

Total number formed by using 5 digits =  $\frac{5!}{2!}$

$$= \frac{5 \times 4 \times 3 \times 2!}{2!} = 60$$

For number greater than **50,000**, digit **2** cannot come at first place.

Hence, number formed in which **2** is at the first place

$$= \frac{4!}{2!} = \frac{4 \times 3 \times 2!}{2!} = 12$$

Hence, total number formed greater than **50000**

$$= 60 - 12 = 48$$

## Question 173

**A regular polygon of n sides has 170 diagonals, then n is equal to**

**Options:**

- A. -20
- B. -17
- C. 24
- D. 20

**Answer: D**

**Solution:**

Solution:

A polygon of **n** sides has number of diagonals = **170**

$$\Rightarrow n \frac{(n-3)}{2} = 170$$

$$\Rightarrow n^2 - 3n = 340$$

$$\Rightarrow n^2 - 3n - 340 = 0$$

$$\Rightarrow n^2 - 20n + 17n - 340 = 0$$

$$\Rightarrow n(n-20) + 17(n-20) = 0$$

$$\Rightarrow (n-20)(n+17) = 0$$

$$\Rightarrow n - 20 \text{ or } n + 17 = 0$$

$$n = 20 \text{ or } n = -17 \text{ [it is not possible]}$$

$$\text{So, } n = 20$$

## Question 174

Let the equation of the pair of lines  $y = px$  and  $y = qx$  can be written as  $(y - px)(y - qx) = 0$ . Then the equation of the pair of the angle bisectors of the line  $x^2 - 4xy - 5y^2 = 0$  is

Options:

A.  $x^2 - 3xy + y^2 = 0$

B.  $x^2 + 4xy - y^2 = 0$

C.  $x^2 + 3xy - y^2 = 0$

D.  $x^2 - 3xy - y^2 = 0$

Answer: C

Solution:

Solution:

Equation of angle of equation of pair of straight line

$ax^2 + 2hxy + by^2$  is

$$\frac{x^2 - y^2}{a - b} = \frac{xy}{h}$$

For  $x^2 - 4xy - 5y^2 = 0$

$a = 1, h = -2, b = -5$

So, equation of angle bisector is

$$\frac{x^2 - y^2}{1 - (-5)} = \frac{xy}{-2}$$

$$\Rightarrow x^2 - y^2 = -3xy$$

$$\Rightarrow x^2 + 3xy - y^2 = 0$$

## Question 175

The distance of the point  $(1, 2)$  from the line  $x + y + 2 = 0$  measured along the line parallel to  $2x - y = 5$  is equal to

Options:

A.  $\frac{125}{3}$

B.  $\frac{125}{\sqrt{3}}$

C.  $\frac{5\sqrt{5}}{3}$

D.  $\frac{5\sqrt{3}}{3}$

Answer: C

Solution:

Solution:

We know to find, PQ

IMAGE

The slope of the line  $2x - y = 5$

$$\Rightarrow y = 2x - 5$$

On comparing with  $y = mx + c$ , we get

$$m = 2$$

Also, slope of  $PQ$ ,  $m_{PQ} = 2$

$$\text{Eq. of } PQ, (y - 2) = 2(x - 1)$$

$$\Rightarrow y - 2 = 2x - 2$$

$$\Rightarrow y = 2x$$

$$\text{So, from } x + y + 2 = 0 \Rightarrow x + 2x + 2 = 0$$

$$\Rightarrow 3x + 2 = 0 \Rightarrow x = -\frac{2}{3}$$

$$y = 2 \times -\frac{2}{3} = -\frac{4}{3}$$

$$\therefore \text{The point } Q \text{ is } \left( -\frac{2}{3}, -\frac{4}{3} \right)$$

$$\text{and } P = (1, 2)$$

$$\text{Distance, } PQ = \sqrt{\left( -\frac{2}{3} - 1 \right)^2 + \left( -\frac{4}{3} - 2 \right)^2}$$

$$= \sqrt{\left( -\frac{5}{3} \right)^2 + \left( -\frac{10}{3} \right)^2}$$

$$= \sqrt{\frac{25}{9} + \frac{100}{9}} = \sqrt{\frac{125}{9}} = \frac{\sqrt{125}}{3} = \frac{5\sqrt{5}}{3}$$

## Question 176

The slope of lines which makes an angle  $45^\circ$  with the line  $2x - y = -7$

Options:

A.  $\frac{1}{3}, -3$

B.  $-1, 1$

C.  $3, \frac{-1}{3}$

D.  $1, \frac{1}{3}$

Answer: A

Solution:

Solution:

$$\text{We have, } \theta = \frac{\pi}{4}$$

$$\text{Given, line is } 2x - y = -7$$

$$y = 2x + 7$$

$$\text{Here, slope } m_1 = 2$$

The required line makes an angle  $45^\circ$  with this line

$$\text{So, } \tan 45^\circ = \left| \frac{2 - m_2}{1 + 2m_2} \right|$$

$$\Rightarrow 1 + 2m_2 = 2 - m_2 \text{ or } 1 + 2m_2 = -(2 - m_2)$$

$$2m_2 + m_2 = 2 - 1 \text{ or } 1 + 2m_2 = -2 + m_2$$

$$\Rightarrow 3m_2 = 1 \Rightarrow 1m_2 - m_2 = -2 - 1$$

$$\therefore m_2 = \frac{1}{3}, m_2 = -3$$

## Question 177

If 2 and 3 are intercepts of a line  $L = 0$ , then the distance of  $L \equiv 0$  from the origin is

Options:

A.  $\frac{5}{\sqrt{13}}$

B.  $\frac{\sqrt{13}}{6}$

C.  $\frac{6}{\sqrt{13}}$

D. 1

Answer: C

Solution:

Solution:

If 2, 3 are intercepts of a line  $L = 0$ , then

x - intercept = 2 = a

y - intercept = 3 = b

Equation of line is  $\frac{x}{a} + \frac{y}{b} = 1$

$$\Rightarrow \frac{x}{2} + \frac{y}{3} = 1$$

$$\Rightarrow 3x + 2y - 6 = 0$$

∴ Required distance from origin is given by

$$= \left| \frac{3(0) + 2(0) - 6}{\sqrt{3^2 + 2^2}} \right| = \frac{|-6|}{\sqrt{13}} = \frac{6}{\sqrt{13}}$$

$$\therefore \text{Distance} = \frac{6}{\sqrt{13}} \text{ units}$$

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## Question 178

The total number of terms in the expansion of  $(x + y)^{100} + (x - y)^{100}$  is

Options:

A. 49

B. 50

C. 51

D. 99

Answer: C

Solution:

Solution:

The expansion  $(x + y)^{100} + (x - y)^{100}$  has

$$\left( \frac{100}{2} + 1 \right) = 51 \text{ terms}$$

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## Question 179

The coefficient of  $x^{20}$  in the expansion of  $(1 + 3x + 3x^2 + x^3)^{20}$  is

Options:

A.  ${}^{60}C_{40}$

B.  ${}^{30}C_{20}$

C.  ${}^{15}C_2$

D. None of these

**Answer: A**

**Solution:**

Solution:

Given expansion is  $(1 + 3x + 2x^2 + x^3)^{20}$

$$= ((1 + x)^3)^{20}$$

$$= (1 + x)^{60} \dots\dots\dots (i)$$

In the expansion of  $(a+b)^n$ ,  $(r+1)$ th term given by

$$t_{r+1} = {}^nC_r \cdot a^r \cdot b^{n-r}$$

$$\text{or, } t_{r+1} = {}^nC_r a^{n-r} \cdot b^r$$

$\therefore$  21st term in Eq.(i) will contain the coefficient of  $x^{20}$  and it is given by

$$t_{21} = {}^{60}C_{20} x^{20}, 1^{40} = {}^{60}C_{20} x^{20}$$

$\therefore$  Coefficient of  $x^{20}$  in  $(1 + x)^{60}$  is  ${}^{60}C_{20}$  or  ${}^{60}C_{40}$ .

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## Question 180

In the expansion of  $(1 - 3x + 3x^2 - x^3)^{2n}$ , the middle term is

Options:

A.  $(n + 1)$  th term

B.  $(2n + 1)$  th term

C.  $(3n + 1)$  th term

D. None of these

**Answer: C**

**Solution:**

Solution:

Given expansion is  $(1 - 3x + 3x^2 - x^3)^{2n}$

$$= [(1 - x)^3]^{2n}$$

$$= (1 - x)^{6n}$$

$\therefore$  Middle term =  $\frac{6n+2}{2}$  th term [ here,  $6n$  is even]

$$= (3n + 1) \text{th term}$$