



## EXERCISE 5.1

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1. In which of the following situations, does the list of numbers involved make an arithmetic progression and why?

(i) The taxi fare after each km when the fare is Rs 15 for the first km and Rs 8 for each additional km.

**Solution:**

We can write the given condition as;

Taxi fare for 1 km = 15

Taxi fare for first 2 kms =  $15+8 = 23$

Taxi fare for first 3 kms =  $23+8 = 31$

Taxi fare for first 4 kms =  $31+8 = 39$

And so on.....

Thus, 15, 23, 31, 39 ... forms an A.P. because every next term is 8 more than the preceding term.

(ii) The amount of air present in a cylinder when a vacuum pump removes  $\frac{1}{4}$  of the air remaining in the cylinder at a time.

**Solution:**

Let the volume of air in a cylinder, initially, be  $V$  litres.

In each stroke, the vacuum pump removes  $\frac{1}{4}$ th of air remaining in the cylinder at a time. Or we can say, after every stroke,  $1-\frac{1}{4} = \frac{3}{4}$ th part of air will remain.

Therefore, volumes will be  $V, \frac{3V}{4}, (\frac{3V}{4})^2, (\frac{3V}{4})^3 \dots$  and so on

Clearly, we can see here, the adjacent terms of this series do not have the common difference between them. Therefore, this series is not an A.P.

(iii) The cost of digging a well after every metre of digging, when it costs Rs 150 for the first metre and rises by Rs 50 for each subsequent metre.

**Solution:**

We can write the given condition as;

Cost of digging a well for first metre = Rs.150

Cost of digging a well for first 2 metres =  $\text{Rs.}150+50 = \text{Rs.}200$

Cost of digging a well for first 3 metres =  $\text{Rs.}200+50 = \text{Rs.}250$



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Cost of digging a well for first 4 metres =Rs.250+50 = Rs.300

And so on..

Clearly, 150, 200, 250, 300 ... forms an A.P. with a common difference of 50 between each term.

**(iv) The amount of money in the account every year, when Rs 10000 is deposited at compound interest at 8% per annum.**

**Solution:**

We know that if Rs. P is deposited at  $r\%$  compound interest per annum for  $n$  years, the amount of money will be:

$$P(1+r/100)^n$$

Therefore, after each year, the amount of money will be;

$$10000(1+8/100), 10000(1+8/100)^2, 10000(1+8/100)^3, \dots$$

Clearly, the terms of this series do not have the common difference between them. Therefore, this is not an A.P.

**2. Write first four terms of the A.P. when the first term  $a$  and the common difference are given as follows:**

**(i)  $a = 10, d = 10$**

**(ii)  $a = -2, d = 0$**

**(iii)  $a = 4, d = -3$**

**(iv)  $a = -1, d = 1/2$**

**(v)  $a = -1.25, d = -0.25$**

**Solutions:**

(i)  $a = 10, d = 10$

Let us consider, the Arithmetic Progression series be  $a_1, a_2, a_3, a_4, a_5 \dots$

$$a_1 = a = 10$$

$$a_2 = a_1 + d = 10 + 10 = 20$$

$$a_3 = a_2 + d = 20 + 10 = 30$$

$$a_4 = a_3 + d = 30 + 10 = 40$$

$$a_5 = a_4 + d = 40 + 10 = 50$$

And so on...

Therefore, the A.P. series will be 10, 20, 30, 40, 50 ...

And First four terms of this A.P. will be 10, 20, 30, and 40.

(ii)  $a = -2, d = 0$



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Let us consider, the Arithmetic Progression series be  $a_1, a_2, a_3, a_4, a_5 \dots$

$$a_1 = a = -2$$

$$a_2 = a_1 + d = -2 + 0 = -2$$

$$a_3 = a_2 + d = -2 + 0 = -2$$

$$a_4 = a_3 + d = -2 + 0 = -2$$

Therefore, the A.P. series will be  $-2, -2, -2, -2 \dots$

And, First four terms of this A.P. will be  $-2, -2, -2$  and  $-2$ .

$$(iii) a = 4, d = -3$$

Let us consider, the Arithmetic Progression series be  $a_1, a_2, a_3, a_4, a_5 \dots$

$$a_1 = a = 4$$

$$a_2 = a_1 + d = 4 - 3 = 1$$

$$a_3 = a_2 + d = 1 - 3 = -2$$

$$a_4 = a_3 + d = -2 - 3 = -5$$

Therefore, the A.P. series will be  $4, 1, -2, -5 \dots$

And, first four terms of this A.P. will be  $4, 1, -2$  and  $-5$ .

$$(iv) a = -1, d = 1/2$$

Let us consider, the Arithmetic Progression series be  $a_1, a_2, a_3, a_4, a_5 \dots$

$$a_2 = a_1 + d = -1 + 1/2 = -1/2$$

$$a_3 = a_2 + d = -1/2 + 1/2 = 0$$

$$a_4 = a_3 + d = 0 + 1/2 = 1/2$$

Thus, the A.P. series will be  $-1, -1/2, 0, 1/2$

And First four terms of this A.P. will be  $-1, -1/2, 0$  and  $1/2$ .

$$(v) a = -1.25, d = -0.25$$

Let us consider, the Arithmetic Progression series be  $a_1, a_2, a_3, a_4, a_5 \dots$

$$a_1 = a = -1.25$$

$$a_2 = a_1 + d = -1.25 - 0.25 = -1.50$$



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$$a_3 = a_2 + d = -1.50 - 0.25 = -1.75$$

$$a_4 = a_3 + d = -1.75 - 0.25 = -2.00$$

Therefore, the A.P series will be  $1.25, -1.50, -1.75, -2.00, \dots$

And first four terms of this A.P. will be  $-1.25, -1.50, -1.75$  and  $-2.00$ .

**3. For the following A.P.s, write the first term and the common difference.**

(i)  $3, 1, -1, -3 \dots$

(ii)  $-5, -1, 3, 7 \dots$

(iii)  $1/3, 5/3, 9/3, 13/3 \dots$

(iv)  $0.6, 1.7, 2.8, 3.9 \dots$

### Solutions

(i) Given series,

$3, 1, -1, -3 \dots$

First term,  $a = 3$

Common difference,  $d = \text{Second term} - \text{First term}$

$$\Rightarrow 1 - 3 = -2$$

$$\Rightarrow d = -2$$

(ii) Given series,  $-5, -1, 3, 7 \dots$

First term,  $a = -5$

Common difference,  $d = \text{Second term} - \text{First term}$

$$\Rightarrow (-1) - (-5) = -1 + 5 = 4$$

(iii) Given series,  $1/3, 5/3, 9/3, 13/3 \dots$

First term,  $a = 1/3$

Common difference,  $d = \text{Second term} - \text{First term}$

$$\Rightarrow 5/3 - 1/3 = 4/3$$

(iv) Given series,  $0.6, 1.7, 2.8, 3.9 \dots$

First term,  $a = 0.6$

Common difference,  $d = \text{Second term} - \text{First term}$

$$\Rightarrow 1.7 - 0.6$$

$$\Rightarrow 1.1$$



4. Which of the following are APs? If they form an A.P. find the common difference  $d$  and write three more terms.

- (i) 2, 4, 8, 16 ...
- (ii) 2,  $5/2$ , 3,  $7/2$  ....
- (iii) -1.2, -3.2, -5.2, -7.2 ...
- (iv) -10, -6, -2, 2 ...
- (v) 3,  $3 + \sqrt{2}$ ,  $3 + 2\sqrt{2}$ ,  $3 + 3\sqrt{2}$
- (vi) 0.2, 0.22, 0.222, 0.2222 ....
- (vii) 0, -4, -8, -12 ...
- (viii)  $-1/2$ ,  $-1/2$ ,  $-1/2$ ,  $-1/2$  ....
- (ix) 1, 3, 9, 27 ...
- (x)  $a$ ,  $2a$ ,  $3a$ ,  $4a$  ...
- (xi)  $a$ ,  $a^2$ ,  $a^3$ ,  $a^4$  ...
- (xii)  $\sqrt{2}$ ,  $\sqrt{8}$ ,  $\sqrt{18}$ ,  $\sqrt{32}$  ...
- (xiii)  $\sqrt{3}$ ,  $\sqrt{6}$ ,  $\sqrt{9}$ ,  $\sqrt{12}$  ...
- (xiv)  $1^2$ ,  $3^2$ ,  $5^2$ ,  $7^2$  ...
- (xv)  $1^2$ ,  $5^2$ ,  $7^2$ ,  $7^3$  ...

**Solution**

(i) Given to us,

2, 4, 8, 16 ...

Here, the common difference is;

$$a_2 - a_1 = 4 - 2 = 2$$

$$a_3 - a_2 = 8 - 4 = 4$$

$$a_4 - a_3 = 16 - 8 = 8$$

Since,  $a_{n+1} - a_n$  or the common difference is not the same every time.

Therefore, the given series are not forming an A.P.

**(ii) Given, 2,  $5/2$ , 3,  $7/2$  ....**

Here,

$$a_2 - a_1 = 5/2 - 2 = 1/2$$

$$a_3 - a_2 = 3 - 5/2 = 1/2$$

$$a_4 - a_3 = 7/2 - 3 = 1/2$$

Since,  $a_{n+1} - a_n$  or the common difference is same every time.

Therefore,  $d = 1/2$  and the given series are in A.P.

The next three terms are;



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$$a_5 = 7/2 + 1/2 = 4$$

$$a_6 = 4 + 1/2 = 9/2$$

$$a_7 = 9/2 + 1/2 = 5$$

**(iii) Given, -1.2, -3.2, -5.2, -7.2 ...**

Here,

$$a_2 - a_1 = (-3.2) - (-1.2) = -2$$

$$a_3 - a_2 = (-5.2) - (-3.2) = -2$$

$$a_4 - a_3 = (-7.2) - (-5.2) = -2$$

Since,  $a_{n+1} - a_n$  or common difference is same every time.

Therefore,  $d = -2$  and the given series are in A.P.

Hence, next three terms are;

$$a_5 = -7.2 - 2 = -9.2$$

$$a_6 = -9.2 - 2 = -11.2$$

$$a_7 = -11.2 - 2 = -13.2$$

**(iv) Given, -10, -6, -2, 2 ...**

Here, the terms and their difference are;

$$a_2 - a_1 = (-6) - (-10) = 4$$

$$a_3 - a_2 = (-2) - (-6) = 4$$

$$a_4 - a_3 = (2) - (-2) = 4$$

Since,  $a_{n+1} - a_n$  or the common difference is same every time.

Therefore,  $d = 4$  and the given numbers are in A.P.

Hence, next three terms are;

$$a_5 = 2 + 4 = 6$$

$$a_6 = 6 + 4 = 10$$

$$a_7 = 10 + 4 = 14$$



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(v) Given,  $3, 3+\sqrt{2}, 3+2\sqrt{2}, 3+3\sqrt{2}$

Here,

$$a_2 - a_1 = 3 + \sqrt{2} - 3 = \sqrt{2}$$

$$a_3 - a_2 = (3 + 2\sqrt{2}) - (3 + \sqrt{2}) = \sqrt{2}$$

$$a_4 - a_3 = (3 + 3\sqrt{2}) - (3 + 2\sqrt{2}) = \sqrt{2}$$

Since,  $a_{n+1} - a_n$  or the common difference is same every time.

Therefore,  $d = \sqrt{2}$  and the given series forms a A.P.

Hence, next three terms are;

$$a_5 = (3 + \sqrt{2}) + \sqrt{2} = 3 + 4\sqrt{2}$$

$$a_6 = (3 + 4\sqrt{2}) + \sqrt{2} = 3 + 5\sqrt{2}$$

$$a_7 = (3 + 5\sqrt{2}) + \sqrt{2} = 3 + 6\sqrt{2}$$

(vi)  $0.2, 0.22, 0.222, 0.2222 \dots$

Here,

$$a_2 - a_1 = 0.22 - 0.2 = 0.02$$

$$a_3 - a_2 = 0.222 - 0.22 = 0.002$$

$$a_4 - a_3 = 0.2222 - 0.222 = 0.0002$$

Since,  $a_{n+1} - a_n$  or the common difference is not same every time.

Therefore, and the given series doesn't forms a A.P.

(vii)  $0, -4, -8, -12 \dots$

Here,

$$a_2 - a_1 = (-4) - 0 = -4$$

$$a_3 - a_2 = (-8) - (-4) = -4$$

$$a_4 - a_3 = (-12) - (-8) = -4$$

Since,  $a_{n+1} - a_n$  or the common difference is same every time.

Therefore,  $d = -4$  and the given series forms a A.P.

Hence, next three terms are;



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$$a_5 = -12 - 4 = -16$$

$$a_6 = -16 - 4 = -20$$

$$a_7 = -20 - 4 = -24$$

**(viii)  $-1/2, -1/2, -1/2, -1/2 \dots$**

Here,

$$a_2 - a_1 = (-1/2) - (-1/2) = 0$$

$$a_3 - a_2 = (-1/2) - (-1/2) = 0$$

$$a_4 - a_3 = (-1/2) - (-1/2) = 0$$

Since,  $a_{n+1} - a_n$  or the common difference is same every time.

Therefore,  $d = 0$  and the given series forms a A.P.

Hence, next three terms are;

$$a_5 = (-1/2) - 0 = -1/2$$

$$a_6 = (-1/2) - 0 = -1/2$$

$$a_7 = (-1/2) - 0 = -1/2$$

**(ix)  $1, 3, 9, 27 \dots$**

Here,

$$a_2 - a_1 = 3 - 1 = 2$$

$$a_3 - a_2 = 9 - 3 = 6$$

$$a_4 - a_3 = 27 - 9 = 18$$

Since,  $a_{n+1} - a_n$  or the common difference is not same every time.

Therefore, and the given series doesn't form a A.P.

**(x)  $a, 2a, 3a, 4a \dots$**

Here,

$$a_2 - a_1 = 2a - a = a$$

$$a_3 - a_2 = 3a - 2a = a$$

$$a_4 - a_3 = 4a - 3a = a$$





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Since,  $a_{n+1} - a_n$  or the common difference is same every time.

Therefore,  $d = a$  and the given series forms a A.P.

Hence, next three terms are;

$$a_5 = 4a + a = 5a$$

$$a_6 = 5a + a = 6a$$

$$a_7 = 6a + a = 7a$$

**(xi)  $a, a^2, a^3, a^4 \dots$**

Here,

$$a_2 - a_1 = a^2 - a = a(a-1)$$

$$a_3 - a_2 = a^3 - a^2 = a^2(a-1)$$

$$a_4 - a_3 = a^4 - a^3 = a^3(a-1)$$

Since,  $a_{n+1} - a_n$  or the common difference is not same every time.

Therefore, the given series doesn't forms a A.P.

**(xii)  $\sqrt{2}, \sqrt{8}, \sqrt{18}, \sqrt{32} \dots$**

Here,

$$a_2 - a_1 = \sqrt{8} - \sqrt{2} = 2\sqrt{2} - \sqrt{2} = \sqrt{2}$$

$$a_3 - a_2 = \sqrt{18} - \sqrt{8} = 3\sqrt{2} - 2\sqrt{2} = \sqrt{2}$$

$$a_4 - a_3 = 4\sqrt{2} - 3\sqrt{2} = \sqrt{2}$$

Since,  $a_{n+1} - a_n$  or the common difference is same every time.

Therefore,  $d = \sqrt{2}$  and the given series forms a A.P.

Hence, next three terms are;

$$a_5 = \sqrt{32} + \sqrt{2} = 4\sqrt{2} + \sqrt{2} = 5\sqrt{2} = \sqrt{50}$$

$$a_6 = 5\sqrt{2} + \sqrt{2} = 6\sqrt{2} = \sqrt{72}$$

$$a_7 = 6\sqrt{2} + \sqrt{2} = 7\sqrt{2} = \sqrt{98}$$

**(xiii)  $\sqrt{3}, \sqrt{6}, \sqrt{9}, \sqrt{12} \dots$**

Here,



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$$a_2 - a_1 = \sqrt{6} - \sqrt{3} = \sqrt{3} \times \sqrt{2} - \sqrt{3} = \sqrt{3}(\sqrt{2} - 1)$$

$$a_3 - a_2 = \sqrt{9} - \sqrt{6} = 3 - \sqrt{6} = \sqrt{3}(\sqrt{3} - \sqrt{2})$$

$$a_4 - a_3 = \sqrt{12} - \sqrt{9} = 2\sqrt{3} - \sqrt{3} \times \sqrt{3} = \sqrt{3}(2 - \sqrt{3})$$

Since,  $a_{n+1} - a_n$  or the common difference is not same every time.

Therefore, the given series doesn't form a A.P.

**(xiv)  $1^2, 3^2, 5^2, 7^2 \dots$**

Or, 1, 9, 25, 49 .....

Here,

$$a_2 - a_1 = 9 - 1 = 8$$

$$a_3 - a_2 = 25 - 9 = 16$$

$$a_4 - a_3 = 49 - 25 = 24$$

Since,  $a_{n+1} - a_n$  or the common difference is not same every time.

Therefore, the given series doesn't form a A.P.

**(xv)  $1^2, 5^2, 7^2, 73 \dots$**

Or 1, 25, 49, 73 ...

Here,

$$a_2 - a_1 = 25 - 1 = 24$$

$$a_3 - a_2 = 49 - 25 = 24$$

$$a_4 - a_3 = 73 - 49 = 24$$

Since,  $a_{n+1} - a_n$  or the common difference is same every time.

Therefore,  $d = 24$  and the given series forms a A.P.

Hence, next three terms are;

$$a_5 = 73 + 24 = 97$$

$$a_6 = 97 + 24 = 121$$

$$a_7 = 121 + 24 = 145$$



## EXERCISE 5.2

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1. Fill in the blanks in the following table, given that  $a$  is the first term,  $d$  the common difference and  $a_n$  the  $n^{\text{th}}$  term of the A.P.

	$a$	$d$	$n$	$a_n$
(i)	7	3	8	.....
(ii)	-18	.....	10	0
(iii)	.....	-3	18	-5
(iv)	-18.9	2.5	.....	3.6
(v)	3.5	0	105	.....

**Solutions:**

(i) Given,

First term,  $a = 7$

Common difference,  $d = 3$

Number of terms,  $n = 8$ ,

We have to find the  $n^{\text{th}}$  term,  $a_n = ?$

As we know, for an A.P.,

$$a_n = a + (n-1)d$$

Putting the values,

$$\Rightarrow 7 + (8-1)3$$

$$\Rightarrow 7 + (7)3$$

$$\Rightarrow 7 + 21 = 28$$

Hence,  $a_n = 28$

(ii) Given,



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First term,  $a = -18$

Common difference,  $d = ?$

Number of terms,  $n = 10$

Nth term,  $a_n = 0$

As we know, for an A.P.,

$$a_n = a + (n-1)d$$

Putting the values,

$$0 = -18 + (10-1)d$$

$$18 = 9d$$

$$d = 18/9 = 2$$

Hence, common difference,  $d = 2$

**(iii)** Given,

First term,  $a = ?$

Common difference,  $d = -3$

Number of terms,  $n = 18$

Nth term,  $a_n = -5$

As we know, for an A.P.,

$$a_n = a + (n-1)d$$

Putting the values,

$$-5 = a + (18-1)(-3)$$

$$-5 = a + (17)(-3)$$

$$-5 = a - 51$$

$$a = 51 - 5 = 46$$

Hence,  $a = 46$

**(iv)** Given,

First term,  $a = -18.9$



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Common difference,  $d = 2.5$

Number of terms,  $n = ?$

Nth term,  $a_n = 3.6$

As we know, for an A.P.,

$$a_n = a + (n - 1)d$$

Putting the values,

$$3.6 = -18.9 + (n - 1)2.5$$

$$3.6 + 18.9 = (n - 1)2.5$$

$$22.5 = (n - 1)2.5$$

$$(n - 1) = 22.5/2.5$$

$$n - 1 = 9$$

$$n = 10$$

Hence,  $n = 10$

(v) Given,

First term,  $a = 3.5$

Common difference,  $d = 0$

Number of terms,  $n = 105$

Nth term,  $a_n = ?$

As we know, for an A.P.,

$$a_n = a + (n - 1)d$$

Putting the values,

$$a_n = 3.5 + (105 - 1)0$$

$$a_n = 3.5 + 104 \times 0$$

$$a_n = 3.5$$

Hence,  $a_n = 3.5$



2. Choose the correct choice in the following and justify:

(i) 30<sup>th</sup> term of the A.P: 10, 7, 4, ..., is

(A) 97 (B) 77 (C) -77 (D) -87

(ii) 11<sup>th</sup> term of the A.P. -3, -1/2, 2 .... is

(A) 28 (B) 22 (C) -38 (D)

**-48  $\frac{1}{2}$**

**Solutions:**

(i) Given here,

A.P. = 10, 7, 4, ...

Therefore, we can find,

First term,  $a = 10$

Common difference,  $d = a_2 - a_1 = 7 - 10 = -3$

As we know, for an A.P.,

$$a_n = a + (n-1)d$$

Putting the values;

$$a_{30} = 10 + (30-1)(-3)$$

$$a_{30} = 10 + (29)(-3)$$

$$a_{30} = 10 - 87 = -77$$

Hence, the correct answer is option C.

(ii) Given here,

A.P. = -3, -1/2, 2 ...

Therefore, we can find,

First term  $a = -3$

Common difference,  $d = a_2 - a_1 = (-1/2) - (-3)$

$$\Rightarrow (-1/2) + 3 = 5/2$$

As we know, for an A.P.,

$$a_n = a + (n-1)d$$

Putting the values;



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$$a_{11} = -3 + (11-1)(5/2)$$

$$a_{11} = -3 + (10)(5/2)$$

$$a_{11} = -3 + 25$$

$$a_{11} = 22$$

Hence, the answer is option B.

**3. In the following APs find the missing term in the boxes.**

$$a_3 = 26$$

As we know, for an A.P.,

(i) 2, , 26

(ii) , 13, , 3

(iii) 5, , ,  $9\frac{1}{2}$

(iv) -4, , , , , 6

(v) , 38, , , , -22

**Solutions:**

(i) For the given A.P., 2, 2, 26 The first and

third term are;

$$a = 2$$

$$a_n = a + (n-1)d$$

Therefore, putting the values here,

$$a_3 = 2 + (3-1)d$$

$$26 = 2 + 2d$$

$$24 = 2d$$



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$$d = 12$$

$$a_2 = 2 + (2-1)12$$

$$= 14$$

Therefore, 14 is the missing term.

**(ii) For the given A.P., , 13, ,3**

$$a_2 = 13 \text{ and}$$

$$a_4 = 3$$

As we know, for an A.P.,

$$a_n = a + (n-1)d$$

Therefore, putting the values here,

$$a_2 = a + (2-1)d$$

$$13 = a + d \dots \dots \dots \text{(i)}$$

$$a_4 = a + (4-1)d$$

$$3 = a + 3d \dots \dots \dots \text{(ii)}$$

On subtracting equation (i) from (ii), we get,

$$-10 = 2d$$

$$d = -5$$

From equation (i), putting the value of d, we get

$$13 = a + (-5)$$

$$a = 18$$

$$a_3 = 18 + (3-1)(-5)$$

$$= 18 + 2(-5) = 18 - 10 = 8$$

Therefore, the missing terms are 18 and 8 respectively.

**(iii) For the given A.P.,**

$$a = 5 \text{ and}$$

$$a_4 = 19/2$$

As we know, for an A.P.,





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$$a_n = a + (n-1)d$$

Therefore, putting the values here,

$$a_4 = a + (4-1)d$$

$$19/2 = 5 + 3d$$

$$(19/2) - 5 = 3d$$

$$3d = 9/2$$

$$d = 3/2$$

$$a_2 = a + (2-1)d$$

$$a_2 = 5 + 3/2$$

$$a_2 = 13/2$$

$$a_3 = a + (3-1)d$$

$$a_3 = 5 + 2 \times 3/2$$

$$a_3 = 8$$

Therefore, the missing terms are  $13/2$  and  $8$  respectively.

(iv) For the given A.P.,

$$a = -4 \text{ and}$$

$$a_6 = 6$$

As we know, for an A.P.,

$$a_n = a + (n-1)d$$

Therefore, putting the values here,

$$a_6 = a + (6-1)d$$

$$6 = -4 + 5d$$

$$10 = 5d$$

$$d = 2$$

$$a_2 = a + d = -4 + 2 = -2$$

$$a_3 = a + 2d = -4 + 2(2) = 0$$



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$$a_4 = a + 3d = -4 + 3(2) = 2$$

$$a_5 = a + 4d = -4 + 4(2) = 4$$

Therefore, the missing terms are -2, 0, 2, and 4 respectively.

(v) For the given A.P.,

$$a_2 = 38$$

$$a_6 = -22$$

As we know, for an A.P.,

$$a_n = a + (n - 1)d$$

Therefore, putting the values here,

$$a_2 = a + (2 - 1)d$$

$$38 = a + d \dots\dots\dots \text{(i)}$$

$$a_6 = a + (6 - 1)d$$

$$-22 = a + 5d \dots\dots\dots \text{(ii)}$$

On subtracting equation (i) from (ii), we get

$$-22 - 38 = 4d$$

$$-60 = 4d$$

$$d = -15$$

$$a = a_2 - d = 38 - (-15) = 53$$

$$a_3 = a + 2d = 53 + 2(-15) = 23$$

$$a_4 = a + 3d = 53 + 3(-15) = 8$$

$$a_5 = a + 4d = 53 + 4(-15) = -7$$

Therefore, the missing terms are 53, 23, 8, and -7 respectively.

### 4. Which term of the A.P. 3, 8, 13, 18, ... is 78?

**Solutions:**

Given the A.P. series as 3, 8, 13, 18, ...

First term,  $a = 3$

Common difference,  $d = a_2 - a_1 = 8 - 3 = 5$



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Let the  $n^{\text{th}}$  term of given A.P. be 78. Now as we know,

$$a_n = a + (n-1)d$$

Therefore,

$$78 = 3 + (n-1)5$$

$$75 = (n-1)5$$

$$(n-1) = 15$$

$$n = 16$$

As we know, for an A.P.,

Hence, 16<sup>th</sup> term of this A.P. is 78.

**5. Find the number of terms in each of the following A.P.**

**(i) 7, 13, 19, ..., 205**

**(ii) 18,  $15\frac{1}{2}$ , 13... -47**

**Solutions:**

**(i) Given, 7, 13, 19, ..., 205 is the A.P**

Therefore

$$\text{First term, } a = 7$$

$$\text{Common difference, } d = a_2 - a_1 = 13 - 7 = 6$$

Let there are  $n$  terms in this A.P.

$$a_n = 205$$

$$a_n = a + (n-1)d$$

$$\text{Therefore, } 205 = 7 + (n-1)6$$

$$198 = (n-1)6$$

$$33 = (n-1)$$

$$n = 34$$

Therefore, this given series has 34 terms in it.



**(ii) Given,  $18, 15\frac{1}{2}, 13, \dots, -47$  is the A.P.**

First term,  $a = 18$

Common difference,  $d = a_2 - a_1 =$

$$15\frac{1}{2} - 18$$

$$d = (31 - 36)/2 = -5/2$$

Let there are  $n$  terms in this A.P.

$$a_n = -47$$

As we know, for an A.P.,

$$a_n = a + (n-1)d$$

$$-47 = 18 + (n-1)(-5/2)$$

$$-47 - 18 = (n-1)(-5/2)$$

$$-65 = (n-1)(-5/2)$$

$$(n-1) = -130/-5$$

$$(n-1) = 26$$

$$n = 27$$

Therefore, this given A.P. has 27 terms in it.

**6. Check whether -150 is a term of the A.P. 11, 8, 5, 2, ...**

**Solution:**

For the given series, A.P. 11, 8, 5, 2..

First term,  $a = 11$

Common difference,  $d = a_2 - a_1 = 8 - 11 = -3$

Let -150 be the  $n^{\text{th}}$  term of this A.P.

As we know, for an A.P.,

$$a_n = a + (n-1)d$$

$$-150 = 11 + (n-1)(-3)$$



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$$-150 = 11 - 3n + 3$$

$$-164 = -3n$$

$$n = 164/3$$

Clearly,  $n$  is not an integer but a fraction.

Therefore,  $-150$  is not a term of this A.P.

**7. Find the 31<sup>st</sup> term of an A.P. whose 11<sup>th</sup> term is 38 and the 16<sup>th</sup> term is 73.**

**Solution:**

Given that,

$$11^{\text{th}} \text{ term, } a_{11} = 38$$

$$\text{and } 16^{\text{th}} \text{ term, } a_{16} = 73$$

We know that,

$$a_n = a + (n-1)d$$

$$a_{11} = a + (11-1)d$$

$$38 = a + 10d \dots\dots\dots \text{(i)}$$

In the same way,

$$a_{16} = a + (16-1)d$$

$$73 = a + 15d \dots\dots\dots \text{(ii)}$$

On subtracting equation (i) from (ii), we get

$$35 = 5d$$

$$d = 7$$

From equation (i), we can write,

$$38 = a + 10 \times (7)$$

$$38 - 70 = a$$

$$a = -32$$

$$a_{31} = a + (31-1)d$$

$$= -32 + 30(7)$$

$$= -32 + 210$$



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$$= 178$$

Hence, 31<sup>st</sup> term is 178.

**8. An A.P. consists of 50 terms of which 3<sup>rd</sup> term is 12 and the last term is 106. Find the 29<sup>th</sup> term.**

**Solution:** Given that,

$$3^{\text{rd}} \text{ term, } a_3 = 12$$

$$50^{\text{th}} \text{ term, } a_{50} = 106$$

We know that,

$$a_n = a + (n-1)d$$

$$a_3 = a + (3-1)d$$

$$12 = a + 2d \dots\dots\dots \text{(i)}$$

In the same way,

$$a_{50} = a + (50-1)d$$

$$106 = a + 49d \dots\dots\dots \text{(ii)}$$

On subtracting equation (i) from (ii), we get

$$94 = 47d$$

$$d = 2 = \text{common difference}$$

From equation (i), we can write now,

$$12 = a + 2(2)$$

$$a = 12 - 4 = 8$$

$$a_{29} = a + (29-1)d$$

$$a_{29} = 8 + (28)2$$

$$a_{29} = 8 + 56 = 64$$

Therefore, 29<sup>th</sup> term is 64.

**9. If the 3<sup>rd</sup> and the 9<sup>th</sup> terms of an A.P. are 4 and – 8 respectively. Which term of this A.P. is zero.**

**Solution:**

Given that,

$$3^{\text{rd}} \text{ term, } a_3 = 4$$



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and 9<sup>th</sup> term,  $a_9 = -8$

We know that,

$$a_n = a + (n-1)d$$

Therefore,

$$a_3 = a + (3-1)d$$

$$4 = a + 2d \dots\dots\dots \text{(i)}$$

$$a_9 = a + (9-1)d$$

$$-8 = a + 8d \dots\dots\dots \text{(ii)}$$

On subtracting equation (i) from (ii), we will get here,

$$-12 = 6d$$

$$d = -2$$

From equation (i), we can write,

$$4 = a + 2(-2)$$

$$4 = a - 4$$

$$a = 8$$

Let  $n^{\text{th}}$  term of this A.P. be zero.

$$a_n = a + (n-1)d$$

$$0 = 8 + (n-1)(-2)$$

$$0 = 8 - 2n + 2$$

$$2n = 10$$

$$n = 5$$

Hence, 5<sup>th</sup> term of this A.P. is 0.

**10. If 17<sup>th</sup> term of an A.P. exceeds its 10<sup>th</sup> term by 7. Find the common difference.**

**Solution:**

We know that, for an A.P series;

$$a_n = a + (n-1)d$$



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$$a_{17} = a + (17-1)d$$

$$a_{17} = a + 16d$$

In the same way,

$$a_{10} = a + 9d$$

As it is given in the question,

$$a_{17} - a_{10} = 7$$

Therefore,

$$(a + 16d) - (a + 9d) = 7$$

$$7d = 7$$

$$d = 1$$

Therefore, the common difference is 1.

**11. Which term of the A.P. 3, 15, 27, 39,.. will be 132 more than its 54<sup>th</sup> term?**

**Solution:**

Given A.P. is 3, 15, 27, 39, ...

*first term,  $a = 3$*

*common difference,  $d = a_2 - a_1 = 15 - 3 = 12$*

We know that,

$$a_n = a + (n-1)d$$

*Therefore,*

$$a_{54} = a + (54-1)d$$

$$\Rightarrow 3 + (53)(12)$$

$$\Rightarrow 3 + 636 = 639$$

$$a_{54} = 639 + 132 = 771$$

We have to find the term of this A.P. which is 132 more than  $a_{54}$ , i.e. 771.

Let  $n^{\text{th}}$  term be 771.

$$a_n = a + (n-1)d$$





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$$771 = 3 + (n - 1)12$$

$$768 = (n - 1)12$$

$$(n - 1) = 64$$

$$n = 65$$

Therefore, 65<sup>th</sup> term was 132 more than 54<sup>th</sup> term.

**Or another method is;**

Let  $n^{\text{th}}$  term be 132 more than 54<sup>th</sup> term.

$$n = 54 + 132/2$$

$$= 54 + 11 = 65^{\text{th}} \text{ term}$$

**12. Two APs have the same common difference. The difference between their 100<sup>th</sup> term is 100, what is the difference between their 1000<sup>th</sup> terms?**

**Solution:**

Let, the first term of two APs be  $a_1$  and  $a_2$  respectively

And the common difference of these APs be  $d$ .

For the first A.P., we know,

$$a_n = a + (n - 1)d$$

Therefore,

$$a_{100} = a_1 + (100 - 1)d$$

$$= a_1 + 99d$$

$$a_{1000} = a_1 + (1000 - 1)d$$

$$a_{1000} = a_1 + 999d$$

For second A.P., we know,

$$a_n = a + (n - 1)d$$

Therefore,

$$a_{100} = a_2 + (100 - 1)d$$

$$= a_2 + 99d$$



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$$a_{1000} = a_2 + (1000 - 1)d$$

$$= a_2 + 999d$$

Given that, difference between 100<sup>th</sup> term of the two APs = 100

Therefore,  $(a_1 + 99d) - (a_2 + 99d) = 100$

$a_1 - a_2 = 100$  ..... (i)

Difference between 1000<sup>th</sup> terms of the two APs

$(a_1 + 999d) - (a_2 + 999d) = a_1 - a_2$

From equation (i),

This difference,  $a_1 - a_2 = 100$

Hence, the difference between 1000<sup>th</sup> terms of the two A.P. will be 100.

### 13. How many three digit numbers are divisible by 7?

**Solution:**

First three-digit number that is divisible by 7 are;

First number = 105

Second number = 105 + 7 = 112

Third number = 112 + 7 = 119

Therefore, 105, 112, 119, ...

All are three digit numbers are divisible by 7 and thus, all these are terms of an A.P. having first term as 105 and common difference as 7.

As we know, the largest possible three-digit number is 999.

When we divide 999 by 7, the remainder will be 5.

Therefore, 999 - 5 = 994 is the maximum possible three-digit number that is divisible by 7.

Now the series is as follows.

105, 112, 119, ..., 994

Let 994 be the nth term of this A.P.

first term, a = 105

common difference, d = 7



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$$a_n = 994$$

$$n = ?$$

As we know,

$$a_n = a + (n-1)d$$

$$994 = 105 + (n-1)7$$

$$889 = (n-1)7$$

$$(n-1) = 127$$

$$n = 128$$

Therefore, 128 three-digit numbers are divisible by 7.

### 14. How many multiples of 4 lie between 10 and 250?

**Solution:**

The first multiple of 4 that is greater than 10 is 12.

Next multiple will be 16.

Therefore, the series formed as;

12, 16, 20, 24, ...

All these are divisible by 4 and thus, all these are terms of an A.P. with first term as 12 and common difference as 4.

When we divide 250 by 4, the remainder will be 2. Therefore,  $250 - 2 = 248$  is divisible by 4.

The series is as follows, now;

12, 16, 20, 24, ..., 248

Let 248 be the  $n^{\text{th}}$  term of this A.P.

*first term,  $a = 12$*

*common difference,  $d = 4$*

$$a_n = 248$$

As we know,

$$a_n = a + (n-1)d$$

$$248 = 12 + (n-1) \times 4$$

$$236/4 = n-1$$



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$$59 = n-1$$

$$n = 60$$

Therefore, there are 60 multiples of 4 between 10 and 250.

**15. For what value of  $n$ , are the  $n^{\text{th}}$  terms of two APs 63, 65, 67, ... and 3, 10, 17, ... equal?**

**Solution:**

Given two APs as; 63, 65, 67,... and 3, 10, 17,....

**Taking first AP,**

63, 65, 67, ...

First term,  $a = 63$

Common difference,  $d = a_2 - a_1 = 65 - 63 = 2$

We know,  $n^{\text{th}}$  term of this A.P. =  $a_n = a + (n-1)d$

$$a_n = 63 + (n-1)2 = 63 + 2n - 2$$

$$a_n = 61 + 2n \dots\dots\dots \text{(i)}$$

**Taking second AP,**

3, 10, 17, ...

First term,  $a = 3$

Common difference,  $d = a_2 - a_1 = 10 - 3 = 7$

We know that,

$n^{\text{th}}$  term of this A.P. =  $3 + (n-1)7$

$$a_n = 3 + 7n - 7$$

$$a_n = 7n - 4 \dots\dots\dots \text{(ii)}$$

Given,  $n^{\text{th}}$  term of these A.P.s are equal to each other.

Equating both these equations, we get,

$$61 + 2n = 7n - 4$$

$$61 + 4 = 5n$$

$$5n = 65$$



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$$n = 13$$

Therefore, 13<sup>th</sup> terms of both these A.P.s are equal to each other.

**16. Determine the A.P. whose third term is 16 and the 7<sup>th</sup> term exceeds the 5<sup>th</sup> term by 12.**

**Solutions:**

Given,

$$\text{Third term, } a_3 = 16$$

As we know,

$$a + (3-1)d = 16$$

$$a + 2d = 16 \dots\dots\dots (i)$$

It is given that, 7<sup>th</sup> term exceeds the 5<sup>th</sup> term by 12.

$$a_7 - a_5 = 12$$

$$[a + (7-1)d] - [a + (5-1)d] = 12$$

$$(a + 6d) - (a + 4d) = 12$$

$$2d = 12$$

$$d = 6$$

From equation (i), we get,

$$a + 2(6) = 16$$

$$a + 12 = 16$$

$$a = 4$$

Therefore, A.P. will be 4, 10, 16, 22, ...

**17. Find the 20<sup>th</sup> term from the last term of the A.P. 3, 8, 13, ..., 253.**

**Solution:**

Given A.P. is 3, 8, 13, ..., 253

Common difference,  $d = 5$ .

Therefore, we can write the given AP in reverse order as;

$$253, 248, 243, \dots, 13, 8, 5$$



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Now for the new AP,

first term,  $a = 253$

and common difference,  $d = 248 - 253 = -5$

$n = 20$

Therefore, using nth term formula, we get,

$$a_{20} = a + (20-1)d$$

$$a_{20} = 253 + (19)(-5)$$

$$a_{20} = 253 - 95$$

$$a = 158$$

Therefore, 20<sup>th</sup> term from the last term of the AP 3, 8, 13, ..., 253, is 158.

**18. The sum of 4<sup>th</sup> and 8<sup>th</sup> terms of an A.P. is 24 and the sum of the 6<sup>th</sup> and 10<sup>th</sup> terms is 44. Find the first three terms of the A.P.**

**Solution:**

We know that, the nth term of the AP is;

$$a_n = a + (n-1)d$$

$$a_4 = a + (4-1)d$$

$$a_4 = a + 3d$$

In the same way, we can write,

$$a_8 = a + 7d$$

$$a_6 = a + 5d$$

$$a_{10} = a + 9d$$

Given that,

$$a_4 + a_8 = 24$$

$$a + 3d + a + 7d = 24$$

$$2a + 10d = 24$$

$$a + 5d = 12 \dots\dots\dots (i)$$

$$a_6 + a_{10} = 44$$



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$$a + 5d + a + 9d = 44$$

$$2a + 14d = 44$$

$$a + 7d = 22 \dots\dots\dots \text{(ii)}$$

On subtracting equation (i) from (ii), we get,

$$2d = 22 - 12$$

$$2d = 10$$

$$d = 5$$

From equation (i), we get,

$$a + 5d = 12$$

$$a + 5(5) = 12$$

$$a + 25 = 12$$

$$a = -13$$

$$a_2 = a + d = -13 + 5 = -8$$

$$a_3 = a_2 + d = -8 + 5 = -3$$

Therefore, the first three terms of this A.P. are  $-13$ ,  $-8$ , and  $-3$ .

**19. Subba Rao started work in 1995 at an annual salary of Rs 5000 and received an increment of Rs 200 each year. In which year did his income reach Rs 7000?**

**Solution:**

It can be seen from the given question, that the incomes of Subba Rao increases every year by Rs.200 and hence, forms an AP.

Therefore, after 1995, the salaries of each year are;

5000, 5200, 5400, ...

Here, first term,  $a = 5000$

and common difference,  $d = 200$

Let after  $n^{\text{th}}$  year, his salary be Rs 7000.

Therefore, by the  $n^{\text{th}}$  term formula of AP,

$$a_n = a + (n-1)d$$

$$7000 = 5000 + (n-1)200$$



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$$200(n-1) = 2000$$

$$(n-1) = 10$$

$$n = 11$$

Therefore, in 11th year, his salary will be Rs 7000.

**20. Ramkali saved Rs 5 in the first week of a year and then increased her weekly saving by Rs 1.75. If in the  $n^{\text{th}}$  week, her weekly savings become Rs 20.75, find  $n$ .**

**Solution:**

Given that, Ramkali saved Rs.5 in first week and then started saving each week by Rs.1.75.

Hence,

First term,  $a = 5$

and common difference,  $d = 1.75$

Also given,

$$a_n = 20.75$$

Find,  $n = ?$

As we know, by the  $n^{\text{th}}$  term formula,

$$a_n = a + (n-1)d$$

Therefore,

$$20.75 = 5 + (n-1) \times 1.75$$

$$15.75 = (n-1) \times 1.75$$

$$(n-1) = 15.75 / 1.75 = 1575 / 175$$

$$= 63 / 7 = 9$$

$$n - 1 = 9$$

$$n = 10$$

Hence,  $n$  is 10.





### EXERCISE 5.3

1. Find the sum of the following APs.

(i) 2, 7, 12, ....., to 10 terms.

(ii) - 37, - 33, - 29, ....., to 12 terms

(iii) 0.6, 1.7, 2.8, ....., to 100 terms

(iv)  $1/15, 1/12, 1/10, \dots$ , to 11 terms

**Solutions:**

(i) Given, 2, 7, 12, ....., to 10 terms

For this A.P.,

first term,  $a = 2$

And common difference,  $d = a_2 - a_1 = 7 - 2 = 5$

$n = 10$

We know that, the formula for sum of nth term in AP series is,

$$S_n = n/2 [2a + (n-1)d]$$

$$S_{10} = 10/2 [2(2) + (10 - 1) \times 5]$$

$$= 5[4 + (9) \times (5)]$$

$$= 5 \times 49 = 245$$

(ii) Given, -37, -33, -29, ....., to 12 terms

For this A.P.,

first term,  $a = -37$

And common difference,  $d = a_2 - a_1$

$$d = (-33) - (-37)$$

$$= -33 + 37 = 4$$

$n = 12$

We know that, the formula for sum of nth term in AP series is,

$$S_n = n/2 [2a + (n-1)d]$$

$$S_{12} = 12/2 [2(-37) + (12-1) \times 4]$$

$$= 6[-74 + 11 \times 4]$$



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$$= 6[-74+44]$$

$$= 6(-30) = -180$$

(iii) Given, 0.6, 1.7, 2.8 ,..., to 100 terms

For this A.P.,

first term,  $a = 0.6$

Common difference,  $d = a_2 - a_1 = 1.7 - 0.6 = 1.1$

$$n = 100$$

We know that, the formula for sum of nth term in AP series is,

$$S_n = n/2[2a + (n-1)d]$$

$$S_{100} = 50/2 [1.2+(99) \times 1.1]$$

$$= 50[1.2+108.9]$$

$$= 50[110.1]$$

$$= 5505$$

(iv) Given,  $1/15, 1/12, 1/10, \dots$  , to 11 terms

For this A.P.,

First term,  $a = 1/5$

Common difference,  $d = a_2 - a_1 = (1/12) - (1/5) = 1/60$

And number of terms  $n = 11$

We know that, the formula for sum of nth term in AP series is,

$$S_n = n/2 [2a + (n - 1) d]$$

$$S_{11} = \frac{11}{2} \left[ 2 \left( \frac{1}{15} \right) + \frac{(11 - 1) 1}{60} \right]$$

$$= 11/2(2/15 + 10/60)$$

$$= 11/2 (9/30)$$

$$= 33/20$$

**2. Find the sums given below:**



(i)  $7 + 10\frac{1}{2} + 14 + \dots + 84$

(ii)  $34 + 32 + 30 + \dots + 10$

(iii)  $-5 + (-8) + (-11) + \dots + (-230)$

Solutions:

(i)

For this given A.P.,  $7 + 10\frac{1}{2} + 14 + \dots + 84$ ,

First term,  $a = 7$

(ii) Given,  $34 + 32 + 30 + \dots + 10$

$n^{\text{th}}$  term,  $a_n = 84$

Common difference,  $d = a_2 - a_1 = 10\frac{1}{2} - 7 = \frac{21}{2} - 7 = \frac{7}{2}$

Let 84 be the  $n^{\text{th}}$  term of this A.P., then as per the  $n^{\text{th}}$  term formula,

$$a_n = a + (n-1)d$$

$$84 = 7 + (n-1) \times \frac{7}{2}$$

$$77 = (n-1) \times \frac{7}{2}$$

$$22 = n-1$$

$$n = 23$$

We know that, sum of  $n$  term is;

$$S_n = \frac{n}{2} (a + l), l = 84$$

$$S_n = \frac{23}{2} (7+84)$$

$$S_n = (23 \times 91/2) = 2093/2$$

$$S_n = 1046\frac{1}{2}$$

For this A.P.,

first term,  $a = 34$

common difference,  $d = a_2 - a_1 = 32 - 34 = -2$

$n^{\text{th}}$  term,  $a_n = 10$

Let 10 be the  $n^{\text{th}}$  term of this A.P., therefore,



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$$a_n = a + (n-1)d$$

$$10 = 34 + (n-1)(-2)$$

$$-24 = (n-1)(-2)$$

$$12 = n - 1$$

$$n = 13$$

We know that, sum of  $n$  terms is;

$$S_n = n/2 (a + l), l = 10$$

$$= 13/2 (34 + 10)$$

$$= (13 \times 44/2) = 13 \times 22$$

$$= 286$$

(iii) Given,  $(-5) + (-8) + (-11) + \dots + (-230)$

For this A.P.,

First term,  $a = -5$

$n$ th term,  $a_n = -230$

Common difference,  $d = a_2 - a_1 = (-8) - (-5)$

$$\Rightarrow d = -8 + 5 = -3$$

Let  $-230$  be the  $n^{\text{th}}$  term of this A.P., and by the  $n^{\text{th}}$  term formula we know,

$$a_n = a + (n-1)d$$

$$-230 = -5 + (n-1)(-3)$$

$$-225 = (n-1)(-3)$$

$$(n-1) = 75$$

$$n = 76$$

And, Sum of  $n$  term,

$$S_n = n/2 (a + l)$$

$$= 76/2 [(-5) + (-230)]$$

$$= 38(-235)$$



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$$= -8930$$

### 3. In an AP

- (i) Given  $a = 5, d = 3, a_n = 50$ , find  $n$  and  $S_n$ .
- (ii) Given  $a = 7, a_{13} = 35$ , find  $d$  and  $S_{13}$ .
- (iii) Given  $a_{12} = 37, d = 3$ , find  $a$  and  $S_{12}$ .
- (iv) Given  $a_3 = 15, S_{10} = 125$ , find  $d$  and  $a_{10}$ .
- (v) Given  $d = 5, S_9 = 75$ , find  $a$  and  $a_9$ .
- (vi) Given  $a = 2, d = 8, S_n = 90$ , find  $n$  and  $a_n$ .
- (vii) Given  $a = 8, a_n = 62, S_n = 210$ , find  $n$  and  $d$ .
- (viii) Given  $a_n = 4, d = 2, S_n = -14$ , find  $n$  and  $a$ .
- (ix) Given  $a = 3, n = 8, S = 192$ , find  $d$ .
- (x) Given  $l = 28, S = 144$  and there are total 9 terms. Find  $a$ .

### Solutions:

- (i) Given that,  $a = 5, d = 3, a_n = 50$

As we know, from the formula of the  $n$ th term in an AP,

$$a_n = a + (n - 1)d,$$

Therefore, putting the given values, we get,

$$\Rightarrow 50 = 5 + (n - 1) \times 3$$

$$\Rightarrow 3(n - 1) = 45$$

$$\Rightarrow n - 1 = 15$$

$$\Rightarrow n = 16$$

Now, sum of  $n$  terms,

$$S_n = n/2 (a + a_n)$$

$$S_n = 16/2 (5 + 50) = 440$$

- (ii) Given that,  $a = 7, a_{13} = 35$

As we know, from the formula of the  $n$ th term in an AP,

$$a_n = a + (n - 1)d,$$

Therefore, putting the given values, we get,

$$\Rightarrow 35 = 7 + (13 - 1)d$$

$$\Rightarrow 12d = 28$$

$$\Rightarrow d = 28/12 = 2.33$$



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Now,  $S_n = n/2 (a+a_n)$

$$S_{13} = 13/2 (7+35) = 273$$

**(iii)** Given that,  $a_{12} = 37, d = 3$

As we know, from the formula of the  $n^{\text{th}}$  term in an AP,

$$a_n = a+(n-1)d,$$

Therefore, putting the given values, we get,

$$\Rightarrow a_{12} = a+(12-1)3$$

$$\Rightarrow 37 = a+33$$

$$\Rightarrow a = 4$$

Now, sum of  $n^{\text{th}}$  term,

$$S_n = n/2 (a+a_n)$$

$$S_n = 12/2 (4+37)$$

$$= 246$$

**(iv)** Given that,  $a_3 = 15, S_{10} = 125$

As we know, from the formula of the  $n^{\text{th}}$  term in an AP,

$$a_n = a +(n-1)d,$$

Therefore, putting the given values, we get,

$$a_3 = a+(3-1)d$$

$$15 = a+2d \dots\dots\dots \textbf{(i)}$$

Sum of the  $n^{\text{th}}$  term,

$$S_n = n/2 [2a+(n-1)d]$$

$$S_{10} = 10/2 [2a+(10-1)d]$$

$$125 = 5(2a+9d)$$

$$25 = 2a+9d \dots\dots\dots \textbf{(ii)}$$

On multiplying equation **(i)** by **(ii)**, we will get;

$$30 = 2a+4d \dots\dots\dots \textbf{(iii)}$$



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By subtracting equation (iii) from (ii), we get,

$$-5 = 5d$$

$$d = -1$$

From equation (i),

$$15 = a + 2(-1)$$

$$15 = a - 2$$

$$a = 17 = \text{First term}$$

$$a_{10} = a + (10-1)d$$

$$a_{10} = 17 + (9)(-1)$$

$$a_{10} = 17 - 9 = 8$$

(v) Given that,  $d = 5$ ,  $S_9 = 75$

As, sum of  $n$  terms in AP is,

$$S_n = n/2 [2a + (n-1)d]$$

Therefore, the sum of first nine terms are;

$$S_9 = 9/2 [2a + (9-1)5]$$

$$25 = 3(a+20)$$

$$25 = 3a + 60$$

$$3a = 25 - 60$$

$$a = -35/3$$

As we know, the  $n^{\text{th}}$  term can be written as;

$$a_n = a + (n-1)d$$

$$a_9 = a + (9-1)(5)$$

$$= -35/3 + 8(5)$$

$$= -35/3 + 40$$

$$= (35 + 120/3) = 85/3$$

(vi) Given that,  $a = 2$ ,  $d = 8$ ,  $S_n = 90$



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As, sum of  $n$  terms in an AP is,

$$S_n = n/2 [2a + (n - 1)d]$$

$$90 = n/2 [2a + (n - 1)d]$$

$$\Rightarrow 180 = n(4 + 8n - 8) = n(8n - 4) = 8n^2 - 4n$$

$$\Rightarrow 8n^2 - 4n - 180 = 0$$

$$\Rightarrow 2n^2 - n - 45 = 0$$

$$\Rightarrow 2n^2 - 10n + 9n - 45 = 0$$

$$\Rightarrow 2n(n - 5) + 9(n - 5) = 0$$

$$\Rightarrow (n - 5)(2n + 9) = 0$$

So,  $n = 5$  (as  $n$  only be a positive integer)

$$\therefore a_5 = 8 + 5 \times 4 = 34$$

**(vii)** Given that,  $a = 8$ ,  $a_n = 62$ ,  $S_n = 210$

As, sum of  $n$  terms in an AP is,

$$S_n = n/2 (a + a_n)$$

$$210 = n/2 (8 + 62)$$

$$\Rightarrow 35n = 210$$

$$\Rightarrow n = 210/35 = 6$$

$$\text{Now, } 62 = 8 + 5d$$

$$\Rightarrow 5d = 62 - 8 = 54$$

$$\Rightarrow d = 54/5 = 10.8$$

**(viii)** Given that,  $n^{\text{th}}$  term,  $a_n = 4$ , common difference,  $d = 2$ , sum of  $n$  terms,  $S_n = -14$ .

As we know, from the formula of the  $n^{\text{th}}$  term in an AP,

$$a_n = a + (n - 1)d,$$

Therefore, putting the given values, we get,

$$4 = a + (n - 1)2$$

$$4 = a + 2n - 2$$





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$$a+2n = 6$$

$$a = 6 - 2n \dots\dots\dots (i)$$

As we know, the sum of n terms is;

$$S_n = n/2 (a+a_n)$$

$$-14 = n/2 (a+4)$$

$$-28 = n (a+4)$$

$$-28 = n (6 - 2n + 4) \text{ {From equation (i)}}$$

$$-28 = n (- 2n + 10)$$

$$-28 = - 2n^2 + 10n$$

$$2n^2 - 10n - 28 = 0$$

$$n^2 - 5n - 14 = 0$$

$$n^2 - 7n + 2n - 14 = 0$$

$$n (n-7) + 2(n-7) = 0$$

$$(n-7)(n+2) = 0$$

Either  $n - 7 = 0$  or  $n + 2 = 0$

$$n = 7 \text{ or } n = -2$$

However,  $n$  can neither be negative nor fractional.

Therefore,  $n = 7$

From equation (i), we get

$$a = 6 - 2n$$

$$a = 6 - 2(7)$$

$$= 6 - 14$$

$$= -8$$

(ix) Given that, first term,  $a = 3$ ,

Number of terms,  $n = 8$

And sum of n terms,  $S = 192$

As we know,



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$$S_n = n/2 [2a+(n-1)d]$$

$$192 = 8/2 [2 \times 3 + (8-1)d]$$

$$192 = 4[6+7d]$$

$$48 = 6+7d$$

$$42 = 7d$$

$$d = 6$$

(x) Given that,  $l = 28, S = 144$  and there are total of 9 terms.

*Sum of n terms formula,*

$$S_n = n/2 (a + l)$$

$$144 = 9/2(a+28)$$

$$(16) \times (2) = a+28$$

$$32 = a+28$$

$$a = 4$$

**4. How many terms of the AP. 9, 17, 25 ... must be taken to give a sum of 636?**

**Solutions:**

Let there be  $n$  terms of the AP. 9, 17, 25 ...

For this A.P.,

First term,  $a = 9$

*Common difference,  $d = a_2 - a_1 = 17 - 9 = 8$*

As, the sum of  $n$  terms, is;

$$S_n = n/2 [2a+(n-1)d]$$

$$636 = n/2 [2 \times a + (8-1) \times 8]$$

$$636 = n/2 [18 + (n-1) \times 8]$$

$$636 = n [9 + 4n - 4]$$

$$636 = n (4n + 5)$$

$$4n^2 + 5n - 636 = 0$$



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$$4n^2 + 53n - 48n - 636 = 0$$

$$n(4n + 53) - 12(4n + 53) = 0$$

$$(4n + 53)(n - 12) = 0$$

Either  $4n + 53 = 0$  or  $n - 12 = 0$

$$n = (-53/4) \text{ or } n = 12$$

$n$  cannot be negative or fraction, therefore,  $n = 12$  only.

**5. The first term of an AP is 5, the last term is 45 and the sum is 400. Find the number of terms and the common difference.**

**Solution:**

Given that,

*first term,  $a = 5$*

*last term,  $l = 45$*

*Sum of the AP,  $S_n = 400$*

As we know, the sum of AP formula is;

$$S_n = n/2 (a+l)$$

$$400 = n/2(5+45)$$

$$400 = n/2(50)$$

*Number of terms,  $n = 16$*

As we know, the last term of AP series can be written as;

$$l = a + (n - 1)d$$

$$45 = 5 + (16 - 1)d$$

$$40 = 15d$$

*Common difference,  $d = 40/15 = 8/3$*

**6. The first and the last term of an AP are 17 and 350 respectively. If the common difference is 9, how many terms are there and what is their sum?**

**Solution:**

Given that,



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First term,  $a = 17$

Last term,  $l = 350$

Common difference,  $d = 9$

Let there be  $n$  terms in the A.P., thus the formula for last term can be written as;

$$l = a + (n - 1)d$$

$$350 = 17 + (n - 1)9$$

$$333 = (n - 1)9$$

$$(n - 1) = 37$$

$$n = 38$$

$$S_n = n/2 (a + l)$$

$$S_{38} = 38/2 (17 + 350)$$

$$= 19 \times 367$$

$$= 6973$$

Thus, this A.P. contains 38 terms and the sum of the terms of this A.P. is 6973.

**7. Find the sum of first 22 terms of an AP in which  $d = 7$  and 22<sup>nd</sup> term is 149.**

**Solution:**

Given,

Common difference,  $d = 7$

22<sup>nd</sup> term,  $a_{22} = 149$

Sum of first 22 term,  $S_{22} = ?$

By the formula of  $n$ th term,

$$a_n = a + (n - 1)d$$

$$a_{22} = a + (22 - 1)d$$

$$149 = a + 21 \times 7$$

$$149 = a + 147$$

$$a = 2 = \text{First term}$$

Sum of  $n$  terms,



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$$S_n = n/2(a+a_n)$$

$$S_{22} = 22/2 (2+149)$$

$$= 11 \times 151$$

$$= 1661$$

**8. Find the sum of first 51 terms of an AP whose second and third terms are 14 and 18 respectively.**

**Solution:**

Given that,

$$\text{Second term, } a_2 = 14$$

$$\text{Third term, } a_3 = 18$$

$$\text{Common difference, } d = a_3 - a_2 = 18 - 14 = 4$$

$$a_2 = a + d$$

$$14 = a + 4$$

$$a = 10 = \text{First term}$$

Sum of n terms;

$$S_n = n/2 [2a + (n - 1)d]$$

$$S_{51} = 51/2 [2 \times 10 + (51 - 1) 4]$$

$$= 51/2 [20 + (50) \times 4]$$

$$= 51 \times 220/2$$

$$= 51 \times 110$$

$$= 5610$$

**9. If the sum of first 7 terms of an AP is 49 and that of 17 terms is 289, find the sum of first n terms.**

**Solution:**

Given that,

$$S_7 = 49$$

$$S_{17} = 289$$

We know, Sum of n terms;

$$S_n = n/2 [2a + (n - 1)d]$$



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Therefore,

$$S_7 = \frac{7}{2} [2a + (n - 1)d]$$

$$S_7 = \frac{7}{2} [2a + (7 - 1)d]$$

$$49 = \frac{7}{2} [2a + 6d]$$

$$7 = (a + 3d)$$

$$a + 3d = 7 \dots\dots\dots \text{(i)}$$

In the same way,

$$S_{17} = \frac{17}{2} [2a + (17 - 1)d]$$

$$289 = \frac{17}{2} (2a + 16d)$$

$$17 = (a + 8d)$$

$$a + 8d = 17 \dots\dots\dots \text{(ii)}$$

Subtracting equation (i) from equation (ii),

$$5d = 10$$

$$d = 2$$

From equation (i), we can write it as;

$$a + 3(2) = 7$$

$$a + 6 = 7$$

$$a = 1$$

Hence,

$$S_n = \frac{n}{2} [2a + (n - 1)d]$$

$$= \frac{n}{2} [2(1) + (n - 1) \times 2]$$

$$= \frac{n}{2} (2 + 2n - 2)$$

$$= \frac{n}{2} (2n)$$

$$= n^2$$

**10. Show that  $a_1, a_2, \dots, a_n, \dots$  form an AP where  $a_n$  is defined as below**



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(i)  $a_n = 3+4n$

(ii)  $a_n = 9-5n$

Also find the sum of the first 15 terms in each case.

**Solutions:**

(i)  $a_n = 3+4n$

$$a_1 = 3+4(1) = 7$$

$$a_2 = 3+4(2) = 3+8 = 11$$

$$a_3 = 3+4(3) = 3+12 = 15$$

$$a_4 = 3+4(4) = 3+16 = 19$$

We can see here, the common difference between the terms are;

$$a_2 - a_1 = 11-7 = 4$$

$$a_3 - a_2 = 15-11 = 4$$

$$a_4 - a_3 = 19-15 = 4$$

Hence,  $a_{k+1} - a_k$  is the same value every time. Therefore, this is an AP with common difference as 4 and first term as 7.

Now, we know, the sum of nth term is;

$$S_n = n/2[2a+(n-1)d]$$

$$S_{15} = 15/2[2(7)+(15-1) \times 4]$$

$$= 15/2[(14)+56]$$

$$= 15/2(70)$$

$$= 15 \times 35$$

$$= 525$$

(ii)  $a_n = 9-5n$

$$a_1 = 9-5 \times 1 = 9-5 = 4$$

$$a_2 = 9-5 \times 2 = 9-10 = -1$$

$$a_3 = 9-5 \times 3 = 9-15 = -6$$

$$a_4 = 9-5 \times 4 = 9-20 = -11$$

We can see here, the common difference between the terms are;



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$$a_2 - a_1 = -1 - 4 = -5$$

$$a_3 - a_2 = -6 - (-1) = -5$$

$$a_4 - a_3 = -11 - (-6) = -5$$

Hence,  $a_{k+1} - a_k$  is same every time. Therefore, this is an A.P. with common difference as  $-5$  and first term as  $4$ .

Now, we know, the sum of  $n$ th term is;

$$S_n = n/2 [2a + (n-1)d]$$

$$S_{15} = 15/2 [2(4) + (15-1)(-5)]$$

$$= 15/2 [8 + 14(-5)]$$

$$= 15/2 (8 - 70)$$

$$= 15/2 (-62)$$

$$= 15(-31)$$

$$= -465$$

**11. If the sum of the first  $n$  terms of an AP is  $4n - n^2$ , what is the first term (that is  $S_1$ )? What is the sum of first two terms? What is the second term? Similarly find the 3<sup>rd</sup>, the 10<sup>th</sup> and the  $n$ <sup>th</sup> terms.**

**Solution:**

Given that,

$$S_n = 4n - n^2$$

$$\text{First term, } a = S_1 = 4(1) - (1)^2 = 4 - 1 = 3$$

$$\text{Sum of first two terms} = S_2 = 4(2) - (2)^2 = 8 - 4 = 4$$

$$\text{Second term, } a_2 = S_2 - S_1 = 4 - 3 = 1$$

$$\text{Common difference, } d = a_2 - a = 1 - 3 = -2$$

$$\text{N<sup>th</sup> term, } a_n = a + (n-1)d$$

$$= 3 + (n-1)(-2)$$

$$= 3 - 2n + 2$$

$$= 5 - 2n$$

$$\text{Therefore, } a_3 = 5 - 2(3) = 5 - 6 = -1$$

$$a_{10} = 5 - 2(10) = 5 - 20 = -15$$





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Hence, the sum of first two terms is 4. The second term is 1.

The 3<sup>rd</sup>, the 10<sup>th</sup>, and the  $n^{\text{th}}$  terms are  $-1$ ,  $-15$ , and  $5 - 2n$  respectively.

**12. Find the sum of first 40 positive integers divisible by 6.**

**Solution:**

The positive integers that are divisible by 6 are 6, 12, 18, 24 ....

We can see here, that this series forms an A.P. whose first term is 6 and common difference is 6.

$$a = 6$$

$$d = 6$$

$$S_{40} = ?$$

By the formula of sum of  $n$  terms, we know,

$$S_n = n/2 [2a + (n - 1)d]$$

Therefore, putting  $n = 40$ , we get,

$$S_{40} = 40/2 [2(6) + (40-1)6]$$

$$= 20[12 + (39)(6)]$$

$$= 20(12 + 234)$$

$$= 20 \times 246$$

$$= 4920$$

**13. Find the sum of first 15 multiples of 8.**

**Solution:**

The multiples of 8 are 8, 16, 24, 32...

The series is in the form of AP, having first term as 8 and common difference as 8.

Therefore,  $a = 8$

$$d = 8$$

$$S_{15} = ?$$

By the formula of sum of  $n^{\text{th}}$  term, we know,

$$S_n = n/2 [2a + (n-1)d]$$



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$$\begin{aligned}S_{15} &= 15/2 [2(8) + (15-1)8] \\&= 15/2[16 + (14)(8)] \\&= 15/2[16 + 112] \\&= 15(128)/2 \\&= 15 \times 64 \\&= 960\end{aligned}$$

**14. Find the sum of the odd numbers between 0 and 50.**

**Solution:**

The odd numbers between 0 and 50 are 1, 3, 5, 7, 9 ... 49.

Therefore, we can see that these odd numbers are in the form of A.P.

Hence,

First term,  $a = 1$

Common difference,  $d = 2$

Last term,  $l = 49$

By the formula of last term, we know,

$$l = a + (n-1)d$$

$$49 = 1 + (n-1)2$$

$$48 = 2(n-1)$$

$$n-1 = 24$$

$$n = 25 = \text{Number of terms}$$

By the formula of sum of nth term, we know,

$$S_n = n/2(a+l)$$

$$S_{25} = 25/2 (1+49)$$

$$= 25(50)/2$$

$$= (25)(25)$$

$$= 625$$



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**15. A contract on construction job specifies a penalty for delay of completion beyond a certain date as follows: Rs. 200 for the first day, Rs. 250 for the second day, Rs. 300 for the third day, etc., the penalty for each succeeding day being Rs. 50 more than for the preceding day. How much money the contractor has to pay as penalty, if he has delayed the work by 30 days.**

**Solution:**

We can see, that the given penalties are in the form of A.P. having first term as 200 and common difference as 50.

Therefore,  $a = 200$  and  $d = 50$

Penalty that has to be paid if contractor has delayed the work by 30 days =  $S_{30}$

By the formula of sum of nth term, we know,

$$S_n = n/2[2a+(n-1)d]$$

Therefore,

$$S_{30} = 30/2[2(200)+(30-1)50]$$

$$= 15[400+1450]$$

$$= 15(1850)$$

$$= 27750$$

Therefore, the contractor has to pay Rs 27750 as penalty.

**16. A sum of Rs 700 is to be used to give seven cash prizes to students of a school for their overall academic performance. If each prize is Rs 20 less than its preceding prize, find the value of each of the prizes.**

**Solution:**

Let the cost of 1<sup>st</sup> prize be Rs.  $P$ .

Cost of 2<sup>nd</sup> prize = Rs.  $P - 20$

And cost of 3<sup>rd</sup> prize = Rs.  $P - 40$

We can see that the cost of these prizes are in the form of A.P., having common difference as  $-20$  and first term as  $P$ .

Thus,  $a = P$  and  $d = -20$

Given that,  $S_7 = 700$

By the formula of sum of nth term, we know,

$$S_n = n/2 [2a + (n-1)d]$$

$$7/2 [2a + (7-1)d] = 700$$



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$$\frac{[2a + (6)(-20)]}{2} = 100$$

$$a + 3(-20) = 100$$

$$a - 60 = 100$$

$$a = 160$$

Therefore, the value of each of the prizes was Rs 160, Rs 140, Rs 120, Rs 100, Rs 80, Rs 60, and Rs 40.

**17. In a school, students thought of planting trees in and around the school to reduce air pollution. It was decided that the number of trees, that each section of each class will plant, will be the same as the class, in which they are studying, e.g., a section of class I will plant 1 tree, a section of class II will plant 2 trees and so on till class XII. There are three sections of each class. How many trees will be planted by the students?**

**Solution:**

It can be observed that the number of trees planted by the students is in an AP.

1, 2, 3, 4, 5, .....12

First term,  $a = 1$

Common difference,  $d = 2 - 1 = 1$

$$S_n = n/2 [2a + (n-1)d]$$

$$S_{12} = 12/2 [2(1) + (12-1)(1)]$$

$$= 6(2+11)$$

$$= 6(13)$$

$$= 78$$

Therefore, number of trees planted by 1 section of the classes = 78

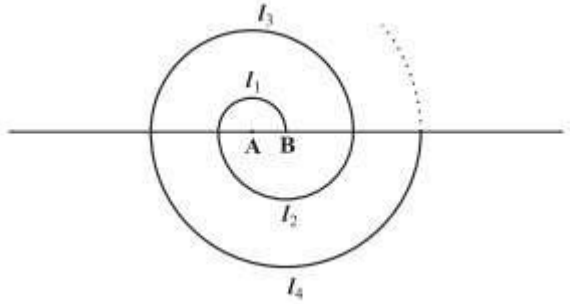
Number of trees planted by 3 sections of the classes =  $3 \times 78 = 234$

Therefore, 234 trees will be planted by the students.

**18. A spiral is made up of successive semicircles, with centres alternately at A and B, starting with centre at A of radii 0.5, 1.0 cm, 1.5 cm, 2.0 cm, ..... as shown in figure. What is the total length of such a spiral made up of thirteen consecutive semicircles? (Take  $\pi = 22/7$ )**



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### Solution:

We know,

Perimeter of a semi-circle =  $\pi r$

Therefore,

$$P_1 = \pi(0.5) = \pi/2 \text{ cm}$$

$$P_2 = \pi(1) = \pi \text{ cm}$$

$$P_3 = \pi(1.5) = 3\pi/2 \text{ cm}$$

Where,  $P_1, P_2, P_3$  are the lengths of the semi-circles.

Hence we got a series here, as,

$$\pi/2, \pi, 3\pi/2, 2\pi, \dots$$

$$P_1 = \pi/2 \text{ cm}$$

$$P_2 = \pi \text{ cm}$$

$$\text{Common difference, } d = P_2 - P_1 = \pi - \pi/2 = \pi/2$$

$$\text{First term} = P_1 = a = \pi/2 \text{ cm}$$

By the sum of n term formula, we know,

$$S_n = n/2 [2a + (n - 1)d]$$

Therefore, Sum of the length of 13 consecutive circles is;

$$S_{13} = 13/2 [2(\pi/2) + (13 - 1)\pi/2]$$

$$= 13/2 [\pi + 6\pi]$$

$$= 13/2 (7\pi)$$

$$= 13/2 \times 7 \times 22/7$$



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= 143 cm

19. 200 logs are stacked in the following manner: 20 logs in the bottom row, 19 in the next row, 18 in the row next to it and so on. In how many rows are the 200 logs placed and how many logs are in the top row?



### Solution:

We can see that the numbers of logs in rows are in the form of an A.P. 20, 19, 18...

For the given A.P.,

First term,  $a = 20$  and common difference,  $d = a_2 - a_1 = 19 - 20 = -1$

Let a total of 200 logs be placed in  $n$  rows.

Thus,  $S_n = 200$

By the sum of  $n$ th term formula,

$$S_n = n/2 [2a + (n - 1)d]$$

$$S_{12} = 12/2 [2(20) + (n - 1)(-1)]$$

$$400 = n (40 - n + 1)$$

$$400 = n (41 - n)$$

$$400 = 41n - n^2$$

$$n^2 - 41n + 400 = 0$$

$$n^2 - 16n - 25n + 400 = 0$$

$$n(n - 16) - 25(n - 16) = 0$$

$$(n - 16)(n - 25) = 0$$

Either  $(n - 16) = 0$  or  $n - 25 = 0$

$$n = 16 \text{ or } n = 25$$

By the  $n$ th term formula,

$$a_n = a + (n - 1)d$$



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$$a_{16} = 20 + (16 - 1)(-1)$$

$$a_{16} = 20 - 15$$

$$a_{16} = 5$$

Similarly, the 25<sup>th</sup> term could be written as;

$$a_{25} = 20 + (25 - 1)(-1)$$

$$a_{25} = 20 - 24$$

$$= -4$$

### Solution:

The distances of potatoes from the bucket are 5, 8, 11, 14..., which is in the form of AP.

Given, the distance run by the competitor for collecting these potatoes are two times of the distance at which the potatoes have been kept.

Therefore, distances to be run w.r.t distances of potatoes, could be written as;

$$10, 16, 22, 28, 34, \dots$$

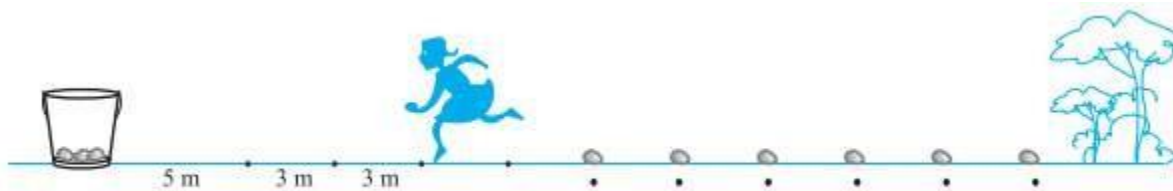
Hence, the first term,  $a = 10$  and  $d = 16 - 10 = 6$

$$S_{10} = ?$$

It can be seen, the number of logs in 16<sup>th</sup> row is 5 as the numbers cannot be negative.

Therefore, 200 logs can be placed in 16 rows and the number of logs in the 16<sup>th</sup> row is 5.

**20. In a potato race, a bucket is placed at the starting point, which is 5 m from the first potato and other potatoes are placed 3 m apart in a straight line. There are ten potatoes in the line.**



A competitor starts from the bucket, picks up the nearest potato, runs back with it, drops it in the bucket, runs back to pick up the next potato, runs to the bucket to drop it in, and she continues in the same way until all the potatoes are in the bucket. What is the total distance the competitor has to run?

[Hint: to pick up the first potato and the second potato, the total distance (in metres) run by a competitor is  $2 \times 5 + 2 \times (5 + 3)$ ]



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By the formula of sum of n terms, we know,

$$S_{10} = 10/2 [2(10)+(10 -1)(6)]$$

$$= 5[20+54]$$

$$= 5(74)$$

$$= 370$$

Therefore, the competitor will run a total distance of 370 m.





EXERCISE 5.4

1. Which term of the AP: 121, 117, 113, . . . , is its first negative term? [Hint: Find n for  $a_n < 0$ ]

**Solution:**

Given the AP series is 121, 117, 113, . . . ,

Thus, first term,  $a = 121$

Common difference,  $d = 117-121 = -4$

By the nth term formula,

$$a_n = a + (n - 1)d$$

Therefore,

$$a_n = 121 + (n - 1)(-4)$$

$$= 121 - 4n + 4$$

$$= 125 - 4n$$

To find the first negative term of the series,  $a_n < 0$

Therefore,

$$125 - 4n < 0$$

$$125 < 4n$$

$$n > 125/4$$

$$n > 31.25$$

Therefore, the first negative term of the series is 32<sup>nd</sup> term.

2. The sum of the third and the seventh terms of an AP is 6 and their product is 8. Find the sum of first sixteen terms of the AP.

**Solution:**

From the given statements, we can write,

$$a_3 + a_7 = 6 \dots\dots\dots (i)$$

And

$$a_3 \times a_7 = 8 \dots\dots\dots (ii)$$

By the nth term formula,



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$$a_n = a + (n-1)d$$

Third term,  $a_3 = a + (3-1)d$

$$a_3 = a + 2d \dots\dots\dots (iii)$$

And Seventh term,  $a_7 = a + (7-1)d$

$$a_7 = a + 6d \dots\dots\dots (iv)$$

From equation (iii) and (iv), putting in equation(i), we get,

$$a + 2d + a + 6d = 6$$

$$2a + 8d = 6$$

$$a + 4d = 3$$

or

$$a = 3 - 4d \dots\dots\dots (v)$$

Again putting the eq.(iii) and (iv), in eq. (ii), we get,

$$(a + 2d) \times (a + 6d) = 8$$

Putting the value of a from equation (v), we get,

$$(3 - 4d + 2d) \times (3 - 4d + 6d) = 8$$

$$(3 - 2d) \times (3 + 2d) = 8$$

$$3^2 - 2d^2 = 8$$

$$9 - 4d^2 = 8$$

$$4d^2 = 1$$

$$d = 1/2 \text{ or } -1/2$$

Now, by putting both the values of d, we get,

$$a = 3 - 4d = 3 - 4(1/2) = 3 - 2 = 1, \text{ when } d = 1/2$$

$$a = 3 - 4d = 3 - 4(-1/2) = 3 + 2 = 5, \text{ when } d = -1/2$$

We know, the sum of nth term of AP is;

$$S_n = n/2 [2a + (n-1)d]$$

So, when  $a = 1$  and  $d = 1/2$



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Then, the sum of first 16 terms are;

$$S_{16} = 16/2 [2 + (16-1)1/2] = 8(2+15/2) = 76$$

And when  $a = 5$  and  $d = -1/2$

Then, the sum of first 16 terms are;

$$S_{16} = 16/2 [2(5) + (16-1)(-1/2)] = 8(5/2) = 20$$

**3. A ladder has rungs 25 cm apart. (see Fig. 5.7). The rungs decrease uniformly in length from 45 cm at the bottom to 25 cm at the top. If the top and the bottom rungs are**

Given, Distance between the rungs of the ladder is 25cm.

Distance between the top rung and bottom rung of the ladder is =

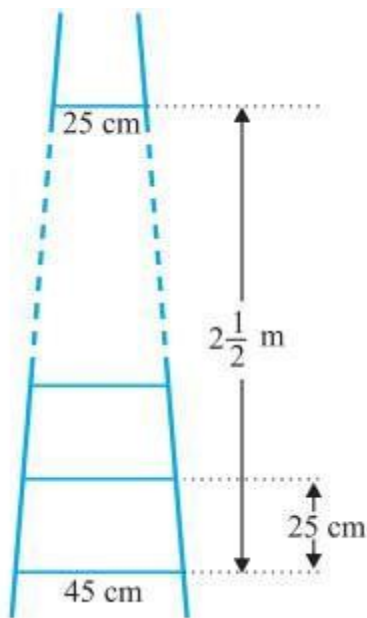
$$2\frac{1}{2}\text{m} = 2\frac{1}{2} \times 100\text{ cm} \\ = 5/2 \times 100\text{cm}$$

$$= 250\text{cm}$$

Therefore, total number of rungs =  $250/25 + 1 = 11$

As we can see from the figure, the ladder has rungs in decreasing order from top to bottom. Thus, we can conclude now, that the rungs are decreasing in an order of AP.

$2\frac{1}{2}\text{m}$  apart, what is the length of the wood required for the rungs? [Hint: Number of rungs =  $-250/25$  ].



**Solution:**



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And the length of the wood required for the rungs will be equal to the sum of the terms of AP series formed.

So,

First term,  $a = 45$

Last term,  $l = 25$

Number of terms,  $n = 11$

Now, as we know, sum of  $n$ th terms is equal to,

$$S_n = n/2(a + l)$$

$$S_n = 11/2(45 + 25) = 11/2(70) = 385 \text{ cm}$$

Hence, the length of the wood required for the rungs is 385cm.

**4. The houses of a row are numbered consecutively from 1 to 49. Show that there is a value of  $x$  such that the sum of the numbers of the houses preceding the house numbered  $x$  is equal to the sum of the numbers of the houses following it. Find this value of  $x$ . [Hint :  $S_x - 1 = S_{49} - S_x$  ]**

**Solution:**

Given,

Row houses are numbers from 1,2,3,4,5.....49.

Thus we can see the houses numbered in a row are in the form of AP.

So,

First term,  $a = 1$

Common difference,  $d=1$

Let us say the number of  $x^{\text{th}}$  houses can be represented as;

$$\text{Sum of } n\text{th term of AP} = n/2[2a + (n-1)d]$$

$$\text{Sum of number of houses beyond } x \text{ house} = S_{x-1}$$

$$= (x-1)/2[2(1) + (x-1-1)1]$$

$$= (x-1)/2 [2+x-2]$$

$$= x(x-1)/2 \dots\dots\dots (i)$$

By the given condition, we can write,

$$S_{49} - S_x = \{49/2[2(1) + (49-1)1]\} - \{x/2[2(1) + (x-1)1]\}$$



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$$= 25(49) - x(x + 1)/2 \dots\dots\dots (ii)$$



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As per the given condition, eq.(i) and eq(ii) are equal to each other;

Therefore,

$$x(x-1)/2 = 25(49) - x(x+1)/2$$

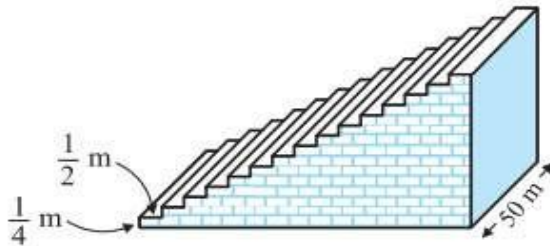
$$x = \pm 35$$

As we know, the number of houses cannot be a negative number. Hence, the value of x is 35.

**5. A small terrace at a football ground comprises of 15 steps each of which is 50 m long and built of solid concrete. Each step has a rise of 14 m and a tread of 12 m. (see Fig. 5.8). Calculate the total volume of concrete required to build the terrace. [Hint : Volume of concrete required to build the first step =  $\frac{1}{4} \times \frac{1}{2} \times 50 \text{ m}^3$ .]**

Volume of concrete required to build the first step =  $\frac{1}{4} \times \frac{1}{2} \times 50 = 25/4$

Volume of concrete required to build the second step =  $\frac{1}{4} \times 1 \times 50 = 25/2$



### Solution:

As we can see from the given figure, the first step is  $\frac{1}{2}$  m wide, 2<sup>nd</sup> step is 1 m wide and 3<sup>rd</sup> step is  $\frac{3}{2}$  m wide. Thus we can understand that the width of step by  $\frac{1}{2}$  m each time when height is  $\frac{1}{4}$  m. And also, given length of the steps is 50 m all the time. So, the width of steps forms a series AP in such a way that;

$$\frac{1}{2}, 1, \frac{3}{2}, 2, \dots\dots$$

Volume of steps = Volume of Cuboid

= Length  $\times$  Breadth

Volume of concrete required to build the second step =  $\frac{1}{4} \times \frac{3}{2} \times 50 = 75/4$

Now, we can see the volumes of concrete required to build the steps, are in AP series;

$$25/4, 25/2, 75/4, \dots\dots$$

Thus, applying the AP series concept,

First term, a =  $25/4$



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Common difference,  $d = 25/2 - 25/4 = 25/4$

As we know, the sum of  $n$  terms is;

$$S_n = n/2[2a+(n-1)d] = 15/2(2 \times (25/4) + (15/2 - 1)25/4)$$

Upon solving, we get,

$$S_n = 15/2 (100)$$

$$S_n = 750$$

Hence, the total volume of concrete required to build the terrace is  $750 \text{ m}^3$ .